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1a. For bacteria growth, we use $\frac{dy}{dt} = ky$

Let y = quantity of bacteria

t = time (hrs).

$$\frac{dy}{dy} = k dt$$

$$\int \frac{dy}{y} = \int k dt$$

$$\ln y = kt + C$$

$$y = e^{kt + C}$$

$$y = e^{kt} \cdot e^C$$

$$y = e^{kt} \cdot C$$

$$y = C e^{kt}$$

at initial time $t = 0, y = 20$

$$20 = C e^{k \cdot 0}$$

$$20 = C$$

$$\text{at } t = 5, y = 2(20)$$

$$t = 5, y = 40$$

$$40 = C e^{k \cdot 5}$$

$$40 = 20 \cdot e^{5k}$$

$$e^{5k} = 2$$

$$5k = \ln 2$$

$$5k = 0.6931$$

$$k = 0.1386$$

$$\therefore y = 20 e^{0.1386t} \quad (\text{The required model})$$

1b At $t = 1\frac{1}{2}$ day

$$t = 24 + 12 \quad (1 \text{ day} = 24 \text{ hrs}, \frac{1}{2} \text{ day} = 12 \text{ hrs})$$

$$t = 36 \text{ hrs}$$

$$y = 20 e^{36 \cdot 0.1386}$$

$$y = 20 \times 146.8777$$

$$y = 2937.55$$

d. At $y=10$, and $t=0$

$$10 = Ce^{k \cdot 0}$$

$$C = 10$$

at $t=5$, $y=20$

$$20 = 10e^{5k}$$

$$e^{5k} = 2$$

$$5k = \ln 2$$

$$k = 0.1386$$

for initial value, 10 we have $y = 10e^{0.1386t}$

for initial value, 30, we have $y = 30e^{0.1386t}$

for initial value, 50 we have $y = 50e^{0.1386t}$

c. The initial amount of bacteria affected the exponential growth of bacteria. the highest initial amount had the highest final amount.