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 IS/ENG011/009  
 CHEMICAL ENGINEERING  
 ENA 381

$$1 \quad \frac{d^2 y}{d\theta^2} + 4 \frac{dy}{d\theta} + 5y = 6 \sin \theta$$

$$\text{let } 6 \sin \theta = 0$$

$$m^2 + 4m + 5 = 0$$

$$a = 1, \quad b = 4, \quad c = 5$$

$$m = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-4 \pm \sqrt{4^2 - 4(1)(5)}}{2(1)} = \frac{-4 \pm \sqrt{-4}}{2} = \frac{-4 \pm j2}{2}$$

$$m = -2 + j$$

$$m = \alpha + j\beta$$

$$C.F = y = e^{-2x} (A \cos \theta + B \sin \theta)$$

$$f(\theta) = 6 \sin \theta, \quad P.I = y = C \cos \theta + D \sin \theta$$

$$\frac{dy}{d\theta} = -C \sin \theta + D \cos \theta$$

$$\frac{d^2 y}{d\theta^2} = -C \cos \theta - D \sin \theta$$

$$\frac{d^2 y}{d\theta^2} + 4 \frac{dy}{d\theta} + 5y = 6 \sin \theta$$

$$-C \cos \theta - D \sin \theta + 4(-C \sin \theta + D \cos \theta) + 5C \cos \theta + 5D \sin \theta = 6 \sin \theta$$

$$-C \cos \theta - D \sin \theta - 4C \sin \theta + 4D \cos \theta + 5C \cos \theta + 5D \sin \theta = 6 \sin \theta$$

$$4C \cos \theta + 4D \sin \theta - 4C \sin \theta + 4D \cos \theta = 6 \sin \theta$$

$$4C \cos \theta + 4D \cos \theta + 4D \sin \theta - 4C \sin \theta = 6 \sin \theta$$

$$(4C + 4D) \cos \theta + (4D - 4C) \sin \theta = 6 \sin \theta$$

$$4C + 4D = 0 \quad \dots \text{ (ii)}$$

$$-4C + 4D = 6 \quad \dots \textcircled{11}$$

$$6D = 6$$

$$D = 3/4$$

From eqn (1)

$$4C + 4(3/4) = 0$$

$$4C + 3 = 0 \quad ; \quad C = -3/4$$

$$P.I = y = -3/4 \cos \theta + 3/4 \sin \theta$$

$$G.S = C.F + P.I$$

$$y = e^{-2x} (A \cos \theta + B \sin \theta) - 3/4 \cos \theta + 3/4 \sin \theta$$

Steady state eqn

$$y' = 3/4 \sin \theta + 3/4 \cos \theta = 0$$

$$\frac{3/4 \sin \theta}{3/4 \cos \theta} = \frac{-3/4 \cos \theta}{3/4 \cos \theta}$$

$$\tan \theta = -1 \quad ; \quad \theta = \tan^{-1}(-1) \quad ; \quad \theta = -45^\circ$$

$$2) \quad EI \frac{d^2 y}{dx^2} = w/2 (1-x)^2$$

$$EI m^2 = 0$$

$$m^2 = 0$$

$$m = \pm \sqrt{0} \quad ; \quad m = \pm 0$$

$$y_i = e^{0x} (A + Bx)$$

$$C.F = y = A + Bx$$

$$P.I = y = Fx^2 + Gx^3 + Hx^4$$

$$\frac{dy}{dx} = 2Fx + 3Gx^2 + 4Hx^3$$

$$\frac{d^2 y}{dx^2} = 2F + 6Gx + 12Hx^2$$

$$EI(2f + 6Gx + 12Hx^2) = \frac{w}{2}(1-x)^2$$

$$2fEI + 6GxEI + 12HEIx^2 = \frac{w}{2}(1-x)^2$$

$$4fEI + 12GxEI + 24HEIx^2 = w(l^2 - 2lx + x^2)$$

$$24HEI = w$$

$$H = \frac{w}{24EI}$$

Comparing both equations

$$12GxEI = -2wx$$

$$G = \frac{-2wx}{12EI} = \frac{-w}{6EI}$$

$$4fEI = wl^2 \quad f = \frac{wl^2}{4EI}$$

$$y = \left[ \frac{wl^2}{4EI} \right] x^2 - \left[ \frac{wx}{6EI} \right] x^3 + \left[ \frac{w}{24EI} \right] x^4$$

$$= \frac{wl^2 x^2}{4EI} - \frac{wx^4}{6EI} + \frac{wx^4}{24EI}$$

$$y = \frac{6wl^2 x^2 - 4wx^4 + wx^4}{24EI}$$

$$G.S = y = A + Bx + \frac{w}{24EI} [6l^2 x^2 - 4x^4 + x^4]$$

$$\text{at } y=0; \quad x=0 = \frac{dy}{dx} = 0$$

$$0 = A + B(0) + \frac{w}{24EI} [6l^2(0)^2 - 4(0)^4 + 0^4]$$

$$A=0$$

$$\frac{dy}{dx} = B + \frac{w}{24EI} [12x^2 - 12x^4 + 4x^3]$$

$$0 = B + \frac{w}{24EI} [12(0)^2 - 12(0)^4 + 4(0)^3]$$

$$B=0$$

$$y = fx^2 + Gx^3 + Hx^4$$

$$= \frac{wl^2 x^2}{4EI} - \frac{wx^4}{6EI} + \frac{wx^4}{24EI}$$

$$y = \frac{w}{24EI} [6lx^2 - 4lx^3 + x^4]$$

$$y = \frac{wx^2}{24EI} [6l^2 - 4lx + x^2]$$

when  $x=l$

$$y = \frac{wl^2}{24EI} [6l^2 - 4l^2 + l^2]$$

$$y = \frac{wl^2}{24EI} [3l^2]$$

$$y = \frac{3wl^4}{24EI}$$

$$y = \frac{wl^4}{8EI}$$