

Agoyi Isaac Oluwole  
 15/ENG02/002  
 Computer Engineering  
 ENG 382 Assignment 3

$$T_1 + T_2 - 2T_3 + T_4 + 3T_5 - T_6 = 4$$

$$2T_1 - T_2 + T_3 + 2T_4 + T_5 - 3T_6 = 20$$

$$T_1 + 3T_2 - 3T_3 - T_4 + 2T_5 + T_6 = -15$$

$$5T_1 + 2T_2 - T_3 - T_4 + 2T_5 + T_6 = -3$$

$$-3T_1 - T_2 + 2T_3 + 3T_4 + T_5 + 3T_6 = 16$$

$$4T_1 + 3T_2 + T_3 - 6T_4 - 3T_5 - 2T_6 = -27$$

6x6 matrix transformation

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 2 & -1 & 1 & 2 & 1 & -3 \\ 1 & 3 & -3 & -1 & 2 & 1 \\ 5 & 2 & -1 & -1 & 2 & 1 \\ -3 & -1 & 2 & 3 & 1 & 3 \\ 4 & 3 & 1 & -6 & -3 & -2 \end{bmatrix} \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 20 \\ -15 \\ -3 \\ 16 \\ -27 \end{bmatrix}$$

\* Using (2) to multiply row 1 and subtract row 2

$$\begin{aligned} & 2(2)1; -1-(2)(1); 1-(2)(-2); 2(2)(1); 1-(2)(3); \\ & -3-(2)(-1); 20-(2 \times 4) \\ & = 0; -3; 5; 0; -5; 1; 12 \end{aligned}$$



\* Using ① to multiply row 1 and subtract from Row 3  
 $1 - (1)(1); 3 - (1)(1); -3(1)(-2); -1 - (1)(1); 2 - (1)(3);$   
 $1 - (1)(-1); -15 - (1)(4)$   
 $= 0; 2; -1; 2; -1; 2; -19$

\* Multiplying 5 to row 1 and subtract from row 4  
 $5(-5)(1); 2 - (5)(1); -1(-5)(-2); -1 - (5)(1); 2 - (5)(3);$   
 $1 - (5)(-1); -3 - (5)(4)$   
 $= 0; -3; 9; -6; -13; 6; -23$

\* Multiply (-3) to row 1 and subtract from row 5  
 $-3 - (-3)(1); -1 - (-3)(1); 2 - (-3)(-2); 3(-3)(1); 1 - (-3)(3);$   
 $3 - (-3)(-1); 16 - (-3)(4)$   
 $= 0; 2; -4; 6; 10; 0; 28$

\* Multiply 4 by row 1 and subtract from row 6  
 $4(-4)(1); 3(4)(1); 1 - (4)(-2); -6 - (4)(1); -3(-4)(3);$   
 $-2(4)(-1); -27 - 4(4)$   
 $= 0; -1; 9; -10; -15; 2; -43$

The matrix becomes.

$$\begin{pmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 2 & -1 & -2 & -1 & 2 \\ 0 & -3 & 9 & -6 & -13 & 6 \\ 0 & 2 & -4 & 6 & 10 & 0 \\ 0 & -1 & 9 & -10 & -15 & 2 \end{pmatrix} \cdot \begin{pmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{pmatrix} = \begin{pmatrix} 4 \\ 12 \\ -19 \\ -23 \\ 28 \\ -43 \end{pmatrix}$$



\*Using a factor of  $(-\frac{2}{3})$  to multiply row 2 and subtract from row 3

$$2 - (-\frac{2}{3})(3); -1 - (-\frac{2}{3})(5); -2 - (-\frac{2}{3})(0); -1 - (-\frac{2}{3})(-5);$$

$$2 - (-\frac{2}{3})(-1); -19 - (-\frac{2}{3})(12)$$

$$= 0; 2.3333; -2; -4.3333; 1.3333; -11$$

\*Using a factor of  $(1)$  to multiply row 2 and subtr. from row 4

$$-3 - (1)(-3); 9 - (1)(5); -6 - (1)(0); -13 - (1)(-5); 6 - (1)(-1);$$

$$23 - (1)(12)$$

$$= 0; 4; -6; -8; 7; -35$$

Using a factor of  $(-\frac{2}{3})$  to mult. row 2 and subtr. from row 5

$$2 - (-\frac{2}{3})(3); -4 - (-\frac{2}{3})(5); 6 - (-\frac{2}{3})(0); 10 - (-\frac{2}{3})(-5); 0 - (-\frac{2}{3})(-1);$$

$$-28 - (-\frac{2}{3})(12)$$

$$= 0; -0.6666; 6; 6.6666; -0.6666$$

Using a factor of  $(\frac{1}{3})$  to multiply row 2 and subtr. row 6

$$-1 - (\frac{1}{3})(-3); 9 - (\frac{1}{3})(5); -10 - (\frac{1}{3})(0); -15 - (\frac{1}{3})(-5); 2 - (\frac{1}{3})(-1);$$

$$-43 - (\frac{1}{3})(1)$$

$$= 0; 7.3333; -10; -15.3333; 2.3333; -47$$

The new matrix is:

1	1	-2	1	3	-1	$T_1$	4
0	-3	5	0	-5	-1	$T_2$	12
0	0	2.3333	-2	-4.3333	1.3333	$T_3$	-11
0	0	4	-6	-8	7	$T_4$	-35
0	0	-0.6666	6	6.6666	-0.6666	$T_5$	36
0	0	7.3333	-10	-13.3333	2.3333	$T_6$	-47



