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**DEPARTMENT OF CHEMICAL AND PETROLEUM ENGINEERING**

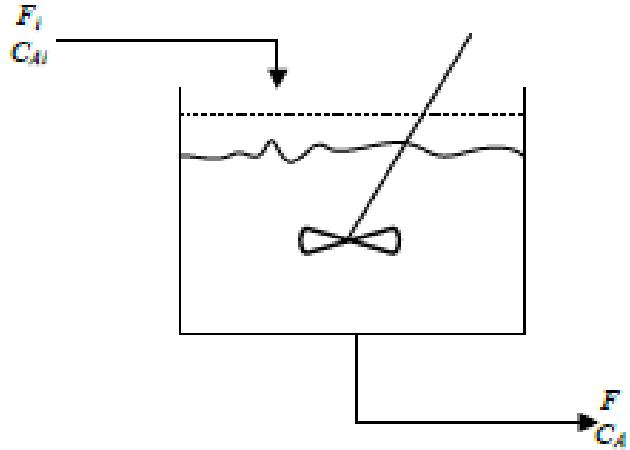
**PROCESS DYNAMICS & CONTROL II**

**CHE 532 ASSIGNMENT I**

**BY**

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**14/ENG01/016**



Overall material balance:

$$\{\text{Accumulation of mass}\} = \{\text{mass in}\} - \{\text{mass out}\}$$

$$\frac{d(\rho V)}{dt} = \rho F_i - \rho F \quad (1a)$$

$$\frac{dV}{dt} = F_i - F \quad (1b)$$

Component balance of A

$$\begin{aligned} & \{\text{Accumulation of component mass}\} \\ &= \{\text{component mass in}\} - \{\text{component mass out}\} \\ &+ \{\text{generation of component mass}\} \end{aligned}$$

$$\frac{d(C_A V)}{dt} = F_i C_{Ai} - F C_A + V r_A$$

But:

$$r_A = -K C_A$$

$$\frac{d(C_A V)}{dt} = V \frac{dC_A}{dt} + C_A \frac{dV}{dt}$$

Therefore:

$$V \frac{dC_A}{dt} + C_A \frac{dV}{dt} = F_i C_{Ai} - FC_A - VKC_A$$

$$V \frac{d(C_A)}{dt} = F_i C_{Ai} - FC_A - VKC_A - C_A \frac{dV}{dt} \quad (2)$$

Recall:

$$\frac{dV}{dt} = F_i - F$$

Therefore:

$$V \frac{d(C_A)}{dt} = F_i C_{Ai} - FC_A - VKC_A - C_A(F_i - F)$$

$$V \frac{d(C_A)}{dt} = F_i C_{Ai} - FC_A - VKC_A - F_i C_A + FC_A$$

$$V \frac{d(C_A)}{dt} = F_i C_{Ai} - VKC_A - F_i C_A$$

$$V \frac{d(C_A)}{dt} = F_i C_{Ai} - C_A(F_i + VK)$$

$$V \frac{d(C_A)}{dt} + C_A(F_i + VK) = F_i C_{Ai}$$

$$F_i = F$$

$$\frac{d(C_A)}{dt} + \left( \frac{F + VK}{V} \right) C_A = \frac{F}{V} C_{Ai}$$

$$\frac{d(C_A)}{dt} + \frac{1}{\tau_p} C_A = \frac{F}{V} C_{Ai} \quad (3)$$

$$\tau_p \frac{d(C_A)}{dt} + C_A = \frac{F\tau}{V} C_{Ai}$$

$$\tau_p \frac{d(C_A)}{dt} + C_A = \frac{F}{V} * \frac{V}{F + VK} C_{Ai}$$

$$\tau_p \frac{d(C_A)}{dt} + C_A = \frac{F}{F + VK} C_{Ai}$$

$$\tau_p \frac{d(C_A)}{dt} + C_A = K_p C_{Ai}$$

$$\tau_p \frac{d(C_{As})}{dt} + C_{As} = K_p C_{Ais}$$

With time constant  $\tau_p = \frac{V}{F + VK}$  \*

where the steady state gain,  $K_p = \frac{F}{F + V_k}$  \*\*

Equation 3 is the dynamic equation. To find the transfer function, we'll have to get the Laplace of the system:

