

NAME: NNAJI PROMISE EBUKA

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$$x = \cos t + t \sin t$$

$$y = \sin t - t \cos t$$

an expression for the radius of curvature (R) in terms of t

Ans

$$x = \cos t + t \sin t$$

$$\frac{dx}{dt} = -\sin t + t \cos t + \sin t = t \cos t$$

$$y = \sin t - t \cos t$$

$$\frac{dy}{dt} = \cos t + t \sin t - \cos t = t \sin t$$

$$\frac{dy}{dx} = \frac{dy}{dt} \times \frac{dt}{dx}$$

$$= \frac{t \sin t}{t \cos t}$$

$$\frac{dy}{dx} = \frac{\sin t}{\cos t}$$

$\frac{d^2y}{dx^2}$

$$U = \sin t, \quad V = \cos t$$

$$\frac{dU}{dt} = \cos t$$

$$\frac{dV}{dt} = -\sin t$$

$$\frac{V \frac{dU}{dx} - U \frac{dV}{dx}}{V^2}$$

$$\frac{\cos t (\cos t) - (\sin t) (-\sin t)}{(\cos t)^2} \times \frac{1}{t \cos t}$$

$$\frac{\cos^2 t + \sin^2 t}{\cos^2 t} \times \frac{1}{t \cos t}$$

$$\frac{1}{\cos^2 t} \times \frac{1}{t \cos t} = \frac{1}{t \cos^3 t}$$

$$\frac{d^2 y}{dx^2} = \frac{1}{t \cos t}$$

$$R = \frac{\left(1 + \left(\frac{dy}{dx}\right)^2\right)^{3/2}}{d^2 y / dx^2}$$

$$R = \frac{\left(1 + \left(\frac{\sin t}{\cos t}\right)^2\right)^{3/2}}{d^2 y / dx^2}$$

$$R = \frac{\left(\frac{1 + \sin^2 t}{\cos^2 t}\right)^{3/2}}{\frac{1}{t \cos^3 t}}$$

$$R = \frac{\left(\frac{\cos^2 t + \sin^2 t}{\cos^2 t}\right)^{3/2}}{t \cos^3 t}$$

$$R = \frac{\left(1 / \cos^2 t\right)^{3/2}}{1/t \cos^3 t}$$

$$R = \frac{1}{\cos^2 t} \times t \cos^3 t$$

$$R = t$$

Expressions for the coordinate (h, k) or
the centre of curvature in terms of t

Ans

$$h = x_1 - R \sin t$$

$$k = y_1 + R \cos t$$

$$R = t, \quad \theta = \tan^{-1} \left(\frac{dy}{dx} \right)$$

$$\frac{dy}{dx} = \frac{\sin t}{\cos t} = \tan t$$

$$\therefore \theta = \frac{1}{\tan} \tan t$$

$$\theta = t$$

$$h = x_1 - t \sin t$$

$$k = y_1 + t \cos t$$

$$\text{but } x = \cos t + t \sin t$$

$$y = \sin t - t \cos t$$

$$h = \cos t + t \sin t - t \sin t$$

$$h = \underline{\underline{\cos t}}$$

$$k = \sin t - t \cos t + t \cos t$$

$$k = \sin t$$

$$(h, k) = (\cos t, \sin t)$$