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16/ENG041017

Elect / Elect

Cys {ENG282}

$$2y_0 = y$$

When  $t = 5$

$$\frac{dy}{dt} = ky$$

dt

$$dy = y k dt$$

y

$$\int \frac{1}{y} dy = k \int dt$$

$$\ln y = t k + C$$

$$y = e^{\ln y} = e^{t k} \cdot e^C \text{ (where } e^C = y_0)$$

$$y = y_0 e^{t k}$$

If  $y_0 = 20$  and  $t = 5$

$$2y_0 = y_0 e^{t k}$$

$$2 \times 20 = 20 e^{5k}$$

$$40 = 20 e^{5k}$$

$$40 = 20 e^{5k}$$

20

$$2 = e^{5k}$$

$$\ln 2 = \ln e^{5k}$$

$$\ln 2 = 5k$$

$$k = \frac{\ln 2}{5}$$

5

$$k = \frac{0.69315}{5}$$

5

$$k = 0.1386$$

$$y = y_0 e^{0.1386t}$$

$$(y = 20 e^{0.1386t}) \text{ is General Solution for Model}$$

ii) (Population of Bacteria =  $1\frac{1}{2}$  days)

(=  $24 \times 12 = 36$  hours)

$$y = y_0 e^{0.1386t}$$

$$y = y_0 e^{0.1386 \times 36}$$

$$y = 200 e^{0.1386 \times 36}$$

$$y = 200 \times 1.99$$

$$y = 20 \times 146.99$$

$$y = 2939.8$$