

ASSIGNMENT

OYEBAOJI OLALEKAN JOSHUA
15 (ENG041049)
Electrical & Electronics
ENG 381

$$1) \frac{d^2y}{dx^2} - \frac{dy}{dx} - 2y = 8$$

$$m^2 - m - 2 = 0$$

$$a = 1, b = -1, c = -2$$

$$(m-2)(m+1) = 0$$

$$m_1 = 2 \text{ or } m_2 = -1$$

$$C.F. = y = Ae^{2x} + Be^{-x}$$

$$P.I. = y = c$$

$$\frac{dy}{dx} = 0$$

$$\frac{d^2y}{dx^2} = 0$$

$$0 - 0 - 2c = 8$$

$$-2c = 8$$

$$c = -4 \text{ and } y = -4$$

$$\text{Ans } y = P.I. + C.F.$$

$$y = Ae^{2x} + Be^{-x} - 4$$

$$2) \frac{d^2y}{dx^2} - 4y = 10e^{3x}$$

$$m^2 - 4 = 0$$

$$m = \sqrt{4}$$

$$m = \pm 2$$

$$y = Ce^{3x}$$

$$C.F. = y = A \cosh 2x + B \sinh 2x$$

$$\frac{d^2y}{dx^2} = 3Ce^{3x}$$

$$\frac{d^2y}{dx^2} = 9Ce^{3x}$$

$$9ce^{3x} - 4(ce^{3x}) = 10e^{2x}$$

$$9c - 4c = 10$$

$$5c = 10$$

$$c = 2$$

$$y = 2e^{3x}$$

$$\text{or } y = PI + Cf$$

$$y = A\cos 2x + B\sin 2x + 2e^{3x}$$

$$3) \frac{d^2y}{dx^2} + 2\frac{dy}{dx} + y = e^{-2x}$$

$$m^2 + 2m + 1 = 0$$

$$a=1, b=2, c=1$$

$$m_1 = -1, m_2 = -1$$

$$Cf = y = e^{-x}(A+Bx)$$

$$P-I = y = ce^{-2x}$$

$$\frac{dy}{dx} = -2ce^{-2x}$$

$$\frac{d^2y}{dx^2} = 4ce^{-2x}$$

$$4ce^{-2x} + 2(-2ce^{-2x}) + ce^{-2x} = e^{-2x}$$

$$4ce^{-2x} - 4ce^{-2x} + ce^{-2x} = e^{-2x}$$

$$4c - 4c + c = 0$$

$$c = 1$$

$$P-I = y = e^{-2x}$$

$$\text{or } y = Cf + PI$$

$$y = e^{-x}(A+Bx) + e^{-2x}$$

$$4) \frac{d^2y}{dx^2} + 25y = 5x^2 + x$$

$$m^2 + 25 = 0$$

$$m = \sqrt{-25}$$

$$m = \pm 5j$$

$$Cf = y = A\cos 5x + B\sin 5x$$

$$P.I = y = cx^2 + Dx + E$$

$$\frac{dy}{dx} = 2cx + D$$

$$\frac{d^2y}{dx^2} = 2c$$

$$2c + 25(cx^2 + Dx + E) = 5x^2 + x$$

$$2c + 25cx^2 + 25Dx + 25E = 5x^2 + x$$

$$25cx^2 + 25Dx + 2c + 25E = 5x^2 + x$$

$$25c = 5 \dots (1)$$

$$25D = 1 \dots (2)$$

$$2c + 25E = 0 \dots (3)$$

$$c = \frac{5}{25} = \frac{1}{5}$$

$$D = \frac{1}{25}$$

$$25E = -2c$$

$$E = \frac{-2c}{25}$$

$$E = \frac{-2}{25} \times \frac{1}{5}$$

$$E = \frac{-2}{125}$$

$$P.I = y = \frac{x^2}{5} + \frac{x}{25} - \frac{2}{125}$$

$$G.S = P.I + C.F$$

$$y = A \cos 5x + B \sin 5x + \frac{x^2}{5} + \frac{x}{25} - \frac{2}{125}$$

$$5) \frac{d^2y}{dx^2} - 2 \frac{dy}{dx} + y = 4 \sin x$$

$$m^2 - 2m + 1 = 0$$

$$(m-1)(m-1) = 0$$

$$m_1 = 1 \quad m_2 = 1$$

$$C.F = y = e^x(A + Bx)$$

$$P.I = y = C \cos x + D \sin x$$

$$\frac{dy}{dx} = -C \sin x + D \cos x$$

$$\frac{d^2 y}{dx^2} = -C \cos x - D \sin x$$

$$-(\cos x - D \sin x - 2(-C \sin x + D \cos x) + (\cos x + D \sin x)) = 4 \sin x$$

$$-C \cos x - D \sin x + 2C \sin x - 2D \cos x + C \cos x + D \sin x = 4 \sin x$$

