

15/ENG04/002

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ELECTRICAL ELECTRONICS ENGINEERING

ENG 381 ASS

$$1.) \frac{d^2y}{dx^2} - \frac{dy}{dx} - 2y = 8$$

$$m^2 - m - 2 = 0$$

$$m^2 - 2m + m - 2 = 0$$

$$m(m-2) + 1(m-2) = 0$$

$$(m+1)(m-2) = 0$$

$$m_1 = -1, m_2 = 2$$

$$y = Ae^{m_1x} + Be^{m_2x}$$

$$C.F: y = Ae^{2x} + Be^{-x}$$

$$P.I: y = C$$

$$\frac{dy}{dx} = 0$$

$$\frac{d^2y}{dx^2} = 0$$

$$0 - 0 - 2C = 8$$

$$-2C = 8$$

$$C = -4$$

The general solution:

$$\therefore G.S = C.F + P.I$$

$$G.S = y = Ae^{2x} + Be^{-x} - 4$$

$$2.) \frac{d^2y}{dx^2} - 4y = 10e^{3x}$$

$$C.F: m^2 - 4 = 0$$

$$m^2 = 4$$

$$m = 2$$

$$C.F: y = A \cosh 2x + B \sinh 2x$$

$$P.I: y = ce^{2x}$$

$$\frac{dy}{dx} = 2ce^{3x}$$

$$\frac{d^2y}{dx^2} = 9ce^{3x}$$

$$9ce^{3x} + 3ce^{3x} =$$

$$9ce^{3x} - 4ce^{2x} = 10e^{2x}$$

$$5ce^{3x} = 10e^{2x}$$

$$5c = 10$$

$$c = 2$$

$$\therefore G.S: y = A \cosh 2x + B \sinh 2x + 2e^{3x}$$

$$3) \frac{dy}{dx} + 2\frac{dy}{dx} + y = e^{-2x}$$

C.F:

$$m^2 + 2m + 1 = 0$$

$$m^2 + m + m + 1 = 0$$

$$m(m+1) + 1(m+1) = 0$$

$$(m+1)(m+1) = 0$$

$$m_{1,2} = -1$$

$$y = e^{-x}(A+Bx)$$

P.I: $y = ce^{-2x}$

$$\frac{dy}{dx} = -2ce^{-2x}$$

$$\frac{d^2y}{dx^2} = 4ce^{-2x}$$

$$4ce^{-2x} + 2(-2ce^{-2x}) + ce^{-2x} = e^{-2x}$$

$$4ce^{-2x} - 4ce^{-2x} + ce^{-2x} = e^{-2x}$$

$$ce^{-2x} = e^{-2x}$$

$$c = 1$$

$$\therefore G.S = y = e^{-x}(A+Bx) + e^{-2x}$$

$$4) \frac{d^2y}{dx^2} + 25y = 5x^2 + x$$

C.F: $m^2 + 25 = 0$

$$m^2 = -25$$

$$m_{1,2} = \pm j5$$

$$y = A \cos 5x + B \sin 5x$$

P.I: $y = Cx^2 + Dx + E$

$$\frac{dy}{dx} = 2Cx + D$$

$$\frac{d^2y}{dx^2} = 2C$$

$$2C + 25(2Cx + D) = 5x^2 + x$$

$$2C + 50Cx + 25D = 5x^2 + x$$

$$2C + 25(Cx^2 + Dx + E) = 5x^2 + x$$

$$2C + 25Cx^2 + 25Dx + 25E = 5x^2 + x$$

$$25Cx^2 + 25Dx + 2C + 25E = 5x^2 + x$$

Comparing both sides

$$25C = 5 \quad \dots \dots \text{--- (1)}$$

$$C = 1/5 \quad \dots \dots \text{--- (1)}$$

$$25D = 1$$

$$D = 1/25 \quad \dots \dots \text{--- (2)}$$

$$2C + 25E = 0 \quad \dots \dots \text{--- (3)}$$

Subst. (1) into (3)

$$2(1/5) + 25E = 0$$

$$2/5 + 25E = 0$$

$$25E = -2/5$$

$$E = -2/125$$

$$\therefore G.S = y = A \cos 5x + B \sin 5x + 1/5 x^2 + 1/25 x - 2/125$$

$$5) \frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = 4\sin x$$

C.F:

$$m^2 - 2m + 1 = 0$$

$$m^2 - m - m + 1 = 0$$

$$m(m-1) - 1(m-1) = 0$$

$$(m-1)(m-1) = 0$$

$$m = 1 \text{ twice}$$

C.F: $y = e^x(A+Bx)$

P.I: $y = C\cos x + D\sin x$

$$\frac{dy}{dx} = -C\sin x + D\cos x$$

$$\frac{d^2y}{dx^2} = -C\cos x - D\sin x$$

$$-C\cos x - D\sin x + 2\sin x + D\cos x + C\cos x + D\sin x = 4\sin x$$

$$+2C\sin x + 2D\cos x = 4\sin x$$

Comparing both sides

$$+2C = 4$$

$$C = 2$$

$$2D = 0$$

$$D = 0$$

G.S: $y = e^x(A+Bx) + 2\cos x$

$$6) \frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 5y = 2e^{-2x}$$

$$(F.m^2 + 4m + 5 = 0)$$

$$m = \frac{-4 \pm \sqrt{(-4)^2 - 4(1)(5)}}{2(1)}$$

$$m = \frac{-4 \pm \sqrt{16 - 20}}{2}$$

$$m_1 = \frac{-4 \pm j2}{2}$$

$$m = -2 \pm j$$

$$m_1 = -2 + j \quad m_2 = -2 - j$$

$$y = e^{-2x}(C\cos x + D\sin x)$$

P.I: $y = Ce^{-2x}$

$$\frac{dy}{dx} = -2Ce^{-2x}$$

$$\frac{d^2y}{dx^2} = 4Ce^{-2x}$$

$$9Ce^{-3x} - 12Ce^{-3x} + 5Ce^{-3x} = 2e^{-3x}$$

$$2Ce^{-3x} = 2e^{-3x}$$

$$C = 1$$

$$G.S: y = e^{-2x}(C\cos x + D\sin x) + e^{-3x}$$

$$4Ce^{-2x} - 8Ce^{-2x} + 5Ce^{-2x} = 2e^{-2x}$$

$$Ce^{-2x}$$

$$C = 2$$

G.S: $y = e^{-2x}(C\cos x + D\sin x) + 2e^{-2x}$

When $x = 0, y = 1, \frac{dy}{dx} = -2$

$$1 = e^0(C\cos 0 + D\sin 0) + 2e^0$$

$$1 = C + 2$$

$$C = -1$$

$$\frac{dy}{dx} = -2e^{-2x}(C\cos x + D\sin x) + (-C\sin x + D\cos x)$$

when $\frac{dy}{dx} = -2, C = -1, x = 0$

$$-2 = -2e^0(-\cos 0 + D\sin 0) + (1\sin 0 + D\cos 0)$$

$$-2 = -2(-1)(1) + D$$

$$-2 = 2 + D$$

$$D = -4$$

$$y = e^{-2x}(-\cos x - \sin x)$$

$$7.) 3 \frac{d^2y}{dx^2} - 2 \frac{dy}{dx} - y = 2x - 3$$

$$\frac{d^2y}{dx^2} - \frac{2}{3} \frac{dy}{dx} - \frac{y}{3} = \frac{2x-3}{3}$$

$$m^2 - \frac{2}{3}m - \frac{1}{3} = 0$$

$$3m^2 - 2m - 1 = 0$$

$$3m^2 - 3m + m - 1 = 0$$

$$3m(m-1) + 1(m-1) = 0$$

$$(3m+1)(m-1) = 0$$

$$m_1 = -\frac{1}{3}, m_2 = 1$$

$$\text{C.F. } y = Ae^{-\frac{x}{3}} + Be^x$$

$$\text{P.I. } y = Cx + D$$

$$\frac{dy}{dx} = C$$

$$\frac{d^2y}{dx^2} = 0$$

$$0 - \frac{2}{3}(C) - \frac{1}{3}(Cx+D) = \frac{2x-1}{3}$$

$$-\frac{2}{3}C - \frac{Cx-D}{3} = \frac{2x-1}{3}$$

$$-Cx - \frac{2}{3}C - \frac{D}{3} = \frac{2x-1}{3}$$

Comparing both sides

$$-\frac{C}{3} = \frac{2}{3}$$

$$C = -2$$

$$-\frac{2}{3}C - \frac{D}{3} = -1$$

$$\frac{4}{3} + 1 = \frac{D}{3}$$

$$4+3 = D$$

$$D = 7$$

$$\text{G.S. } y = Ae^{-\frac{x}{3}} + Be^x - 2x + 7$$

$$8.) \frac{d^2y}{dx^2} - 6 \frac{dy}{dx} + 8y = 8e^{4x}$$

$$m^2 - 6m + 8 = 0$$

$$m^2 - 4m - 2m + 8 = 0$$

$$m(m-4) - 2(m-4) = 0$$

$$(m-2)(m-4) = 0$$

$$m_1 = 2, m_2 = 4$$

$$\text{C.F. } y = Ae^{2x} + Be^{4x}$$

$$\text{P.I. } y = Cx e^{4x}$$

$$\frac{dy}{dx} = 4Cx e^{4x}$$

$$\frac{d^2y}{dx^2} = 16Cx e^{4x}$$

$$16Cx e^{4x} - 24Cx e^{4x} + 8Cx e^{4x} = 8e^{4x}$$

$$\text{P.I. } y = Cx e^{4x}$$

$$\frac{dy}{dx} = 4Cx e^{4x}$$

$$-\frac{d^2y}{dx^2} = 4C(4x e^{4x} + e^{4x})$$

$$4C(4x e^{4x} + e^{4x}) - 6(4Cx e^{4x}) + 8Cx e^{4x} = 8e^{4x}$$

$$16Cx e^{4x} + 4C e^{4x} - 24Cx e^{4x} + 8Cx e^{4x} = 8e^{4x}$$

$$4C e^{4x} = 8e^{4x}$$

$$4C = 8$$

$$C = 2$$

$$\text{G.S. } y = Ae^{2x} + Be^{4x} + 2x e^{4x}$$