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15/Eng02/035
Assignment 381 (Maths)

$$y = \frac{w}{24EI}\left[6L^2x^2 - 4x^3 + x^4\right]$$

when $x = L$

$$y = \frac{w}{24EI}\left[6L^4 - 4L^4 + L^4\right]$$

$$y = \frac{w}{24EI}\left[3L^4\right]$$

$$y = \frac{wL^4}{8EI}$$

$y = -\frac{3}{4}\cos\theta + \frac{3}{4}\sin\theta$ // P.I

$y = e^{-2\theta}(A\cos\theta + B\sin\theta) - \frac{3}{4}\cos\theta + \frac{3}{4}\sin\theta$

$y = e^{-2\theta}(A\cos\theta + B\sin\theta) + \frac{3}{4}(\sin\theta - \cos\theta)$ // G.S

at steady state,

$\frac{dy}{d\theta} = 0$ and $\theta = \alpha$

$y = e^{-2\theta}(A\cos\theta + B\sin\theta) + \frac{3}{4}(\sin\theta - \cos\theta)$

$\frac{dy}{d\theta} = e^{-2\theta}(B\cos\theta - A\sin\theta) - 2e^{-2\theta}(A\cos\theta + B\sin\theta)$

$+ \frac{3}{4}(\sin\theta - \cos\theta)$

$\frac{dy}{d\theta} = e^{-2\alpha}(B\cos\alpha - A\sin\alpha) - 2e^{-2\alpha}(A\cos\alpha + B\sin\alpha)$

$+ \frac{3}{4}(\sin\alpha - \cos\alpha)$

$\frac{dy}{d\theta} = \frac{3}{4}(\sin\alpha - \cos\alpha)$

$\frac{dy}{d\theta} = \frac{3}{4}(\sin\theta - \cos\theta)$

ETM 581 ASSIGNMENT 2

1- $\frac{d^2y}{d\theta^2} + 4\frac{dy}{d\theta} + 5y = 6\sin\theta$

// convert equation into a homogeneous equation

$\frac{d^2y}{d\theta^2} + 4\frac{dy}{d\theta} + 5y = 0$

$m^2 + 4\frac{dy}{d\theta} + 5y = 0$

$m^2 + 4m + 5 = 0$

$a=1 \quad b=4 \quad c=5$

$m = \frac{-4 \pm \sqrt{4^2 - 4\times1\times5}}{2\times1} \Rightarrow m = \frac{-4 \pm \sqrt{-4}}{2} \Rightarrow m = \frac{-4 \pm 2i}{2}$

$m = -2 \pm i$

$\therefore y = e^{-2\theta}(A\cos\theta + B\sin\theta)$ // CF

$y = C\cos\theta + D\sin\theta$

$\frac{dy}{d\theta} = -C\sin\theta + D\cos\theta$

$-C\cos\theta - D\sin\theta + 4[-C\sin\theta + D\cos\theta] + 5[C\cos\theta + D\sin\theta] = 6\sin\theta$

$-C\cos\theta - D\sin\theta - 4C\sin\theta + 4D\cos\theta + 5C\cos\theta + 5D\sin\theta = 6\sin\theta$

$-C + 4D + 5C = 0$

$-D + 4C + 5D = 6$

$4C + 4D = 0 \quad \text{—①}$

$-4C + 4D = 6 \quad \text{—②}$

$8D = 6$

$D = 6/8 = 3/4$

// substitute $D = 3/4$ into eqn ①

$4 \times \frac{3}{4} - 4C = 6$

$4C = 3 - 6 = -3$

$C = -3/4$

2) $EI\frac{d^2y}{dx^2} = \frac{w}{2}(L-x)^2$

// convert equation into a homogeneous equation

$EI\frac{d^2y}{dx^2} = 0$

$EI\frac{d^2y}{dx^2} = 0$

$EIm^2 = 0$

$m^2 = 0 \Rightarrow m = \pm\sqrt{0} = 0$

$m_1 = m_2 = 0$

$y = e^{ax}(A + Bx)$

$y = A + Bx$ // CF

$y = Rx^2 + Sx^3 + Tx^4$

$\frac{dy}{dx} = 2Rx + 3Sx^2 + 4Tx^3$

$$\frac{d^2y}{dx^2} = 2R + 6Sx + 12Tx^2$$

$$EI[2R + 6Sx + 12Tx^2] = \frac{W}{2}(L-x)^2$$

$$2REI + 6SxEI + 12Tx^2EI = \frac{W}{2}[L^2 - 2Lx + x^2]$$

// multiply equation by 2

$$4REI + 12SxEI + 24Tx^2EI = WL^2 - 2WLx + Wx^2$$

$$24TEI = W$$

$$T = \frac{W}{24EI}$$

$$12SEI = -2WL$$

$$S = \frac{-2WL}{24EI}$$

$$y = \left[\frac{WL^2}{4EI}\right]x^2 - \left[\frac{WL}{6EI}\right]x^3 + \left[\frac{W}{24EI}\right]x^4$$

$$y = \frac{WL^2x^2}{4EI} - \frac{WLx^3}{6EI} + \frac{Wx^4}{24EI}$$

$$y = \frac{6WL^2x^2 - 4WLx^3 + Wx^4}{24EI}$$

$$y = \frac{W}{24EI}\left[6L^2x^2 - 4Lx^3 + x^4\right] \quad // \text{ RI}$$

$$y = A + Bx + \frac{W}{24EI}\left[6L^2x^2 - 4Lx^3 + x^4\right]$$

at $x = 0$ $y = 0$ $dy/dx = 0$

$$0 = A + B(0) + \frac{W}{24EI}\left[12L^2x - 12Lx^2 + 4x^3\right]$$

$$0 = B + \frac{W}{24EI}\left[12L^2(0) - 12L(0)^2 + 4(0)^3\right]$$

$$B = 0$$

when $A = B = 0$

$$y = 0 + 0x + \frac{W}{24EI}\left[6L^2x^2 - 4Lx^3 + x^4\right]$$

$$y = \frac{w}{24EI}\left[6L^2x^2 - 4x^3 + x^4\right]$$

when $x = L$

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$$y = \frac{wL^4}{8EI}$$