

ENQ281

① $P = \frac{E^2}{R}$ given $E = 200V$
 $R = 8\Omega$
 $\delta E = -5V$
 $\delta R = 0.2\Omega$

$P = f(E, R)$

$\delta P = \frac{\partial P}{\partial E} \delta E + \frac{\partial P}{\partial R} \delta R$

$\frac{\partial P}{\partial E} = 2E \times \frac{1}{R} = \frac{2E}{R}$

$\frac{\partial P}{\partial R} = -E^2 R^{-2} = -\frac{E^2}{R^2}$

$\delta P = \frac{2E}{R} (-5) - \frac{E^2}{R^2} (0.2)$

$= \frac{2(200)(-5)}{8} - \frac{(200)^2(0.2)}{40,000(8)^2}$

$= \frac{-2000}{8} - \frac{28 \times 0.2}{64}$

$= -250 - 125 = -375 \text{ W}$

P decreases by 375 watts.

② $y = \frac{kwd^4}{t^3}$ given $\delta w = \frac{3w}{100}$

$\delta d = \frac{25d}{100}$

$\delta t = \frac{4t}{100}$

$\delta y = \frac{\partial y}{\partial w} \delta w + \frac{\partial y}{\partial d} \delta d + \frac{\partial y}{\partial t} \delta t$

$\frac{\partial y}{\partial w} = \frac{kd^4}{t^3}$, $\frac{\partial y}{\partial d} = \frac{4kwd^3}{t^3}$

$\frac{\partial y}{\partial t} = \frac{3kwd}{t^4}$

$\delta y = \frac{kd^4}{t^3} \left[\frac{3w}{100} \right] + \frac{4kwd^3}{t^3} \left[\frac{2.5d}{100} \right]$

$- \frac{3kwd}{t^4} \left[\frac{4t}{100} \right]$

$= \frac{kwd^4}{t^3} \left[\frac{3}{100} \right] + \frac{kwd^4}{t^3} \left[\frac{10}{100} \right]$

$- \frac{kwd^4}{t^3} \left[\frac{12}{100} \right]$

$= \frac{kwd^4}{t^3} \left[\frac{3}{100} + \frac{10}{100} - \frac{12}{100} \right]$

$= y \left[\frac{1}{100} \right]$

$= 1$ percent of y .