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Dept: Petroleum Engineering

Course: ENG 381 Assignment 5

$$3s^2 + 14 = A(s^2 + 4) + B(3s - 6)$$

$$4A - 6B = 14$$

$$-6B = 14 - 12$$

$$B = -1/3$$

$$Y(s) = \frac{3}{s} - \frac{1}{3(s^2 + 4)}$$

$$[3][Ls^{-1}] - \frac{1}{3}[Ls^{-2} + 4]$$

$$= e^{2t} - \frac{1}{6} \sin 2t$$

$$1) \frac{dy}{dt} + 3y = e^{-2t}$$

$$y(t) + 3y(t) = e^{-2t}$$

$$L[y'(t)] = sY(s) - Y(s)$$

$$L[y(t)] = Y(s), L[e^{-2t}] = \frac{1}{s+2}$$

$$sY(s) = Y(s) + 3Y(s) = \frac{1}{s+2}$$

$$(s-3)Y(s) - 2 = \frac{1}{s+2}$$

$$(s-3)Y(s) = \frac{1}{s+2} + 2 = \frac{1+2s+4}{s+2} = \frac{2s+5}{s+2}$$

$$Y(s) = \frac{2s+5}{(s+2)(s-3)} = \frac{A}{s+2} + \frac{B}{s-3}$$

$$2(-2) + 5 = A(-2-3) \Rightarrow A = \frac{1}{-5}$$

$$2(3) + 5 = B(3-2) \Rightarrow B = \frac{11}{-5}$$

$$Y(s) = \frac{-1}{5(s+2)} + \frac{11}{5(s-3)} = -\frac{1}{5}e^{-2t} + \frac{11}{5}e^{3t}$$

$$1) 3 \frac{dy}{dt} - 6y = \sin 2t = 3y'(t) - 6y(t)$$

$$L[y'(t)] = sY(s) - Y(s)$$

$$L[y(t)] = Y(s)$$

$$L[\sin 2t] = \frac{2}{s^2+4} = \frac{2}{s^2+4}$$

$$3s + Y(s) - 3Y(s) - 6Y(s) = \frac{2}{s^2+4}$$

$$Y(s)[3s-6] = \frac{2}{s^2+4} + 3 = \frac{2+3s^2+12}{s^2+4}$$

$$\frac{2+3s^2+12}{s^2+4} = \frac{3s^2+14}{s^2+4}$$

$$Y(s) = \frac{3s^2+14}{(3s-6)(s^2+4)} = \frac{A}{3s-6} + \frac{B}{s^2+4}$$

$$11) \frac{dy}{dt} - 4y = 8$$

$$y'(t) = 4y(t) = 8$$

$$y'(t) - 4y(t) = 8$$

$$sY(s) - Y(s) - 4Y(s) = \frac{8}{s}$$

$$(s-4)Y(s) = \frac{8}{s} + 2 = \frac{8+2s}{s}$$

$$Y(s) = \frac{2s+8}{s(s-4)}$$

$$\frac{2s+8}{s(s-4)} = \frac{A}{s} + \frac{B}{s-4}$$

$$2s+8 = A(s-4) + B(s)$$

$$2(0)+8 = A(0-4) \Rightarrow A = -2$$

$$2(4)+8 = A(4-4) + B(4)$$

$$B = 4$$

$$L^{-1}[\frac{-2}{s} + \frac{4}{s-4}] = -2 + 4e^{4t}$$

$$1V) \frac{d^2y}{dt^2} - 2 \frac{dy}{dt} + 5y = e^{2t}$$

$$y''(t) - 2y'(t) + 5y(t) = e^{2t}$$

$$L[y''(t)] = s^2Y(s) - sY(s) - Y'(s)$$

$$L[y'(t)] = sY(s) - Y(s)$$

$$L[y(t)] = Y(s)$$

$$s^2Y(s) - sY(s) - Y'(s) - 2sY(s) + 2Y(s) + 5Y(s) = \frac{1}{s-2}$$

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$$[(s^2 - 2s + 5)Y(s) + (2 - s)Y_0 - Y'(0)] = \frac{1}{s-2}$$

$$Y(s) = \frac{2s - 5}{(s-3)(s-2)(s+1)} = \frac{A}{s-3} + \frac{B}{s+2} + \frac{C}{s+1}$$

$$[(s^2 - 2s + 5)Y(s)] = \frac{1}{s-2} - 2(2-s) + 1$$

$$2s - 5 = A(s-2)(s+1) + B(s-3)(s+1) + C(s-3)(s-2)$$

$$= \frac{1}{s-2} + 2s - 4 + 1 = \frac{1}{s-2} + 2s - 3$$

$$2s - 5 = A(s^2 - 6s + 8) + B(s^2 - 7s + 2) + C(s^2 - 5s + 6)$$

$$= \frac{1 + (2s-3)(3-2)}{(s-2)} + \frac{1s}{s-2}$$

$$2(3) - 5 = A(3-2)(3+1)$$

$$2(4) - 5 = C(4-3)(4-2)$$

$$-6A - 7B - 5C = 7$$

$$-6C - 17 - 7(B) - 5(\frac{3}{2}) = 7$$

$$-7B = 2 + \frac{15}{2} - 6 = \frac{4+15-12}{2} = \frac{7}{2}$$

$$Y(s) = \frac{2s^2 - 7s + 7}{(s-2)(s^2 + 2s + 5)}$$

$$2s^2 - 7s + 7 = \frac{A}{s-2} + \frac{B}{s^2 + 2s + 5}$$

$$B = -1/2$$

$$2s^2 - 7s + 7 = A(s^2 - 2s + 5) + B(s^2 + 2s + 5)$$

$$L^{-1} \left[ \frac{1}{s-3} - \frac{1}{2(s-2)} + \frac{3}{2(s+1)} \right]$$

$$A = 2$$

$$= 2e^{3t} - \frac{1}{2}e^{2t} + \frac{3}{2}e^{-t}$$

$$-2A + B = -7$$

$$B = -7 + 4 = -3$$

$$= \frac{2}{s-2} - \frac{3}{s^2 + 2s + 5}$$

$$2e^{2t} - \frac{7}{3} \sin 2t$$

$$V) \frac{d^2y}{dt^2} - 6\frac{dy}{dt} + 8y = e^{3t}$$

$$s^2 Y(s) - sY(0) - Y'(0) - 6sY(s) + 6Y(0) + 8Y(s) = \frac{1}{s-3}$$

$$[(s^2 - 6s + 8)Y(s) + (6-s)Y(0) - Y'(0)] = \frac{1}{s-3}$$

$$[(s^2 - 6s + 8)Y(s)] = \frac{1}{s-3} + 2 = \frac{1 + 2s - 5}{s-3}$$

$$= \frac{2s - 5}{s-3}$$