$$\overline{C_A} = C_A(s)$$

$$\overline{C_{Ai}} = C_{Ai}(s)$$

$$\overline{C_A}(t) = sC_A(s) - C_A(0)$$

$$\tau_p \frac{d(C_A - C_{As})}{dt} + (C_A - C_{As}) = K_p (C_{Ai} - C_{Ais})$$

$$\tau_p \frac{d(\overline{C_A})}{dt} + \overline{C_A} = K_p \overline{C_{Ai}}$$

$$\tau_p [S\overline{C_A}(s) - \overline{C_A}(0)] + \overline{C_A}(s) = K_p \overline{C_{Ai}}(s)$$

$$\tau_p S\overline{C_A}(s) + \overline{C_A}(s) = K_p \overline{C_{Ai}}(s)$$

$$\overline{C_A}(s)(\tau_p S + 1) = K_p \overline{C_{Ai}}(s)$$

$$\frac{\overline{C_A}(s)}{\overline{C_{Ai}}(s)} = \frac{K_p}{(\tau_p S + 1)}$$

$$G(s) = \frac{\overline{C_A}(s)}{\overline{C_{Ai}}(s)} = \frac{K_p}{(\tau_p S + 1)}$$

The screenshot shows a MATLAB code editor window titled "Editor - C:\Users\Muniratu Abubakar\Desktop\CHE 531 - 14-ENG01-016\assignmentsoluti...". The current file is "assignmentsolution.m", which contains the following MATLAB code:

```
1 - commandwindow
2 - clear all
3 - clc
4 - bdclose all
5
6 - F=0.085
7 - V=2.1
8 - K=0.04
9 - Kp=F/ (F+(V*K) )
10 - Tp=V/ (F+(V*K) )
11 - Steptime=0.5
12 - ufinal=1.5
13 - open('Assignment1')
14 - sim('Assignment1', [0 100])
15 - [t,x,y]=sim('Assignment1', [0 100])
16 - plot(t,y)
17 - xlabel('Time (mins')
18 - ylabel('concentration (mol/m^3)')
19
```