$$-C \cos x + C \cos x - D \sin x + D \sin x + 2C \sin x - 2D \cos x = 4 \sin x$$

$$2C \sin x - 2D \cos x = 4 \sin x$$

$$C \sin x - D \cos x = 2 \sin x$$

$$C = 2$$

$$-D = 0$$

$$P.I = y = 2 \cos x$$

$$G.S = y = c.f + P.I$$

$$y = e^x (A + Bx) + 2 \cos x$$

$$6) \frac{d^2 y}{dx^2} + 4 \frac{dy}{dx} + 5y = 2e^{-2x}$$

$$m^2 + 4m + 5 = 0$$

$$m = -2 \pm j$$

$$C.F = y = e^{-2x} (A \cos x + B \sin x)$$

$$P.I = Ce^{-2x}$$

$$\frac{dy}{dx} = -2Ce^{-2x}$$

$$\frac{d^2 y}{dx^2} = 4Ce^{-2x}$$

$$4Ce^{-2x} + 4(-2Ce^{-2x}) + 5(Ce^{-2x}) = 2e^{-2x}$$

$$4Ce^{-2x} - 8Ce^{-2x} + 5Ce^{-2x} = 2e^{-2x}$$

$$Ce^{-2x} = 2e^{-2x}$$

$$C = 2$$

$$P.I = y = 2e^{-2x}$$

$$G.S = y = e^{-2x} (A \cos x + B \sin x) + 2e^{-2x}$$

$$\text{given that } x=0, y=1 \text{ and } \frac{dy}{dx} = -2$$

$$1 = e^{-2(0)} (A \cos(0) + B \sin(0)) + 2e^{-2(0)}$$

$$A + 2 = 1$$

$$A = -1$$

$$\frac{dy}{dx} = e^{-2x} (-A \sin x + B \cos x) + (A \cos x + B \sin x) - 2e^{-2x} - 4e^{-2x}$$

$$-2 = e^{-2(0)} (B) + (A) - 2 - 4$$

$$-2 = B - 2A - 4$$

$$-2 = B + 1 - 4$$

$$B = 1$$

$$y = e^{-2x} (-\cos x + \sin x) + 2e^{-2x}$$

$$7) 3 \frac{d^2y}{dx^2} - 2 \frac{dy}{dx} - y = 2x - 3$$

$$3m^2 - 2m - 1 = 0$$

$$m_1 = \frac{1}{3} \quad m_2 = -1$$

$$Cf = y = A e^{x/3} + B e^{-x}$$

$$P.I = Cx + D$$

$$\frac{dy}{dx} = C$$

$$\frac{d^2y}{dx^2} = 0$$

$$3(0) - 2C - (Cx + D) = 2x - 3$$

$$-2C - Cx + D = 2x - 3$$

$$-Cx - 2C + D = 2x - 3$$

$$-Cx = 2x$$

$$-C = 2$$

$$C = -2$$

$$-2C + D = -3$$

$$D = -3 + 2C$$

$$\text{at } C = -2$$

$$D = -3 + 2(-2)$$

$$D = -3 - 4$$

$$D = -7$$

$$P.I = y = -2x - 7$$

$$G_s = PI + Cf$$

$$= Ae^{x/3} + Be^{-x} - 2x - 7$$

$$7) \frac{d^2y}{dx^2} - 6\frac{dy}{dx} + 8y = 8e^{4x}$$

$$m^2 - 6m + 8 = 0$$

$$(m-4)(m-2) = 0$$

$$m_1 = 4 \text{ \& } m_2 = 2$$

$$Cf \ y = Ae^{4x} + Be^{2x}$$

$$y = cxe^{4x}$$

$$\frac{dy}{dx} = c(x \cdot 4e^{4x} + e^{4x} \cdot 1)$$

$$\frac{dy}{dx} = c(4xe^{4x} + e^{4x})$$

$$\frac{dy}{dx} = 4cxe^{4x} + ce^{4x}$$

$$\frac{d^2y}{dx^2} = 4c(x \cdot 4e^{4x} + e^{4x} \cdot 1) + 4ce^{4x}$$

$$\frac{d^2y}{dx^2} = 4c(4xe^{4x} + e^{4x}) + 4ce^{4x}$$

$$= 16cxe^{4x} + 4ce^{4x} + 4ce^{4x}$$

$$16cxe^{4x} + 8ce^{4x} - 6(4cxe^{4x} + ce^{4x}) + 8(cxe^{4x}) = 8e^{4x}$$

$$16cxe^{4x} + 8ce^{4x} - 24cxe^{4x} - 6ce^{4x} + 8cxe^{4x} = 8e^{4x}$$

$$16cx + 8c - 24cx - 6c + 8cx = 8$$

$$2c = 8$$

$$c = 4$$

$$PI = y = 4xe^{4x}$$

$$G_s = PI + Cf$$

$$= Ae^{4x} + Be^{2x} + 4xe^{4x}$$