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16/ENG04/023

Elect / Elect

ENG 232

Assignment

1a) For bacteria growth we use

$$dy/dt = ky$$

$$dy/y = k dt$$

$$\int dy/y = \int k dt$$

$$\ln y = kt + C$$

$$y = e^{kt+C}$$

$$y = e^{kt} \cdot e^C$$

$$y = e^{kt} \cdot C$$

$$y = Ce^{kt}$$

At initial time $t = 0$ hrs, $y = 20$

$$20 = Ce^{k \cdot 0}$$

$$C = 20$$

At $t = 5$, $y = 2y_0$

$t = 5$, $y = 40$

$$40 = Ce^{k \cdot 5}$$

$$40 = 20 \cdot e^{5k}$$

$$e^{5k} = 2$$

$$5k = \ln 2$$

$$5k = 0.6931$$

$$k = 0.1386$$

$y = 20e^{0.1386t}$ is the required model

1b) At $t = 1\frac{1}{2}$ days

$$t = (24 + 12) \text{ hours}$$

$$t = 36 \text{ hours}$$

$$y = 20 e^{36 \times 0.1386}$$

$$y = 20 \times 146.9777$$

$$y = 2937.55$$

1d) At $y = 10$ and $t = 0$

$$10 = C e^{k \cdot 0}$$

$$C = 10$$

At $t = 5$, $y = 20$

$$20 = 10 e^{5k}$$

$$e^{5k} = 2$$

$$5k = \ln 2$$

$$k = 0.1386$$

For initial value = 10, we have $y = 10 e^{0.1386t}$

$$// \quad = 30, \quad // \quad y = 30 e^{0.1386t}$$

$$// \quad = 50 \quad // \quad y = 50 e^{0.1386t}$$

1e) The initial amount of bacteria affected the experimental growth of the bacteria the highest initial amount had the highest final amount