Figure 1. 1. open loop dynamic model simulation

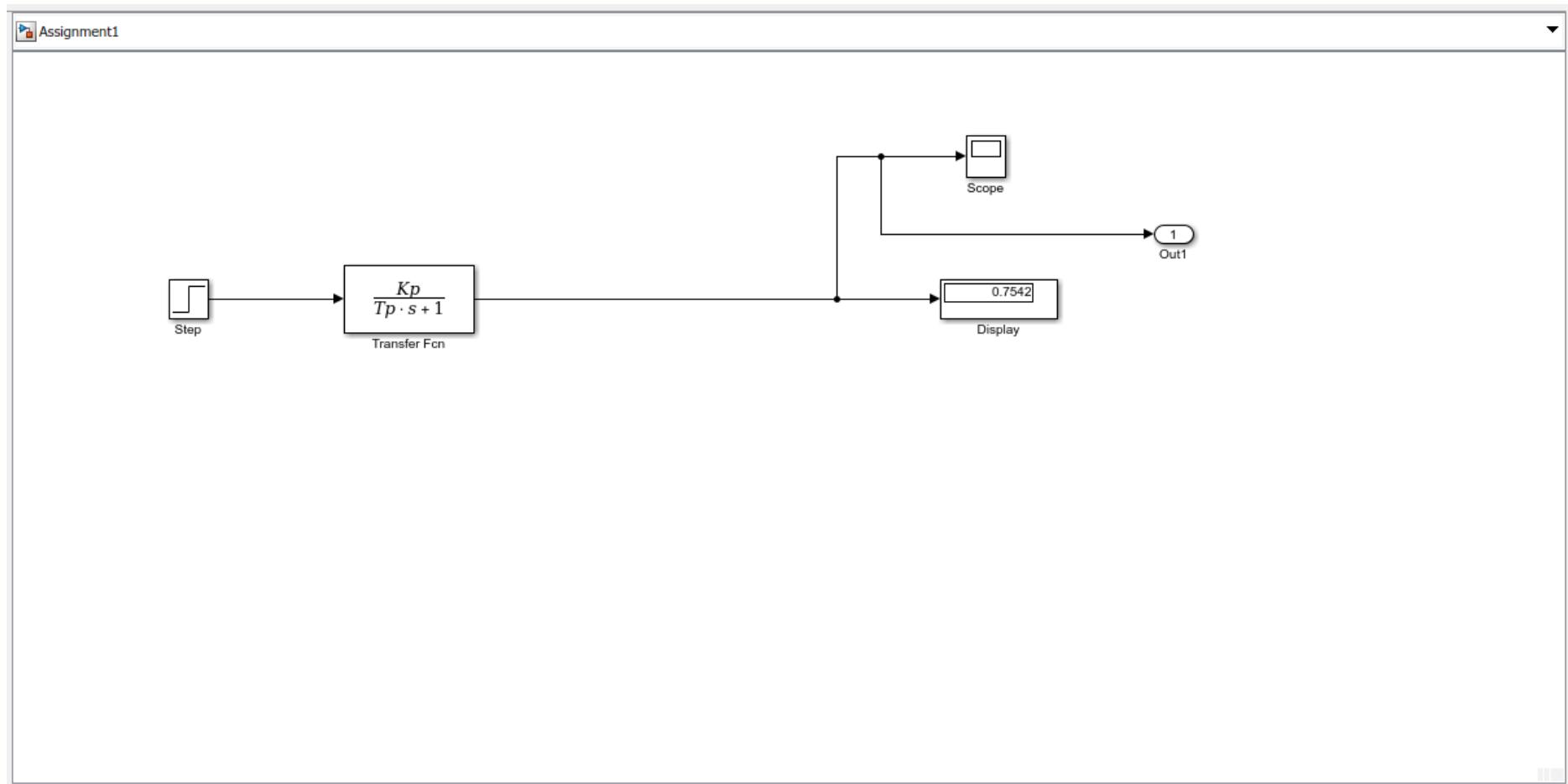


Figure 1. 2. Open loop dynamic model

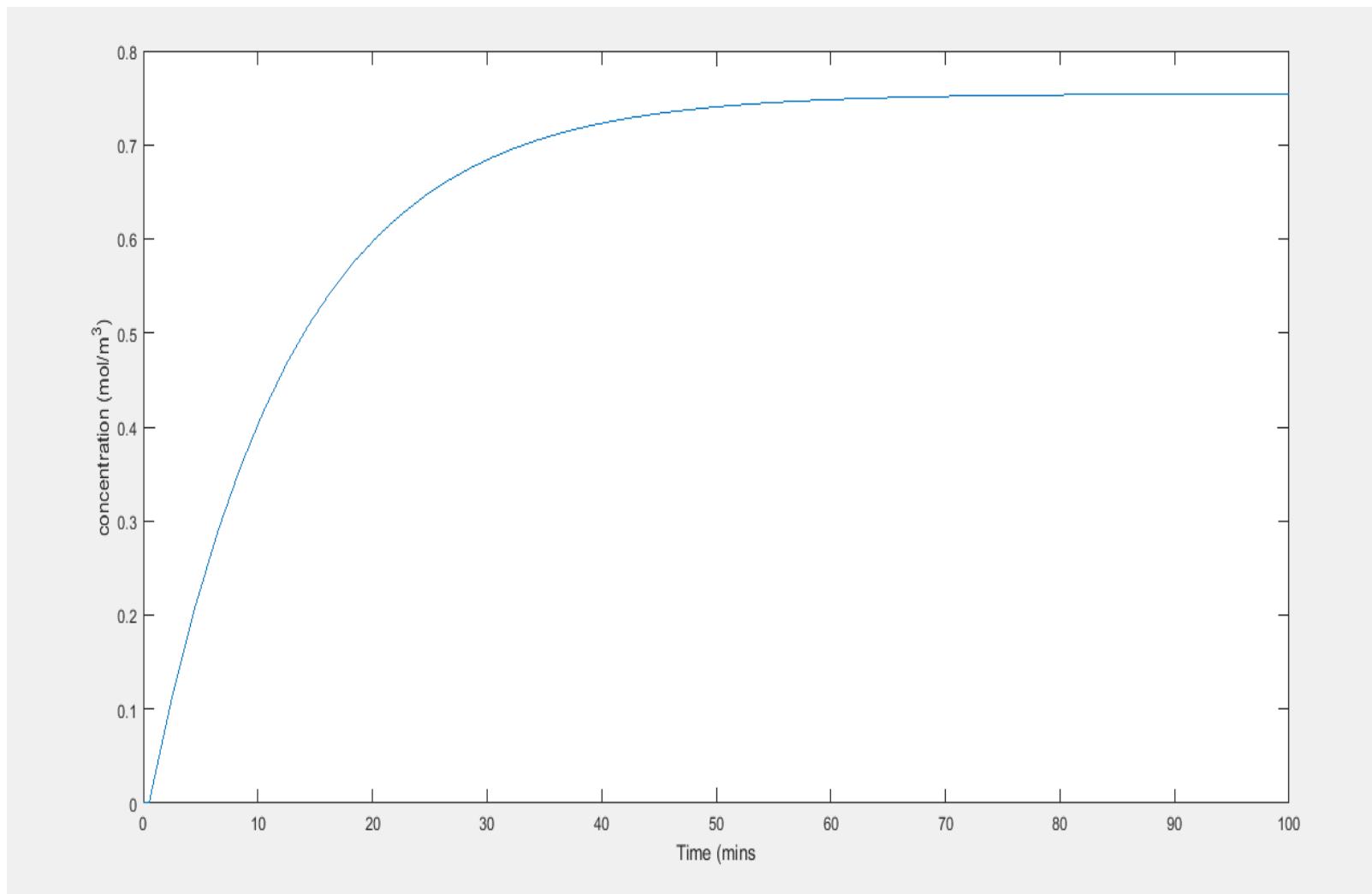


Figure 1. 3. Open loop dynamic model plot

The screenshot shows the MATLAB Editor window with two tabs: 'assignmentsolution.m' and 'Assignmentsolution2.m'. The 'assignmentsolution.m' tab is active, displaying the following MATLAB script:

```
2 - clear all
3 - clc
4 - bdclose all
5
6 - F=0.085;
7 - V=2.1;
8 - K=0.04;
9 - Kp=F/ (F+ (V*K) )
10 - Tp=V/ (F+ (V*K) )
11 - Steptime=0.15;
12 - ufinal=2.5;
13 - Kc=0.5
14 - Ti=0.3
15 - Td=0.1
16 - P=Kc
17 - I=Kc/Ti
18 - D=Kc*Td
19
20 - open('Assignmentclosedloop')
21 - [t,x,y]=sim('Assignmentclosedloop', [0 100])
22 - plot(t,y)
23 - hold on
24 - ssvalue = ufinal*I
25 - Abodiga = length(y)
26 - ssvalueeg = ssvalue*ones(Abodiga,1)
27 - plot(t,ssvalueeg)
28 - xlabel('Time (mins)')
29 - ylabel('concentration (mol/m^3)')
30 - legend('Dynamic response', 'set point')
```

