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Mechatronics Engineering

ENG 281

$$\textcircled{1} P = \frac{E^2}{R}$$

$$E = 200V, R = 8\Omega \quad \frac{dE}{dt} = -5V, \quad \frac{dR}{dt} = 0.2$$

$$\frac{dP}{dt} = \frac{dP}{dE} \cdot \frac{dE}{dt} + \frac{dP}{dR} \cdot \frac{dR}{dt}$$

$$\frac{dE}{dt} = \frac{2E}{R}, \quad \frac{dR}{dt} = -\frac{E^2}{R^2}$$

$$\therefore \frac{dP}{dt} = \frac{2E}{R} \cdot \frac{dE}{dt} + \left(-\frac{E^2}{R^2} \right) \frac{dR}{dt}$$

$$= \frac{2 \times 200 \times (-5)}{8} - \left[\frac{200^2 \times 0.2}{8^2} \right]$$

$$= -250 - 125$$

$$dP = -375W$$

$$\textcircled{2} y = \frac{Kwd^4}{t^3} \quad \frac{dw}{w} = 3\% \quad \frac{dd}{d} = 22\frac{1}{2}\% \quad \frac{dt}{t} = 4\%$$

$$\frac{dy}{dw} = \frac{dy}{dw} \frac{dw}{w} + \frac{dy}{dd} \cdot \frac{dd}{d} + \frac{dy}{dt} \cdot \frac{dt}{t} \Rightarrow \frac{kd^4}{t^3} \frac{dw}{w}$$

$$= \frac{kd^4}{t^3} (3\%) + \frac{4kwd^3}{t^3} \left(\frac{5d\%}{2} \right) - \frac{3kwd^4}{t^4} (4\%)$$

$$= \frac{3}{100} \frac{kwd^4}{t^3} + \frac{10}{100} \frac{kwd^4}{t^3} - \frac{12kwd^4}{100t^3}$$

$$\Rightarrow \frac{kwd^4}{t^3} \left(\frac{3}{100} + \frac{10}{100} - \frac{12}{100} \right)$$

$$= \frac{1}{100} \frac{kwd^4}{t^3} = 1\%y$$