

① $f(x) = e^{-0.5x} (4-x) - 2 \quad \text{--- (1)}$

Applying newton Raphson method:

Applying product rule to diff eqn (1)
 $f'(x) = \left[u \frac{dv}{dx} + v \frac{du}{dx} \right]$

$u = e^{-0.5x}, \quad v = (4-x)$
 $u' = -0.5 e^{-0.5x}$
 $v' = -1$

$f'(x) = -1 e^{-0.5x} + (4-x) - 0.5 e^{-0.5x} = 0$

$f(x) = -e^{-0.5x} - 0.5 e^{-0.5x} (4-x) \quad \text{--- (2)}$
 iter = 0, $x_i = 0.5$

Recall:

$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)} \quad \text{--- (*)}$

Initial value $x_0 = 0.5 \Rightarrow \text{iter} = 0$

$x_{i+1} = 0.5 - \frac{e^{-0.5x_i} (4-x_i) - 2}{-e^{-0.5x_i} - 0.5 e^{-0.5x_i} (4-x_i)}$

$x_{i+1} = 0.5 - \frac{e^{-0.5(0.5)} (4-0.5) - 2}{-e^{-0.5(0.5)} - 0.5 (e^{-0.5(0.5)} (4-0.5))}$

$x_{i+1} = 0.5 - \frac{0.7258027407}{-2.141702153}$

$x_{i+1} = 0.8388906061$

$x_{i+1} = 0.8388906061$

$$\% \text{ error} = \left| \frac{0.8388906061 - 0.5}{0.8388906061} \right| \times 100 = 0.40397473$$

$$\text{for iter} = 2 = 40.397473\%$$

$$x_i = 0.8388906061$$

$$x_{i+1} = 0.8388906061 - \frac{e^{-0.5(0.8388906061)} (4 - 0.8388906061) - 2}{-e^{-0.5(0.8388906061)} - 0.5 e^{-0.5(0.8388906061)}} = 0.884956000$$

$$x_{i+1} = 0.884956000$$

$$\% \text{ error} = \left| \frac{0.884956000 - 0.8388906061}{0.884956000} \right| \times 100 = 5.205388064\%$$

$$\% \text{ error} = 5.205388064\%$$

$$\text{for iter} = 3$$

$$x_i = 0.884956000$$

$$x_{i+1} = 0.884956000 - \frac{e^{-0.5(0.884956000)} (4 - 0.884956000) - 2}{-e^{-0.5(0.884956000)} - 0.5 e^{-0.5(0.884956000)}} = 0.885708605$$

$$x_{i+1} = 0.885708605$$

$$\% \text{ error} = \left| \frac{0.885708605 - 0.884956000}{0.885708605} \right| \times 100 = 0.084971984\%$$

$$\% \text{ error} = 0.084971984\%$$

for iter = 4

$$x_i = 0.885708605$$

$$x_{i+1} = 0.885708605 - \frac{e^{-0.5(0.885708605)} (4 - 0.885708605) - 2}{-e^{-0.5(0.885708605)} - 0.5 e^{-0.5(0.885708605)} (4 - 0.885708605)}$$

$$x_{i+1} = 0.885708802$$

$$\% \text{ error} = \left| \frac{0.885708802 - 0.885708605}{0.885708802} \right| \times 100\%$$

$$\% \text{ error} = 2.224267317 \times 10^{-7}\%$$

for iter = 5

$$x_i = 0.885708802$$

$$x_{i+1} = 0.885708802 - \frac{e^{-0.5(0.885708802)} (4 - 0.885708802) - 2}{-e^{-0.5(0.885708802)} - 0.5 e^{-0.5(0.885708802)} (4 - 0.885708802)}$$

$$x_{i+1} = 0.885708802$$

$$\% \text{ error} = \left| \frac{0.885708802 - 0.885708802}{0.885708802} \right| \times 100\% = 0$$

Table of Values

i	x_i	% error
0	0.5	
1	0.8388906061	40.993473
2	0.884956000	5.205388064
3	0.885708605	0.084971964
4	0.885708802	$2.224267319 \times 10^{-7} \%$
5	0.885708802	0

② MATLAB Code

Command window

clear

clc

close all

iter = 0;

V = 18;

for i = (1:inf)

iter(i+1) = i;

$f_{t1} = ((0.3 * V(i)^{12}) / (500 + (\log(V(i))^{13}))) - 0.02 * V(i)^{12}$

$f_{t2} = ((3 * (V(i))) / (5 * (\log(V(i))^{13} + 500))) - (9 * V(i) * \log(V(i))^{12}) / (V(i) * \log(V(i))^{13} + 500)^{12} - 1/50$

$V(i+1) = V(i) - (f_{t1} / f_{t2})$;

$ea = \text{abs}(V(i+1) - V(i)) * 100$;

if $ea(i+1) > 1e-15$

break

end

end

table = [iter' V' ea'];