Figure 1. 4. closed loop dynamic model simulation

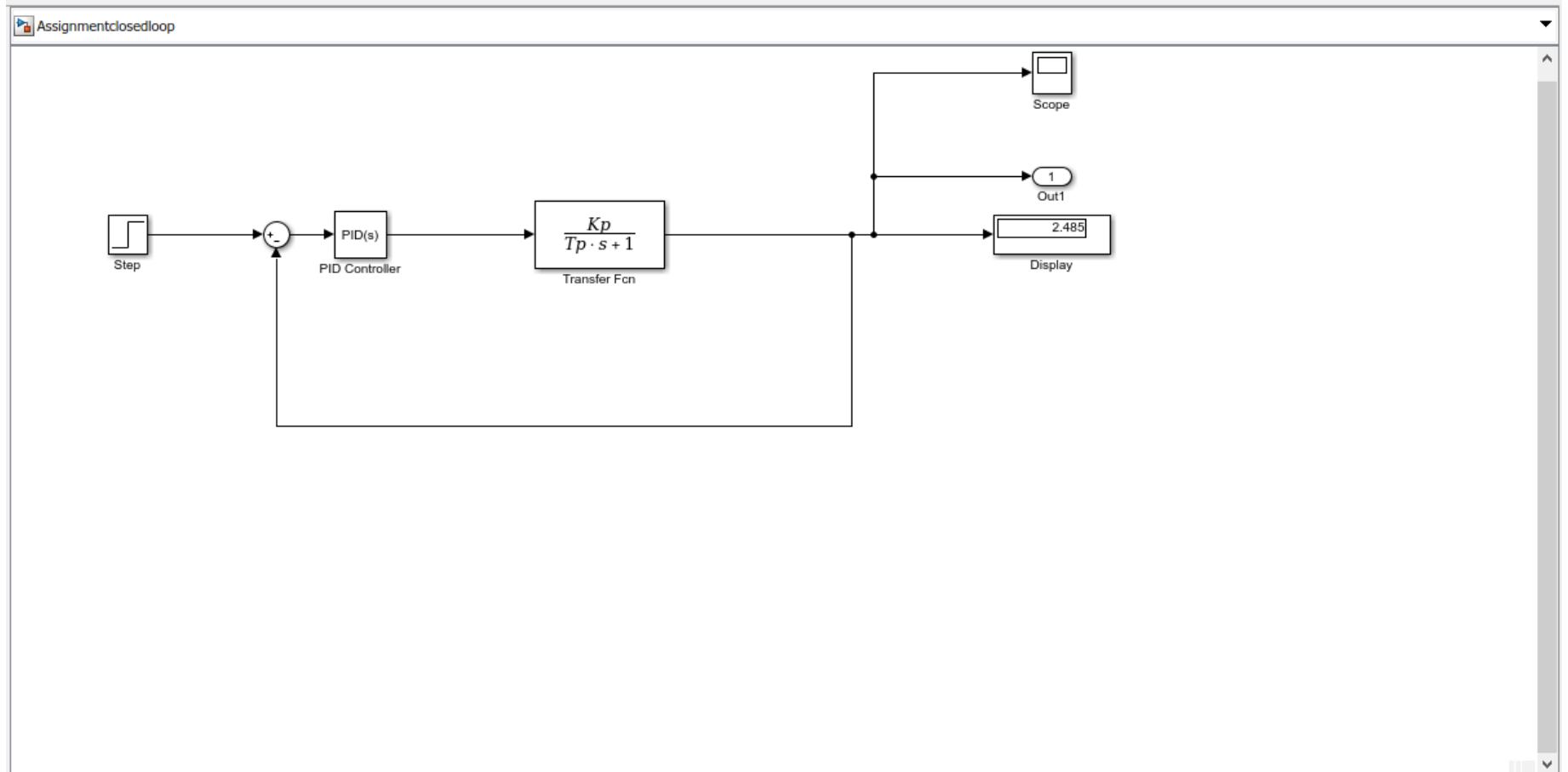


