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 MATHEMATICAL ENGINEERING.

ANSWER

a)  $\frac{dy}{dt} = ky$

$$\int \frac{1}{y} dy = \int k dt$$

$\ln y = kt + c$   
 $y = e^{kt+c}$   
 $y = e^{kt} \cdot e^c$

Let  $e^c = y_0$   
 $y = y_0 \cdot e^{kt}$

But  $y = 20$  and  $t = 5$  hrs  
 $20 = y_0 \cdot e^{5k}$   
 $\ln 20 = \ln y_0 + 5k$

$\ln 2 = \ln y_0 + 5k$   
 $k = \frac{\ln 2 - \ln y_0}{5} = \frac{\ln 2}{5} = 0.139$

or  $y = y_0 \cdot e^{0.139t}$

b) 24 hrs = 1 day

$x = 1/2$  day

$x = 24 \times 1/2 = 12$  hrs

When  $y_0 = 20$  and  $t = 36$

$y = 20 \cdot e^{0.139 \times 36}$

$y = 2080.8$