

# Assignment ENGA381

$$\begin{aligned} i) \quad T_1 + T_2 - 2T_3 + T_4 + 3T_5 - T_6 &= 4 \\ 2T_1 - T_2 + T_3 + 2T_4 + T_5 - 3T_6 &= 20 \\ T_1 + 3T_2 - 3T_3 - T_4 + 2T_5 + T_6 &= -15 \\ 3T_1 + 2T_2 - T_3 - T_4 + 2T_5 + T_6 &= -3 \\ 3T_1 - T_2 + 2T_3 + 3T_4 + T_5 + T_6 &= 16 \\ 4T_1 + 3T_2 + T_3 - 6T_4 - 3T_5 - 2T_6 &= -27 \end{aligned}$$

The augmented matrix  $\Rightarrow$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 2 & -1 & 1 & 2 & 1 & -3 \\ 1 & 3 & -3 & -1 & 2 & 1 \\ 3 & 2 & -1 & -1 & 2 & 1 \\ -3 & -1 & 2 & 3 & 3 & 1 \\ 4 & 3 & 1 & -6 & -3 & -2 \end{bmatrix} \cdot \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 20 \\ -15 \\ -3 \\ 16 \\ -27 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 2 - (2/1) \cdot 1 & -1 - (1/1) \cdot 1 & 1 - (-2/1) \cdot 2 & 2 - (1/1) \cdot 1 & 1 - (3/1) \cdot 3 & -3 - (-1/1) \cdot 1 \\ 1 - (1/1) \cdot 1 & 3 - (3/1) \cdot 1 & -3 - (-3/1) \cdot 2 & -1 - (-1/1) \cdot 1 & 2 - (2/1) \cdot 3 & 1 - (1/1) \cdot 1 \\ 3 - (3/1) \cdot 1 & 2 - (2/1) \cdot 1 & -1 - (-1/1) \cdot 2 & -1 - (1/1) \cdot 1 & 2 - (3/1) \cdot 3 & 1 - (1/1) \cdot 1 \\ -3 - (-3/1) \cdot 1 & -1 - (-1/1) \cdot 1 & 2 - (-2/1) \cdot 2 & 3 - (-3/1) \cdot 1 & 3 - (-1/1) \cdot 3 & 1 - (-1/1) \cdot 1 \\ 4 - (4/1) \cdot 1 & 3 - (3/1) \cdot 1 & 1 - (-2/1) \cdot 2 & -6 - (-6/1) \cdot 1 & -3 - (-3/1) \cdot 3 & -2 - (-2/1) \cdot 1 \end{bmatrix} \cdot \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 20 - (2/1) \cdot 4 \\ -15 - (1/1) \cdot 4 \\ -3 - (3/1) \cdot 4 \\ 16 - (-3/1) \cdot 4 \\ -27 - (4/1) \cdot 4 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 2 & -1 & -2 & -1 & 2 \\ 0 & -3 & 9 & -6 & -13 & 6 \\ 0 & 2 & -4 & 6 & 10 & 0 \\ 0 & -1 & 9 & -10 & -15 & 2 \end{bmatrix} \cdot \begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -19 \\ -23 \\ 28 \\ 43 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 2 - (-\frac{2}{3}) \cdot 3 & -1 - (-\frac{2}{3}) \cdot 5 & 1 - (-\frac{2}{3}) \cdot 0 & 3 - (-\frac{2}{3}) \cdot 3 & 2 - (-\frac{2}{3}) \cdot 1 \\ 0 & -3 - (-\frac{2}{3}) \cdot 3 & 5 - (-\frac{2}{3}) \cdot 5 & 0 - (-\frac{2}{3}) \cdot 0 & -5 - (-\frac{2}{3}) \cdot 3 & -1 - (-\frac{2}{3}) \cdot 1 \\ 0 & 2 - (-\frac{2}{3}) \cdot 3 & -4 - (-\frac{2}{3}) \cdot 5 & 6 - (-\frac{2}{3}) \cdot 0 & 10 - (-\frac{2}{3}) \cdot 3 & 0 - (-\frac{2}{3}) \cdot 1 \\ 0 & 1 - (-\frac{2}{3}) \cdot 3 & 9 - (-\frac{2}{3}) \cdot 5 & -10 - (-\frac{2}{3}) \cdot 0 & 15 - (-\frac{2}{3}) \cdot 3 & 2 - (-\frac{2}{3}) \cdot 1 \end{bmatrix} \begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \\ r_5 \\ r_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -14 - (-\frac{2}{3}) \cdot 12 \\ -33 - (-\frac{2}{3}) \cdot 12 \\ 28 - (-\frac{2}{3}) \cdot 12 \\ -43 - (-\frac{2}{3}) \cdot 12 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.4 & -2 & -4.4 & 1.4 \\ 0 & 0 & 4 & -6 & -8 & 7 \\ 0 & 0 & -0.7 & 6 & 6.7 & -0.7 \\ 0 & 0 & 7.4 & -10 & -13.4 & 2.4 \end{bmatrix} \begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \\ r_5 \\ r_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -35 \\ 36 \\ -47 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.4 & -2 & -4.4 & 1.4 \\ 0 & 0 & 4 - (\frac{4}{2.4}) \cdot 2.4 & -6 - (\frac{4}{2.4}) \cdot 2.4 & -8 - (\frac{4}{2.4}) \cdot 4.4 & 7 - (\frac{4}{2.4}) \cdot 1.4 \\ 0 & 0 & -0.7 - (\frac{0.7}{2.4}) \cdot 2.4 & 6 - (\frac{0.7}{2.4}) \cdot 2.4 & 6.7 - (\frac{0.7}{2.4}) \cdot 4.4 & -0.7 - (\frac{0.7}{2.4}) \cdot 1.4 \\ 0 & 0 & 7.4 - (\frac{7.4}{2.4}) \cdot 2.4 & -10 - (\frac{7.4}{2.4}) \cdot 2.4 & -13.4 - (\frac{7.4}{2.4}) \cdot 4.4 & 2.4 - (\frac{7.4}{2.4}) \cdot 1.4 \end{bmatrix} \begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \\ r_5 \\ r_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -35 - (\frac{4}{2.4}) \cdot 11 \\ 36 - (\frac{0.7}{2.4}) \cdot 11 \\ -47 - (\frac{7.4}{2.4}) \cdot 11 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.4 & -2 & -4.4 & 1.4 \\ 0 & 0 & 0 & -2.7 & -0.7 & 4.7 \\ 0 & 0 & 0 & 5.42 & 5.42 & -0.74 \\ 0 & 0 & 0 & -3.84 & 0.17 & -1.91 \end{bmatrix} \begin{bmatrix} r_1 \\ r_2 \\ r_3 \\ r_4 \\ r_5 \\ r_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -16.7 \\ -0.74 \\ 10.7 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.4 & -2 & -4.4 & 1.4 \\ 0 & 0 & 0 & -2.2 & -0.7 & 4.7 \\ 0 & 0 & 0 & 5.42\left(\frac{5.42}{-2.2}\right) - 2.2 & 5.24\left(\frac{5.42}{-2.2}\right) - 0.7 & -0.74 - \left(\frac{5.22}{-2.2}\right) 4.7 \\ 0 & 0 & 0 & -3.80\left(\frac{-3.84}{-2.2}\right) 2.2 & 0.17\left(\frac{3.84}{-2.2}\right) - 0.7 & -1.91\left(\frac{3.84}{-2.2}\right) 4.7 \end{bmatrix} \begin{bmatrix} \lambda_1 \\ \lambda_2 \\ \lambda_3 \\ \lambda_4 \\ \lambda_5 \\ \lambda_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -16.7 \\ 32.27 - \left(\frac{5.42}{-2.2}\right) \cdot -16.7 \\ -13.08 - \left(\frac{-3.84}{-2.2}\right) \cdot -10.7 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & 3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.4 & -2 & -4.4 & 1.4 \\ 0 & 0 & 0 & -2.2 & -0.7 & 4.7 \\ 0 & 0 & 0 & 0 & 4.01 & 9.2 \\ 0 & 0 & 0 & 0 & 1.16 & -8.59 \end{bmatrix} \begin{bmatrix} \lambda_1 \\ \lambda_2 \\ \lambda_3 \\ \lambda_4 \\ \lambda_5 \\ \lambda_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -16.7 \\ -0.74 \\ 10.7 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & 3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.4 & -2 & -4.4 & 1.4 \\ 0 & 0 & 0 & -2.2 & -0.7 & 4.7 \\ 0 & 0 & 0 & 0 & 4.01 & 9.2 \\ 0 & 0 & 0 & 0 & 1.16\left(\frac{1.16}{4.01}\right) \cdot 4.01 & -8.59 - \left(\frac{-8.59}{4.01}\right) 9.2 \end{bmatrix} \begin{bmatrix} \lambda_1 \\ \lambda_2 \\ \lambda_3 \\ \lambda_4 \\ \lambda_5 \\ \lambda_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -16.7 \\ -0.74 \\ 10.7 - \left(\frac{1.16}{4.01}\right) - 0.74 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 1 & -2 & 1 & 3 & -1 \\ 0 & -3 & 5 & 0 & -5 & -1 \\ 0 & 0 & 2.4 & -2 & -4.4 & 1.4 \\ 0 & 0 & 0 & -2.2 & -0.7 & 4.7 \\ 0 & 0 & 0 & 0 & 4.01 & 9.2 \\ 0 & 0 & 0 & 0 & 0 & -11.3 \end{bmatrix} \begin{bmatrix} \lambda_1 \\ \lambda_2 \\ \lambda_3 \\ \lambda_4 \\ \lambda_5 \\ \lambda_6 \end{bmatrix} = \begin{bmatrix} 4 \\ 12 \\ -11 \\ -16.7 \\ -0.74 \\ 10.92 \end{bmatrix}$$