Figure 1. 5. Closed loop dynamic model

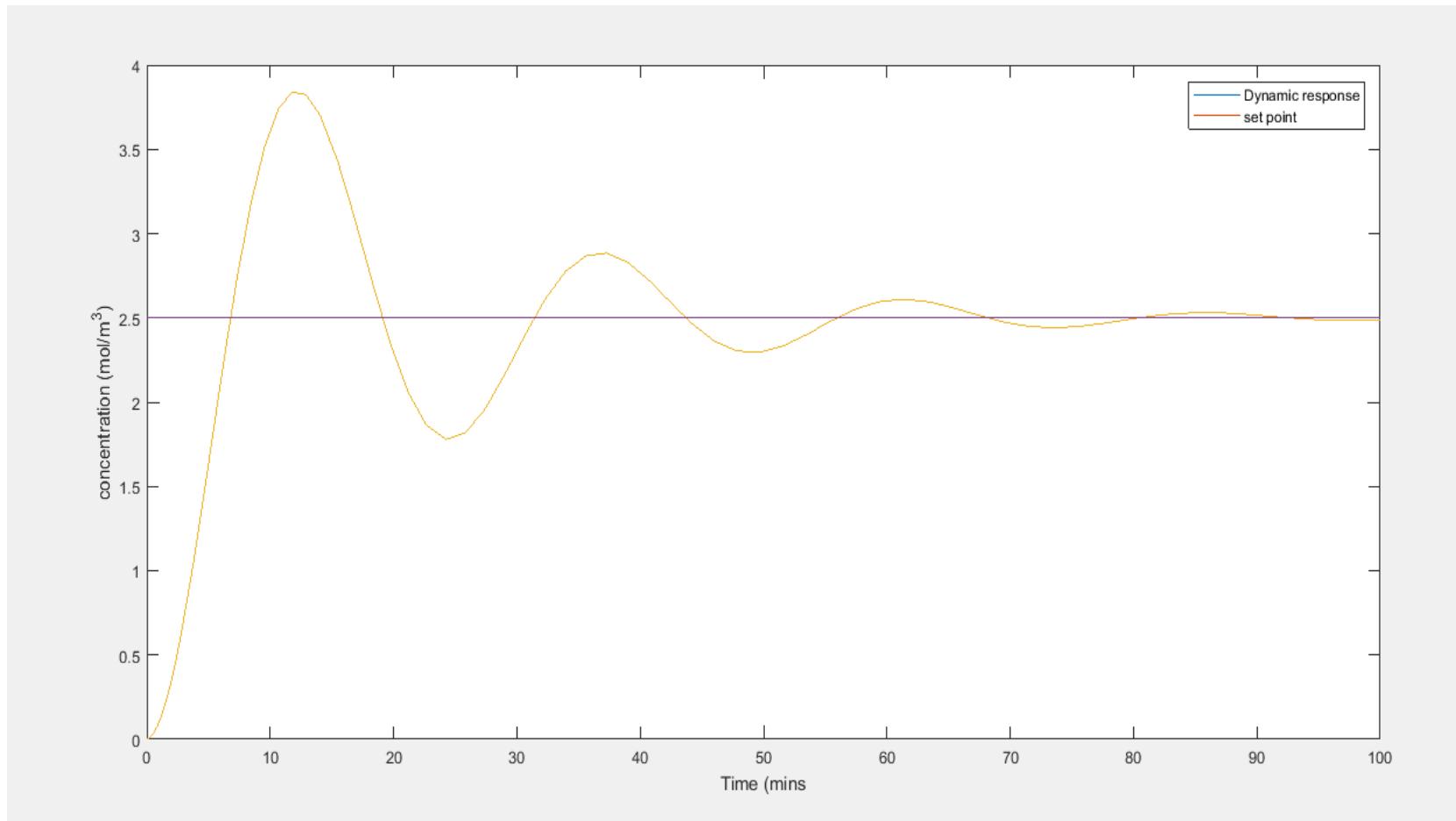


Figure 1. 6. Closed loop dynamic model plot