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Assignment I

1.) The power P dissipated in a resistor is given as eqn (1)

$$P = \frac{E^2}{R}$$

If $E = 200$ volts and $R = 8$ ohms, find the change in P resulting from a drop of 5 volts in E and an increase of 0.2 ohm in R .

2.) The deflection y at the centre of a circular plate suspended at the edge and uniformly

$$y = \frac{Kwd^4}{t^3}$$

where;

w = total load.

d = diameter of plate.

t = thickness

K = constant.

Calculate the approximate percentage change in y if w is increased by 3 percent, d is increased by 2½ percent and t is increased by 4 percent.

Solution

$$1.) P = \frac{E^2}{R} = E^2 R^{-1}$$

$$\delta P = \frac{\partial P}{\partial E} \cdot \delta E + \frac{\partial P}{\partial R} \cdot \delta R$$

$$\frac{\partial P}{\partial E} = 2ER^{-1} = \frac{2E}{R} = \frac{2(200)}{8} = 50.$$

$$\frac{\partial P}{\partial R} = -E^2 R^{-2} = -\frac{E^2}{R^2} = -\frac{(200)^2}{8^2} = -625.$$

$$\delta P = \frac{\partial P}{\partial E} \cdot \delta E + \frac{\partial P}{\partial R} \cdot \delta R$$

$$\delta P = 50(-5) + (-625)(0.2)$$

$$\delta P = -250 + -125.$$

$$\delta P = \underline{-375W.}$$

2) $y = \frac{Kwd^4}{t^3} = Kwd^4t^{-3}.$

$$\delta y = \frac{\partial y}{\partial w} \cdot \delta w + \frac{\partial y}{\partial d} \cdot \delta d + \frac{\partial y}{\partial t} \cdot \delta t.$$

$$\frac{\partial y}{\partial w} = Kd^4t^{-3} = \frac{Kd^4}{t^3}.$$

$$\frac{\partial y}{\partial d} = 4Kwd^3t^{-3} = \frac{4Kwd^3}{t^3}.$$

$$\frac{\partial y}{\partial t} = -3Kwd^4t^{-4} = -\frac{3Kwd^4}{t^4}.$$

$$\delta w = \frac{3}{100} \text{ of } w = \frac{3w}{100}$$

$$\delta d = \frac{2.5}{100} \text{ of } d = \frac{2.5d}{100}$$

$$\delta t = \frac{4}{100} \text{ of } t = \frac{4t}{100}$$

$$\delta y = \frac{\partial y}{\partial w} \cdot \delta w + \frac{\partial y}{\partial d} \cdot \delta d + \frac{\partial y}{\partial t} \cdot \delta t$$

$$\delta y = \frac{Kd^4}{t^3} \left(\frac{3w}{100} \right) + \frac{4Kwd^3}{t^3} \left(\frac{2.5d}{100} \right) + \left(-\frac{3Kwd^4}{t^4} \right) \left(\frac{4t}{100} \right)$$

$$\delta y = \frac{Kwd^4}{t^3} \left(\frac{3}{100} \right) + \frac{Kwd^4}{t^3} \left(\frac{10}{100} \right) + -\frac{Kwd^4}{t^3} \left(\frac{12}{100} \right)$$

$$\delta y = \frac{Kwd^4}{t^3} \left(\frac{3}{100} + \frac{10}{100} - \frac{12}{100} \right)$$

$$\delta y = \frac{Kwd^4}{t^3} \left(\frac{1}{100} \right)$$

Recall that;

$$\frac{Kwd^4}{t^3} = y$$

$$\delta y = y \left(\frac{1}{100} \right) = 1 \text{ percent of } y.$$