

①  $f(x) = \pi$

$$\lim_{x \rightarrow 3} f(x)$$

$$x \rightarrow 3$$

$$\lim_{x \rightarrow 3} f(x) = 0$$

The limit does not exist because  $\lim_{x \rightarrow 3} f(x) = 0$

②  $f(x) = 5x - 21$

$\delta = 0.1$ ; and using a step of 0.01

$$\therefore \delta = 0.1$$

$$\delta = 0.01$$

R.H.S

$(a+\delta)$	left-hand side	$f(x)$	$a-\delta$	$f(x)$
	5.9	8.5	6.1	9.5
	5.91	8.55	6.09	9.45
	5.92	8.6	6.08	9.4
	5.93	8.65	6.07	9.35
	5.94	8.7	6.06	9.3
	5.95	8.75	6.05	9.25
	5.96	8.8	6.04	9.2
	5.97	8.85	6.03	9.15
	5.98	8.9	6.02	9.1
	5.99	8.95	6.01	9.05
	6	9	6	9

③  $\lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|}$

sol

$$\lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|} = \lim_{x \rightarrow 3^+} \frac{\cancel{3} - \cancel{3} + \delta}{|\cancel{3} - \cancel{3} + \delta|} = \frac{-\delta}{|\delta|} = -1 //$$

④  $\lim_{x \rightarrow 3} \frac{x-3}{|x-3|}$

sol

To check if the above exist find  $\lim_{x \rightarrow 3} \frac{x-3}{|x-3|}$  taking limit of  $x \rightarrow 3^+$  and  $x \rightarrow 3^-$  respectively

$$\text{So } \lim_{x \rightarrow 3^+} \frac{x-3}{|x-3|} = \lim_{x \rightarrow 3^+} \frac{3.1-3}{|3.1-3|} = \lim_{x \rightarrow 3^+} \frac{0.1}{|0.1|} = 1 //$$

$$\lim_{x \rightarrow 3^-} \frac{x-3}{|x-3|} = \lim_{x \rightarrow 3^-} \frac{2.9-3}{|2.9-3|} = \frac{-0.1}{|-0.1|} = \frac{-0.1}{0.1} = -1 //$$

$$\text{Hence } \lim_{x \rightarrow 3} \frac{x-3}{|x-3|} = 0$$

The limit does not exist

⑤ interval  $[4, 8]$ ,  $f(x) = \sqrt{x-4}$

$x$	$f(x) = \sqrt{x-4}$
4	0
5	1
6	$\sqrt{2}$ or 1.41
7	$\sqrt{3}$ or 1.73
8	2

$f(x)$

Hence the equation  $f(x) = \sqrt{x-4}$  is a continuous equation.

