

Let  $y$  represent fresh air

rate of accumulator = rate of in flow - rate of outflow

$$\frac{dy}{dt} = 600 - 0.03y$$

rate of income =  $600 \text{ ft}^3/\text{min}$

rate of outflow =  $\frac{600}{20000} \times y = 0.03y$

$$\frac{dy}{dt} = -0.03(y - 20000)$$

$$\frac{dy}{(y - 20000)} = -0.03 dt$$

$$\ln(y - 20000) = -0.03t + C$$

$$y - 20000 = e^{-0.03t + C}$$

$$y - 20000 = y_0 e^{-0.03t}$$

$$y = 20000 + y_0 e^{-0.03t}$$

If the room contained no fresh air

$$y = 0, t = 0$$

$$0 = 20000 + y_0$$

$$y_0 = -20000$$

$$y = 20000 - 20000 e^{-0.03t}$$

$$y = 20000 (1 - e^{-0.03t})$$

This is the model for the amount of oil at any time  $t$ .

b. room contains 20000 ft<sup>3</sup> of oil

$$90\frac{1}{2} \text{ of } 20000$$

$$= 18500 \text{ ft}^3/\text{min}$$

from the model:

$$y = 20000(1 - e^{-0.03t})$$

$$18500 = 20000(1 - e^{-0.03t})$$

$$e^{-0.03t} = -\left(\frac{18500}{20000} - 1\right)$$

$$e^{-0.03t} = +0.1$$

$$-0.03t = \ln 0.1$$

$$-0.03t = -2.303$$

$$t = \frac{2.303}{0.03}$$

$$0.03$$

$$t = 76.77 \text{ min}$$

c. Shows to what extent because

$$60 \text{ minutes} = 1 \text{ hour}$$

$$n = 6$$

$$6 \times 60 = n \times 1$$

$$n = 360 \text{ minute}$$

d. The steady state value of the fresh amount of air in the room gives 20,000 ft<sup>3</sup> of air.

c The graph gave a straight line which entails that the steady rate value of the amount of fresh air in the room does not change even with the expense of increase in time