

UNDIE FIDELIS BEWAPUNTE

15/ENG03/033

CIVIL ENGINEERING

ENG 381

$$1) \frac{d^2y}{d\theta^2} + 4 \frac{dy}{d\theta} + 5y = 6\sin\theta$$

Convert into a homogenous equation

$$\frac{d^2y}{d\theta^2} + 4 \frac{dy}{d\theta} + 5y = 0$$

$$m^2 + 4m + 5 = 0$$

$$a=1, b=4, c=5$$

$$m = \frac{-4 \pm \sqrt{4^2 - 4 \times 1 \times 5}}{2 \times 1} = m = \frac{-4 \pm \sqrt{-4}}{2}$$

$$m = \frac{-4 \pm 2j}{2}$$

$$m = -2 \pm j$$

$$C.F = y = e^{-2\theta} (A \cos\theta + B \sin\theta)$$

$$y = C \cos\theta + D \sin\theta$$

$$\frac{dy}{d\theta} = -C \sin\theta + D \cos\theta$$

$$-C \cos\theta - D \sin\theta + 4(-C \sin\theta + D \cos\theta) + 5(C \cos\theta + D \sin\theta) = 6 \sin\theta$$

$$-C \cos\theta - D \sin\theta - 4C \sin\theta + 4D \cos\theta + 5C \cos\theta + 5D \sin\theta = 6 \sin\theta$$

$$-C + 4D + 5C = 0$$

$$-D + 4C + 5D = 6$$

$$+4C + 4D = 0 \quad \text{--- (1)}$$

$$4C + 4D = 6 \quad \text{--- (2)}$$

$$8D = 6$$

$$D = \frac{6}{8} = \frac{3}{4}$$

Substitute $D = \frac{3}{4}$ into eqn 2

$$-4C + 4\left(\frac{3}{4}\right) = 6$$

$$-4C + 3 = 6$$

$$-4C = 3$$

$$C = -\frac{3}{4}$$

$$y = -\frac{3}{4} \cos\theta + \frac{3}{4} \sin\theta$$

$$y = e^{-2\theta} (A \cos\theta + B \sin\theta) = \frac{3}{4} \sin\theta$$

$$y = e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

at steady state

$$\frac{dy}{dx} = 0 \text{ and } \theta = \alpha$$

$$y = e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

$$\frac{dy}{dx} = (B \cos \theta - A \sin \theta) - 2e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

$$\frac{dy}{dt} = e^{-2\theta} (B \cos \theta - A \sin \theta) - 2e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

$$\frac{dy}{dt} = \frac{3}{4} (\sin \theta - \cos \theta)$$

$$\frac{dy}{dt} = \frac{3}{4} (\sin \theta - \cos \theta)$$

$$2) EI \frac{d^2y}{dx^2} = \frac{w}{2} (L-x)^2$$

$$EI \frac{d^2y}{dx^2} = 0$$

$$EI m^2 = 0$$

$$m^2 = 0 = m = \pm \sqrt{0} = 0$$

$$m_1 = m_2 = 0$$

$$y = e^{ax} (A + Bx)$$

$$CF \div y = A + Bx$$

$$y = Rx^2 + Sx^3 + Tx^4$$

$$\frac{dy}{dx} = 2Rx + 3Sx^2 + 4Tx^3$$

$$\frac{d^2y}{dx^2} = 2R + 6Sx + 12Tx^2$$

$$EI (2R + 6Sx + 12Tx^2) = \frac{w}{2} (L-x)^2$$

$$2REI + 6SxEI + 12Tx^2EI = \frac{w}{2} (L^2 - 2Lx + x^2)$$

$$4REI + 12SxEI + 24Tx^2EI = wL^2 - 2wLx + wx^2$$

$$24TEI = w$$

$$T = \frac{w}{24EI}$$

$$12SEI = -2wL$$

$$S = \frac{-2wL}{24EI}$$

$$y = \left[\frac{WL^2}{4EI} \right] x^2 - \left[\frac{WL}{6EI} \right] x^3 + \left[\frac{w}{24EI} \right] x^4$$

$$y = \frac{WL^2 x^2}{4EI} - \frac{WL x^3}{6EI} + \frac{w x^4}{24EI}$$

$$y = \frac{6WL^2 x^2 - 4WL x^3 + w x^4}{24EI}$$

$$y = \frac{6WL^2 x^2 - 4WL x^3 + w x^4}{24EI}$$

$$P \cdot I \div y = \frac{w}{24EI} \left[6L^2 x^2 - 4L x^3 + x^4 \right]$$

$$y = A + Bx + \frac{w}{24EI} \left[6L^2 x^2 - 4L x^3 + x^4 \right]$$

$$\text{at } x=0, y=0, \frac{dy}{dx} = 0$$

$$0 = A + B(0) + \frac{w}{24EI} \left[12L^2(0) - 12L(0)^2 + 4(0)^3 \right]$$

$$B = 0$$

When $A = B = 0$

$$y = 0 + 0x + \frac{w}{24EI} (6L^2 x^2 - 4L x^3 + x^4)$$

$$y = \frac{w}{24EI} (6L^2 x^2 - 4L x^3 + x^4)$$

When $x = L$

$$y = \frac{w}{24EI} (6L^4 - 4L^4 + L^4)$$

$$y = \frac{w}{24EI} (3L^4)$$

$$y = \frac{wL^4}{8EI}$$