

1.  $y = e^{x^2+x}$

$v = 1 \quad v' = 0$

$u = e^{x^2+x} \quad u^n = (2x+1)^n e^{x^2+x}$

$y = u^n \cdot v^0$

$y^n = (2x+1)^n e^{x^2+x}$

$y' = (2x+1)' e^{x^2+x}$

$v = 2x+1 \quad v' = 2 \quad v'' = 0$  (From  $y'$ )

$u^n = (2x+1)^n e^{x^2+x}$

$y'' = u^n \cdot v^2 + n u^{(n-1)} v' + 0$

$= (2x+1)' e^{x^2+x} \cdot 2x+1 + n (2x+1)^{n-1} e^{x^2+x} \cdot 2 + 0$

$= (2x+1)' e^{x^2+x} (2x+1) + 2n (2x+1)^{n-1} e^{x^2+x}$

Recall  $(2x+1)' e^{x^2+x} = y'$   
 $e^{x^2+x} = y$

$y'' = y' (2x+1) + 2n y$

Prove that  $y^{(n+2)} = (2x+1) y^{(n+1)} + 2(n+1) y^n$

where  $w = y''$

$y'' - y' (2x+1) - 2y = 0$

$v = 1 \quad v' = 0$

$u = y'' \quad u^n = y^{(n+2)}$

$w^n = u^n v + 0$

$w^n = y^{(n+2)}$

$w^n = y^{(n+2)}$

where  $w^n = (2x+1) y^n$

$v = 2x+1 \quad v' = 2 \quad v'' = 0$

$u = y' \quad u^n = y^{(n+1)}$

$w^n = u^n v^0 + n u^{(n-1)} v'$

$w^n = (n+1) y^{(n+1)}$