For  $\lambda_6$  make above

$$-11.3\lambda_6 = 10.92$$

$$\lambda_6 = \frac{0.92}{-11.3} = -0.966$$

$$4.01\lambda_5 + 9.2\lambda_6 = -0.74$$

$$\lambda_5 = \frac{-0.74 - 9.2(-0.966)}{4.01} = 2.031$$

$$-2.274 - 0.775 + 4.776 = -16.7$$

$$T_4 = \frac{-16.7 - 4.7(0.966) + 0.7(2.031)}{-2.77} = \frac{3.977}{-2.77} = -1.436$$

$$2.473 - 274 - 4.475 + 1.476 = -11$$

$$T_3 = \frac{-11 - 1.4(0.966) + 4.4(2.031) + 2(3.977)}{2.4} = 3.017$$

$$-372 + 873 + 074 - 575 - 176 = 12$$

$$T_2 = \frac{12 + 6(0.966) + 5(2.031) - 5(3.017)}{-3} = -2.034$$

$$T_1 + T_2 - 2T_3 + T_4 + 3T_5 - T_6 = 4$$

$$T_1 = 4 - 2(-2.034) - 3(2.031) - 3.977 + 2(3.017) + 2.034 = 1.032$$

$$T_1 = 1.032^\circ\text{C}$$

$$T_2 = -2.034^\circ\text{C}$$

$$T_3 = 3.017^\circ\text{C}$$

$$T_4 = 3.972^\circ\text{C}$$

$$T_5 = 2.031^\circ\text{C}$$

$$T_6 = -0.966^\circ\text{C}$$