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Computer Engineering
15/CE602/002
CE6301 Assignment

1) $\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 5y = 6\sin\theta$
convert into homogeneous equation
 $\frac{d^2y}{dt^2} + 4\frac{dy}{dt} + 5y = 0$

$$m^2 + 4m + 5 = 0$$

$$a=1, b=4, c=5$$

$$m = \frac{-4 \pm \sqrt{4^2 - 4 \times 1 \times 5}}{2 \times 1} \Rightarrow m = \frac{-4 \pm j}{2}$$

$$m = \frac{-4 \pm 2j}{2}$$

$$m = -2 \pm j$$

CF: $y = e^{-2\theta} (A \cos\theta + B \sin\theta)$

$$y = C \cos\theta + D \sin\theta$$

$$\frac{dy}{d\theta} = -C \sin\theta + D \cos\theta$$

$$- (C \cos\theta - D \sin\theta + 4[C \sin\theta + D \cos\theta] + 5[C \cos\theta + D \sin\theta]) = 6 \sin\theta$$

$$- C \cos\theta - D \sin\theta - 4C \sin\theta + 4D \cos\theta + 5C \cos\theta + 5D \sin\theta = 6 \sin\theta$$
$$-C + 4D + 5C = 0$$
$$-D + 4C + 5D = 6$$

$$4C + 4D = 0 \quad \text{--- (1)}$$

$$+ 4C + 4D = 6 \quad \text{--- (2)}$$

$$2D = 6$$

$$D = \frac{6}{2} = 3/1$$

Substitute $D = 3/1$ in eqn (1)

$$-4C + 4(3/1) = 6$$

$$-4C + 3 = 6$$

$$-4C = 3$$

$$C = -3/4$$

$$y = -\frac{3}{4} \cos \theta + \frac{3}{4} \sin \theta$$

$$y = e^{-2\theta} (A \cos \theta + B \sin \theta) - \frac{3}{4} \cos \theta + \frac{3}{4} \sin \theta$$

$$y = e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

at steady state

$$\frac{dy}{d\theta} = 0 \quad \text{and} \quad \theta = \alpha$$

$$y = e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

$$\frac{dy}{d\theta} = e^{-2\theta} (B \cos \theta - A \sin \theta) - 2e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

$$\frac{dy}{d\theta} = e^{-2\alpha} (B \cos \alpha - A \sin \alpha) - 2e^{-2\alpha} (A \cos \alpha + B \sin \alpha) + \frac{3}{4} (\sin \alpha - \cos \alpha)$$

$$\frac{dy}{d\theta} = \frac{3}{4} (\sin \alpha - \cos \alpha)$$

$$\frac{dy}{d\theta} = \frac{3}{4} (\sin \theta - \cos \theta)$$

$$2) \quad EI \frac{d^2 y}{dx^2} = \frac{w}{2} (L-x)^2$$

$$EI \frac{d^2 y}{dx^2} = 0$$

$$EI \frac{d^2 y}{dx^2} = 0$$

$$EI m^2 = 0$$

$$m^2 = 0 \Rightarrow m = \pm \sqrt{0} = 0$$

$$m_1 = m_2 = 0$$

$$y = e^{0x} (A + Bx)$$

$$CF: \quad y = A + Bx$$

$$y = Rx^2 + Sx^3 + Tx^4$$

$$\frac{dy}{dx} = 2Rx + 3Sx^2 + 4Tx^3$$

$$\frac{d^2 y}{dx^2} = 2R + 6Sx + 12Tx^2$$

$$EI [2R + 6Sx + 12Tx^2] = \frac{w}{2} (L-x)^2$$

$$2REI + 6SxEI + 12Tx^2EI = \frac{w}{2} [L^2 - 2Lx + x^2]$$

$$4REI + 12SxEI + 24Tx^2EI = wL^2 - 2wLx + wx^2$$

$$24TEI = w$$

$$T = \frac{w}{24EI}$$

$$12JEL = -2WL$$

$$S = \frac{-2WL}{24EI}$$

$$y = \left[\frac{wL^2}{-4EI} \right] x^2 - \left[\frac{wL}{6EI} \right] x^3 + \left[\frac{w}{24EI} \right] x^4$$

$$y = \frac{wL^2 x^2}{4EI} - \frac{wL x^3}{6EI} + \frac{w x^4}{24EI}$$

$$y = \frac{6wL^2 x^2 - 4wL x^3 + w x^4}{24EI}$$

$$y = \frac{6wL^2 x^2 - 4wL x^3 + w x^4}{24EI}$$

$$\text{PI: } y = \frac{w}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$y = A + Bx + \frac{w}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$\text{at } x=0, y=0; \frac{dy}{dx} = 0$$

$$0 = A + B(0) + \frac{w}{24EI} [12L^2 x - 12L x^2 + 4x^3]$$

$$0 = B + \frac{w}{24EI} [12L^2(0) - 12L(0)^2 + 4(0)^3]$$

$$B = 0$$

when $A = B = 0$

$$y = 0 + 0x + \frac{w}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$y = \frac{w}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

when $x = L$

$$y = \frac{w}{24EI} [6L^4 - 4L^4 + L^4]$$

$$y = \frac{w}{24EI} [3L^4]$$

$$y = \frac{wL^4}{8EI}$$

