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1. The power P dissipated in a resistor is given as an Equation 1

$$P = \frac{E^2}{R}$$

If $E = 200$ Volts and $R = 8$ Ohms, Find the change in P resulting from a drop of 5 volts.

Solution.

$$dp = \frac{\partial p}{\partial E} \Delta E + \frac{\partial p}{\partial R} \Delta R$$

$$E = 200V \quad R = 8 \Omega \quad \Delta p = P \quad E_{\text{drop}} = 5V, \quad \Delta R = 0.2 \Omega$$

$$\frac{\partial p}{\partial E} = \frac{2E}{R} \quad \frac{\partial p}{\partial R} = -\frac{E^2}{R^2} = -\frac{E^2}{R^2}$$

$$\Delta E = -5V \quad \Delta R = 0.2 \Omega$$

$$\Delta p = \left(\frac{2E}{R} \right) (-5V) + \left(-\frac{E^2}{R^2} \right) (0.2 \Omega)$$

$$\Delta p = \left(\frac{2 \times 200}{8} \right) (-5) + \left(-\frac{(200)^2}{8^2} \right) (0.2) (8)$$

$$\Delta p = -250 + (-125)$$

$$\Delta p = -375 \text{ Watts.}$$

$\therefore p$ decrease by 375 Watts.

2. The deflection y at the Centre of a circular suspended at the edge and uniformly loaded is given in Equation (2).

$$y = \frac{kwd^4}{t^3}$$

where w = total load d = diameter of plate, t = thickness and k is a constant.
 Calculate the approximate percentage in y if w is increased by 3 per cent, d is increased by $2\frac{1}{2}$ per cent and t is increased by 4 per cent.

$$y = \frac{kwd^4}{t^3}$$

$$w = +3\% \quad d = 2\frac{1}{2}\% \quad t = 4\%$$

$$\frac{dy}{dw} \frac{dw}{w} + \frac{dy}{dd} \frac{dd}{d} + \frac{dy}{dt} \frac{dt}{t}$$

$$\frac{dy}{dw} = \frac{kd^4}{t^3} \quad \frac{dy}{dd} = \frac{4kwd^3}{t^3} \quad \frac{dy}{dt} = -\frac{3kwd^4}{t^4}$$

$$dw = \frac{3}{100} \text{ of } w \quad dd = \frac{5}{100} \text{ of } d \quad dt = \frac{4}{100} \text{ of } t$$

$$dy = \left(\frac{kd^4}{t^3}\right) \left(\frac{3w}{100}\right) + \left(\frac{4kwd^3}{t^3}\right) \left(\frac{5d}{100}\right) + \left(\frac{-3kwd^4}{t^4}\right) \left(\frac{4t}{100}\right)$$

$$dy = \left[\frac{3kwd^4}{100t^3} + \frac{20kwd^4}{200t^3} - \frac{12kwd^4}{100t^3} \right]$$

$$dy = \frac{kwd^4}{t^3} \left[\frac{3}{100} + \frac{20}{200} - \frac{12}{100} \right]$$

$$\frac{kwd^4}{t^3} \left[\frac{6 + 20 - 24}{200} \right]$$

$$\frac{kwd^4}{t^3} \left[\frac{2}{200} \right]$$

Recall $y = \frac{kwd^4}{t^3}$

$$y = \left[\frac{1}{100} \right]$$

$$dy = y \left[\frac{1}{100} \right]$$

Therefore y Increases by 1 percent (1%).