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Assignment 2

$$(1) \frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 5y = 6\sin\theta$$

$$m^2 + 4m + 5 = 0$$

$$m = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \quad m = \frac{-4 \pm \sqrt{4^2 - (4 \times 1 \times 5)}}{2 \times 1}$$

$$m = \frac{-4 \pm \sqrt{16 - 20}}{2} = \frac{-4 \pm \sqrt{-4}}{2}$$

$$m = \frac{-4 \pm \sqrt{4} \cdot \sqrt{-1}}{2}$$

$$m = -\frac{4}{2} \pm \frac{2j}{2}$$

$$m = -2 \pm j$$

$$y = e^{-2\theta} [C \cos\theta + D \sin\theta]$$

PI \Rightarrow

$$y = A \cos\theta + B \sin\theta$$

$$\frac{dy}{d\theta} = -A \sin\theta + B \cos\theta$$

$$\frac{d^2y}{d\theta^2} = -A \cos\theta - B \sin\theta$$

$$\therefore [A \cos\theta - B \sin\theta] + 4[-A \sin\theta + B \cos\theta] + 5[A \cos\theta + B \sin\theta] = 6 \sin\theta$$

$$-A \cos\theta - B \sin\theta - 4A \sin\theta - 4B \cos\theta + 5A \cos\theta + 5B \sin\theta = 6 \sin\theta$$

$$-A \cos\theta + 4B \sin\theta + 5A \cos\theta - B \sin\theta - 4A \sin\theta + 5B \sin\theta = 6 \sin\theta$$

Comparing coefficient:

$$-A + 4B + 5A + 5B = 0$$

$$4A + 4B = 0 \quad \text{--- eqn (1)}$$

$$-B - 4A + 5B = 6$$

$$= 4A + 4B = 6 \quad \text{--- eqn (2)}$$

adding eqn (1) & eqn (2)

$$5B = 6$$

$$B = \frac{3}{2}$$

$$4A + 4\left(\frac{3}{2}\right) = 0$$

$$4A = -6 \quad A = -\frac{3}{2}$$

$$y = e^{2x}(\cos\theta - \frac{3}{2}\sin\theta) - \frac{3}{2}\cos\theta + \frac{3}{2}\sin\theta$$

$$y(0) = 0 \quad y'(0) = \frac{3}{2}$$

$$y = e^{2x}[(\cos\theta) + (\sin\theta)]$$

$$-2e^{2x} + \frac{3}{2}\sin\theta + \frac{3}{2}\cos\theta$$

$$-2 + \frac{3}{2}\sin\theta + \frac{3}{2}\cos\theta = 0$$

$$\frac{3}{2}\cos\theta = 2 - \frac{3}{2}\sin\theta$$

$$-\cos\theta = \sin\theta$$

$$\text{Divide both sides by } -\cos\theta$$

$$\frac{-\cos\theta}{-\cos\theta} = \frac{\sin\theta}{-\cos\theta}$$

$$\frac{-\sin\theta}{-\cos\theta} = 1$$

$$-\tan\theta = 1$$

$$\tan\theta = -1$$

$$\theta = \tan^{-1}(-1)$$

$$\theta = 135^\circ$$

$$EI \frac{d^4 y}{dx^4} = \frac{w}{2}(1-x)^2$$

Solution

$$EI m^4 = 0$$

$$m^4 = 0$$

$$m = +\sqrt[4]{0}$$

$$m = -\sqrt[4]{0}$$

$$y = e^{mx}(A+Bx)$$

$$y = A+Bx \quad \text{--- (F)}$$

$$y = Px^2 + Qx^3 + Rx^4$$

$$d^4 y/dx^4 = 24P + 36Qx + 48Rx^2$$

$$24P = \frac{w}{2}$$

$$36Qx = \frac{w}{2}(1-x)$$

$$48Rx^2 = \frac{w}{2}(1-x)^2$$

$$24PEI = \frac{w}{2}EI$$

$$36QEIx = \frac{w}{2}EI(1-x)$$

$$48REIx^2 = \frac{w}{2}EI(1-x)^2$$

$$R = \frac{w}{24EI} \quad \text{--- (1)}$$

$$12QEI = -2wL$$

$$Q = \frac{-2wL}{12EI} = \frac{-wL}{6EI} \quad \text{--- (2)}$$

$$4PEI = wL^2$$

$$P = \frac{wL^2}{4EI}$$

$$y = \left[\frac{wL^2}{4EI} \right] x^2 - \left[\frac{wL}{6EI} \right] x^3 + \left[\frac{w}{24EI} \right] x^4$$

$$= \frac{wL^2}{4EI} x^2 - \frac{wL}{6EI} x^3 + \frac{w}{24EI} x^4$$

$$= \frac{w}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$= \frac{w}{24EI} [6L^2 x^2 - 4L x^3 + x^4] \quad \text{--- PI}$$

$$y = A + B(1-x) \frac{w}{24EI} [6L^2 x^2 - 4L x^3 + x^4]$$

$$y(0) = 0, \quad x=0 \quad \frac{dy}{dx} = 0$$

$$0 = A + B(1-0) \frac{w}{24EI} [6L^2(0) - 4L(0) + 0]$$

$$A = 0$$

$$\frac{dy}{dx} = \frac{B + W}{24EI} [6l^2(x) - 4l(x) + 0]$$

$$0 = \frac{B + W}{24EI} [12(0) - 12(0) + 4(0)]$$

$$B = 0$$

Particular solution

$$y = \frac{W}{24EI} [6l^2x^2 - 4lx^3 + x^4]$$

$$y = \frac{Wx^2}{24EI} [6l^2 - 4lx + x^2]$$

$$y = \frac{Wx^2}{24EI} [x^2 - 4lx + 6l^2]$$

When $x = l$

$$y = \frac{Wl^2}{24EI} [l^2 - 4l^2 + 6l^2]$$

$$y = \frac{Wl^4}{8EI}$$