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15/ENG05/007

Mechanics Engineering

1) $T_1 e^{2x+x^2}$

soln

$$y' = (2x+1)e^{2x+x^2}$$

$$y'' = 2e^{2x+x^2} + (2x+1)(2x+1)e^{2x+x^2}$$

$$y'' = 2y + (2x+1)y'$$

hence

$$y'' - y'(2x+1) = 2y$$

$$y^{(n+2)} - y^{(n+1)}(2x+1) + y^{(n)} = 2y^{(n)}$$

$$y^{(n+2)} = (2x+1)y^{(n+1)} + 2y^{(n)}$$

2) $T_2 x^3 e^{4x}$

$$y^n = \frac{4^n x^n}{n!} + \frac{n 4^{n-1} x^{n-1}}{2!} + \frac{n(n-1) 4^{n-2} x^{n-2}}{3!} + \dots +$$

x^3 , $\sqrt{\quad}$ and $4 = e^{4x}$

$$T_5 = (60)^5 e^{4x} \cdot x^3 + 5(4)^4 e^{4x} \cdot 3x^2 + 10(4)^3 e^{4x} \cdot 6x + 10(4)^2 e^{4x} \cdot 6 + 0$$

$$y_5 = 60240x^3 e^{4x} + 38400x^2 e^{4x} + 38400x e^{4x} + 46080 e^{4x} + 0$$

$$y_5 = e^{4x} [60240x^3 + 38400x^2 + 38400x + 46080]$$

$$3) x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = 0$$

$$x^2 y'' + x y' + y = 0$$

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using Leibnitz theorem

$$y^n = x^2 y^{(n+2)} + 2x y^{(n+1)} + n(n-1)y^n + x y^{(n+1)} + n y^{(n)} + y^{(n)}$$

$$y^n = y^{(n+2)}(x^2) + y^{(n+1)}(2nx+x) + y^{(n)}(n(n-1)+n+1)$$

$$y^n = x^2 y^{(n+2)} + (2n+1)x y^{(n+1)} + (n^2-1)y^n$$

$$x^2 y^{(n+2)} + (2n+1)x y^{(n+1)} + (n^2-1)y^n = 0$$