

EZIMUDOR GREAT

MECHATRONICS ENGR

15/SC103/006

ENR 381

ASSIGNMENT

$$1) \frac{d^2y}{d\theta^2} + 4\frac{dy}{d\theta} + 5y = 6\sin\theta$$

Convert into a homogeneous equation

$$\frac{d^2y}{d\theta^2} + 4\frac{dy}{d\theta} + 5y = 0$$

$$m^2 + 4m + 5 = 0$$

$$a=1, b=4, c=5$$

$$m = \frac{-4 \pm \sqrt{4^2 - 4 \times 1 \times 5}}{2 \times 1} \Rightarrow m = \frac{-4 \pm \sqrt{4}}{2}$$

$$m = \frac{-4 \pm 2j}{2}$$

$$m = -2 \pm j$$

$$CF = y = e^{-2\theta} (A\cos\theta + B\sin\theta)$$

$$y = C\cos\theta + D\sin\theta$$

$$\frac{dy}{d\theta} = -C\sin\theta + D\cos\theta$$

$$-C\cos\theta - D\sin\theta + 4[-C\sin\theta + D\cos\theta] + 5[C\cos\theta + D\sin\theta] = 6\sin\theta$$

$$-C\cos\theta - D\sin\theta - 4C\sin\theta + 4D\cos\theta + 5C\cos\theta + 5D\sin\theta = 6\sin\theta$$

$$-C + 4D + 5C = 0$$

$$-D + 4C + 5D = 6$$

$$+ 4C + 4D = 0 \quad \text{--- (1)}$$

$$-4C + 4D = 6 \quad \text{--- (2)}$$

$$8D = 6$$

$$D = 6/8 = 3/4$$

Substitute $D = 3/4$ in eqn (2)

$$-4C + 4(3/4) = 6$$

$$-4C + 3 = 6$$

$$-4C = 3$$

$$C = -3/4$$

$$y = -\frac{3}{4} \cos \theta + \frac{3}{4} \sin \theta$$

$$y = e^{-2\theta} (A \cos \theta + B \sin \theta) - \frac{3}{4} \cos \theta + \frac{3}{4} \sin \theta$$

$$y = e^{-2\theta} (A \cos \theta + B \sin \theta) + \frac{3}{4} (\sin \theta - \cos \theta)$$

at steady state

$$\frac{dy}{dx} \Rightarrow \text{ and } \theta = x$$

$$y = e^{-2x} (A \cos x + B \sin x) + \frac{3}{4} (\sin x - \cos x)$$

$$\frac{dy}{dx} = e^{-2x} (B \cos x - A \sin x) - 2e^{-2x} (A \cos x + B \sin x) + \frac{3}{4} (\cos x + \sin x)$$

~~dy~~

$$\frac{dy}{dx} = e^{-2x} (B \cos x - A \sin x) - 2e^{-2x} (A \cos x + B \sin x) + \frac{3}{4} (\cos x + \sin x)$$

~~dx~~

$$\frac{dy}{dx} = \frac{3}{4} (\sin x - \cos x)$$

~~dx~~

$$\frac{dy}{dx} = \frac{3}{4} (\sin x - \cos x)$$

$$2) \quad EI \frac{d^2 y}{dx^2} = \frac{w}{2} (L-x)^2$$

$$EI \frac{d^2 y}{dx^2} = 0$$

$$-EI m^2 = 0$$

$$m^2 = 0 \Rightarrow m = \pm \sqrt{0} = 0$$

$$m_1 = m_2 = 0$$

$$y = e^{0x} (A + Bx)$$

$$CF: \quad y = A + Bx$$

$$y = Rx^2 + Sx^3 + Tx^4$$

$$\frac{dy}{dx} = 2Rx + 3Sx^2 + 4Tx^3$$

$$\frac{d^2 y}{dx^2} = 2R + 6Sx + 12Tx^2$$

$$EI [2R + 6Sx + 12Tx^2] = \frac{w}{2} (L-x)^2$$

$$2REI + 6SxEI + 12Tx^2EI = \frac{w}{2} [L^2 - 2Lx + x^2]$$

$$4REI + 12SxEI + 24Tx^2EI = wL^2 - 2wLx + wx^2$$

$$24TEI = w$$

$$T = \frac{w}{24EI}$$

$$24EI$$

$$12JEL = -2WL$$

$$S = -2WL$$

$$24EI$$

$$y = \left[\frac{WL^2}{4EI} \right] x^2 - \left[\frac{WL}{6EI} \right] x^3 + \left[\frac{W}{24EI} \right] x^4$$

$$y = \frac{WL^2 x^2}{4EI} - \frac{WL x^3}{6EI} + \frac{W x^4}{24EI}$$

$$y = \frac{6WL^2 x^2 - 4WL x^3 + W x^4}{24EI}$$

$$y = \frac{6WL^2 x^2 - 4WL x^3 + W x^4}{24EI}$$

$$24EI$$

$$PI: y = \frac{W}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$24EI$$

$$y = A + Bx + \frac{W}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$24EI$$

$$\text{at } x=0; y=0; \frac{dy}{dx} = 0$$

$$0 = A + B(0) + \frac{W}{24EI} [12L^2 x - 12L x^2 + 4x^3]$$

$$0 = B + \frac{W}{24EI} [12L^2(0) - 12(0)^2 + 4(0)^3]$$

$$24EI$$

$$B = 0$$

$$\text{when } A = B = 0$$

$$y = 0 + 0x + \frac{W}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$24EI$$

$$y = \frac{W}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$24EI$$

$$\text{when } x = L$$

$$y = \frac{W}{24EI} [6L^4 - 4L^4 + L^4]$$

$$24EI$$

$$y = \frac{W}{24EI} [3L^4]$$

$$24EI$$

$$y = \frac{WL^4}{8EI}$$

$$8EI$$