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1.) The power P dissipated in a resistor is given by $P = \frac{E^2}{R}$ if $E = 200$ volts and $R = 80 \Omega$, find the change in P , resulting from a drop of 3 volts in E and an increase of 0.2 ohms

Soln

$$\delta P = \frac{\partial P}{\partial E} \delta E + \frac{\partial P}{\partial R} \delta R$$

$$P = \frac{E^2}{R} \quad \frac{\partial P}{\partial R} = -\frac{E^2}{R^2}$$

$$\frac{\partial P}{\partial E} = 2ER^{-1} = \frac{2E}{R}$$

$$R = 8, E = 200, \delta R = 0.2, \delta E = -3$$
$$\delta P = \frac{(2)(200)(-3)}{8} - \frac{(200)^2(0.2)}{8^2}$$

$$= -250 - 125$$

$$= -375$$

Hence power decreases by 375 watts.

2.) Calculate the approximate percentage change in y if w is increased by 3 percent, d is increased by 2% percent as t is increased by 4 percent.

Soln

$$\delta y = w \left(\frac{dy}{dw} \delta w + \frac{dy}{dd} \delta d + \frac{dy}{dt} \delta t \right)$$

$$\frac{dy}{dw} = \frac{d^4}{t^5}, \quad \frac{dy}{dd} = \frac{4d^3}{t^3} = \frac{dy}{dt} = \frac{-5wd^5}{t^6}$$

$$\delta w = \frac{3w}{100}, \quad \delta d = \frac{2d}{100}, \quad \delta t = \frac{4t}{100}$$

$$\delta y = \left(\frac{K d^4}{t^3} \left(\frac{3w}{w} \right) + \frac{4wt + wd^3}{t^3} \left(\frac{\delta d}{2w} \right) \right) = \frac{K d^4}{t^3} \left(\frac{4d}{w} \right)$$

$$\delta y = \frac{31wd^4}{100t^3} + \frac{200wd^4}{200t^3} - \frac{10wd^4}{100t^3}$$

$$\delta y = \frac{1}{100} \left(\frac{31wd^4}{t^3} + \frac{10wd^4}{t^3} - \frac{12wd^4}{t^3} \right)$$

$$\delta y = \frac{1}{100} (11y)$$

$$\delta y = \frac{1}{100} y$$

$\therefore y$ increases by 1/100 percent.