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$$\frac{dy}{dt} = ky$$

dt

$$\frac{1}{y} dy = k dt$$

y

$$\int \frac{1}{y} dy = \int k dt$$

$$\ln y = kt + C$$

$$\therefore y = e^{kt+C}$$

$$y = e^{kt} \cdot e^C$$

Since e^C is also a constant it can be represented as C

$$y = e^{kt} \cdot C$$

$$y = Ce^{kt}$$

Given initial conditions

$$\text{at } t=0 \quad y=20$$

$$20 = Ce^{k(0)}$$

$$20 = Ce^0$$

$$20 = C \times 1$$

$$\therefore C = 20$$

Our model becomes

$$y = 20e^{kt}$$

b) Expressing $1\frac{1}{2}$ days in hours

$$24 \text{ hr} \rightarrow 1 \text{ day}$$

$$\therefore 1\frac{1}{2} \text{ days} = 36 \text{ hrs}$$

also y doubles every 5 hours \therefore at $t=5$ $y=40$ (i.e. $t=0$, $y=20$)

$$\therefore 40 = 20e^{k(5)}$$

$$\frac{40}{20} = e^{5k}$$

$$20$$