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It is discovered that  $600 \text{ ft}^3/\text{min}$  of fresh air flows into a room containing  $20000 \text{ ft}^3$  of air. The mixture, which is made practically uniform by circulating fans, is exhausted at a rate of 600 cubic feet per minute [CFM]. If the room contains no fresh air initially.

Solve

a.) Develop a model for the amount of fresh air at any time.

\* Let  $y$  represent fresh air.

\* Rate of accumulation  $\equiv$  rate of inflow - rate of outflow.

$$\frac{dy}{dt} = 600 - 0.03y$$

rate of inflow =  $600 \text{ ft}^3/\text{min}$

$$\text{rate of outflow} = \frac{600}{20000} \times y = 0.03y$$

$$\frac{dy}{dt} = -0.03(y - 20000)$$

$$\frac{dy}{(y - 20000)} = -0.03 dt$$

$$\ln[y - 20000] = -0.03t + C$$

$$y - 20000 = e^{-0.03t + C}$$

$$y - 20000 = y_0 e^{-0.03t}$$

$$y = 20000 + y_0 e^{-0.03t}$$

If the room contained no fresh air

$$y = 0, t = 0$$

$$0 = 20000 + y_0$$

$$y_0 = -20000$$

$$y = 20000 - 20000 e^{-0.03t}$$

$$y = 20000 [1 - e^{-0.03t}]$$

This model is for the amount of air at any time,  $t$

b) Calculate the time which 90% of the air in the room will have become fresh.

Solu

Room contains  $20000 \text{ ft}^3$  of air

$$90\% \text{ of } 20000 = 18000 \text{ ft}^3/\text{min}$$

$$\rightarrow \text{from the model, } y = 20000 [1 - e^{-0.03t}]$$

$$18000 = 20000 [1 - e^{-0.03t}]$$

$$e^{-0.03t} = -\left[\frac{18000}{20000} - 1\right]$$

$$e^{-0.03t} = 0.1$$

$$\Rightarrow 0.03t = \ln [0.1]$$

$$\Rightarrow 0.03t = -2.303$$

$$t = \frac{2.303}{0.03} = 76.77 \text{ min}$$

d) From the dynamic response plotted, the steady state value of the amount of fresh air in the room is  $20000 \text{ ft}^3$  of air.

e) It was noticed that the value of amount of fresh air steadily increase until it get to  $20000 \text{ ft}^3$  of air. Therefore despite the increase in time, the amount of fresh air remained  $20000 \text{ ft}^3$  giving the steady-state value. In conclusion,  $20000 \text{ ft}^3$  of air is the maximum air for the room.