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16/ENGG01/019
Petroleum Engineering
ENG 251 Assignment

$$1) P = \frac{E^2}{R}$$

$$E = 200V$$

$$R = 8\Omega$$

$$\Delta E = -5V$$

$$\Delta R = 0.2\Omega$$

$$\Delta P = \frac{\partial P}{\partial E} \Delta E + \frac{\partial P}{\partial R} \Delta R = \frac{2E\Delta E}{R} + \left(\frac{-E^2}{R^2}\right) \Delta R$$

$$= \frac{2 \times 200 \times -5}{8} - \left[\frac{200^2}{8^2} \times 0.2 \right]$$

$$= -250 - 125$$

$$\Delta P = -375W$$

$$2) y = \frac{kwd^4}{t^3}$$

$$\Delta w = 3\%, \Delta d = 2\frac{1}{2}\%, \Delta t = 1\%$$

$$dy = \frac{\partial y}{\partial w} \Delta w + \frac{\partial y}{\partial d} \Delta d + \frac{\partial y}{\partial t} \Delta t$$

$$= \frac{k d^4}{t^3} \Delta w + \frac{4kwd^3}{t^3} \Delta d + \left(\frac{-3kwd^4}{t^4}\right) \Delta t$$

$$= \frac{k d^4}{t^3} (3\%) + \frac{4kwd^3}{t^3} (2\frac{1}{2}\%) - \frac{3kwd^4}{t^4} (1\%)$$

$$\frac{3 \text{ kwd}^4}{100 \text{ f}^3} + \frac{10 \text{ kwd}^4}{100 \text{ f}^3} - \frac{12 \text{ kwd}^4}{100 \text{ f}^3}$$

$$= \frac{\text{kwd}^4}{\text{f}^3} \left(\frac{3}{100} + \frac{10}{100} - \frac{12}{100} \right)$$

$$= \frac{1 \text{ kwd}^4}{100 \text{ f}^3} = 1\% \cdot y$$