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$$(1) P = \frac{E^2}{R}$$

If  $E = 200$  volts and  $R = 80$  volts, find the change in  $P$  resulting from a drop.

Solution

$$dP = \frac{\partial P}{\partial E} dE + \frac{\partial P}{\partial R} dR$$

$$\frac{\partial P}{\partial E} = \frac{2E}{R} = \frac{2 \times 200}{80} = 5$$
$$\frac{\partial P}{\partial R} = -\frac{E^2}{R^2} = -\frac{200^2}{80^2} = -6.25$$

$$dE = -5 \text{ V} \quad dR = 0.2 \Omega$$

$$dP = \left( \frac{2E}{R} \right) (dE) + \left( -\frac{E^2}{R^2} \right) (dR)$$

$$dP = \left( \frac{2 \times 2000}{80} \right) (-5) + \left( -\frac{200^2}{80^2} \right) (0.2) (8)$$

$$dP = -250 + (-125)$$

$$dP = -375 \text{ watts}$$

Increase in  $P = -375$  watts

$$(2) y = \frac{kwd}{t^3}$$

$$w = t3\%, \delta = 2\frac{1}{2}\% \approx 5\frac{1}{2}\%; t = t\%$$

$$\therefore \frac{dy}{dw} \frac{\partial w}{\partial d} + \frac{dy}{d\delta} \frac{\partial \delta}{\partial d} + \frac{dy}{dt} \frac{\partial t}{\partial d}$$

$$\frac{dy}{dw} = \frac{k\delta^4}{t^3} - \frac{dy}{dt} = \frac{4kwd^3}{t^3} \cdot \frac{dt}{dt} = \frac{3kwd^4}{t^4}$$

$$\frac{dw}{w} = \frac{3}{100} \times w \quad \frac{\partial \delta}{\partial d} = \frac{5}{2} \times \frac{1}{100} \times \delta \quad \frac{dt}{dt} = \frac{4}{100} \times t$$

$$dy = \left( \frac{k\delta^4}{t^3} \right) \left( \frac{3w}{100} \right) + \left( \frac{4kwd^3}{t^3} \right) \left( \frac{5}{2} \times \frac{1}{100} \right) + \left( \frac{-3kwd^4}{t^4} \right) \left( \frac{4t}{100} \right)$$

$$dy = \left( \frac{3kw\delta^4}{100t^3} \right) + \left( \frac{20kwd^4}{200t^3} \right) - \left( \frac{12kwd^4}{100t^3} \right)$$

$$dy = \frac{kwd^4}{t^3} \left( \frac{3w}{100} + \frac{20}{200} - \frac{12}{100} \right)$$

$$\frac{kwd^4}{t^3} = \frac{6 + 20 - 24}{200}$$

$$\frac{kwd^4}{t^3} = \frac{2}{200} = \frac{1}{100}$$

$$\text{Recall } y = \frac{k\omega^4}{t^3}$$

$$\therefore y = \frac{1}{100}$$

$$\therefore \text{ (decrease) } = 1\%$$