Using a factor of 0.2856 to multiply row 3 and subtract row 5.

$$-0.6666(-0.2856)(2.3333); 6 - (-0.2856)(-2); 6.6666(-0.2856)(-1.3333);$$

$$6.6666(0.2856)(-4.3333); -0.6666(0.2856)(1.3333); 36 - (-0.2856)(-11)$$

$$= 0; 5.4285; 5.4285; -0.2857; 32.8571$$

Using a factor of  $(\frac{7.3333}{2.3333})$  to multiply row 1 and subtract row 6

$$7.3333 - (3.1428)(2.3333); -10 - (3.1428)(-2); -13.3333(3.1428)(-4.3333);$$

$$2.3333 - (3.1428)(1.3333); -47 - (3.1428)(-11)$$

$$= 0; -3.71429; 0.2857; -1.88714; -12.4286$$

The new matrix becomes

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.3333 & -2 & -4.3333 & 1.3333 \\ 0 & 0 & 0 & -2.571 & -0.5714 & 4.7142 \\ 0 & 0 & 0 & 5.4285 & 5.4285 & -0.2857 \\ 0 & 0 & 0 & -3.7142 & 0.2857 & -1.8571 \end{bmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{matrix} 4 \\ 12 \\ -11 \\ -16.1429 \\ 32.8571 \\ -12.4286 \end{matrix}$$

Using a factor  $(\frac{5.4285}{-2.571})$  to multiply row 4 and subtract from row 5

$$5.4285 - (-2.1114)(-2.571); 5.4285 - (-2.1114)(-0.5714);$$

$$-0.2857 - (-2.1114)(4.7142); 32.8571 - (-2.1114)(-16.1429)$$

$$= 0; 4.2222; 9.6666; -1.2222$$



Using a factor of  $(-3.7142/-2.571)$  to multiply row 5 and divide row 6.

$$-3.9142 - (1.4446)(-2.571), 0.2857 - (1.4446)(-0.5714),$$

$$-1.8571(-1.4) - 1.8571 - (1.4446)(4.7142),$$

$$-12.4286 - (1.4446)(-16.1429)$$

$$= 0; 1.1111; -8.6666; 10.8888$$

The new matrix becomes

$$\left( \begin{array}{cccccc|c|c} 1 & 1 & -2 & 1 & 3 & -1 & 7 & 4 \\ 0 & -3 & 5 & 0 & -5 & -1 & T_2 & 12 \\ 0 & 0 & 2.3333 & -2 & -4.3333 & 1.3333 & T_3 & -11 \\ 0 & 0 & 0 & -2.5714 & 0.5714 & 4.7142 & T_4 & -16.1429 \\ 0 & 0 & 0 & 0 & 4.2222 & 9.6666 & T_5 & -1.2222 \\ 0 & 0 & 0 & 0 & 1.1111 & -8.6666 & T_6 & 10.8888 \end{array} \right)$$

Using a factor of  $(1.1111/4.2222)$  to multiply row 5 and subtract row 6.

$$1.1111 - (0.2031)(4.2222), -8.6666 - (0.2651)(9.6666),$$

$$10.8888 - (0.2631)(-1.2222)$$

$$= 0; -11.2105; 11.2105$$



The matrix becomes:

$$\begin{pmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.3333 & -2 & -4.3333 & 1.3333 \\ 0 & 0 & 0 & -2.5714 & -6.5714 & 4.7142 \\ 0 & 0 & 0 & 0 & 4.2222 & 9.6666 \\ 0 & 0 & 0 & 0 & 0 & -11.2105 \end{pmatrix} \begin{matrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{matrix} = \begin{pmatrix} 4 \\ 12 \\ -11 \\ -16.1429 \\ -1.2222 \\ 11.2105 \end{pmatrix}$$

Using Back substitution

$$-11.2105 T_6 = 11.2105$$

$$T_6 = \frac{11.2105}{-11.2105} = -1$$

$$4.2222 T_5 + 9.6666 T_6 = -1.2222$$

$$T_5 = \frac{-1.2222 - 9.6666(-1)}{4.2222} = 2$$

$$-2.5714 T_4 - 6.5714 T_5 + 4.7142 T_6 = -16.1429$$

$$T_4 = \frac{-16.1429 - 4.7142(-1) + 6.5714(2)}{-2.5714} = 4$$

$$2.3333 T_3 - 2 T_4 - 4.3333 T_5 + 1.3333 T_6 = -11$$

$$T_3 = \frac{-11 - 1.3333(-1) + 4.3333(2) + 2(4)}{-2.3333} = 3$$

$$\Rightarrow -8 T_2 + 5 T_3 + 6 T_4 - 5 T_5 - T_6 = 12$$

$$T_2 = \frac{12 + (-1) + 5(2) - 5(3) - (-4)}{-8} = -2$$

$$T_1 + T_2 - 2 T_3 + T_4 + 3 T_5 - T_6 = 4$$



$$T_1 = 4 + (-1) - 3(2) - 4 + 2(3) - (-2) = 1$$

Therefore:  $T_1 = 1$

$$T_2 = -2$$

$$T_3 = 3$$

$$T_4 = 4$$

$$T_5 = 2$$

$$T_6 = -1$$