

## ENG 281 [Engineering Maths]

1.  $f(x) = \pi$

$$\lim_{x \rightarrow 3} \pi$$

$$\pi = 3.14 \text{ or } \frac{22}{7}$$

$$\therefore \lim_{x \rightarrow 3} \pi = \frac{22}{7} \text{ because } \pi \text{ is a constant.}$$

2.	$x^-$	$f(x^-)$	$x^+$	$f(x^+)$
	5.90	8.50	6.10	9.50
	5.91	8.55	6.09	9.45
	5.92	8.60	6.08	9.40
	5.93	8.65	6.07	9.35
	5.94	8.70	6.06	9.30
	5.95	8.75	6.05	9.25
	5.96	8.80	6.04	9.20
	5.97	8.85	6.03	9.15
	5.98	8.90	6.02	9.10
	5.99	8.95	6.01	9.05
	6.00	9.00	6.00	9.00

Since limits of  $x^+$  and  $x^-$  are real and are both approaching ~~zero~~ 9.0, the limit of  $f(x)$ ,  $\lim_{x \rightarrow 6} = 5x - 21$  which is equal to 9.

$$3. \lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|}$$

let  $\delta$  be a small increment in  $x$

$$\lim_{x \rightarrow 3^+} \frac{3-(3+\delta)}{|3-(3+\delta)|}$$

$$\lim_{x \rightarrow 3^+} \left[ \frac{3-3-\delta}{|3-3-\delta|} \right] = \lim_{x \rightarrow 3^+} \left[ \frac{-\delta}{|-\delta|} \right]$$

$$= -1$$

$$\therefore \lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|} = -1$$

$$4. \lim_{x \rightarrow 3} \left[ \frac{x-3}{|x-3|} \right]$$

$$\lim_{x \rightarrow 3} \left[ \frac{3-3}{|3-3|} \right] = \frac{0}{0} \text{ Indeterminate.}$$

$$\lim_{x \rightarrow 3^+} \left[ \frac{x-3}{|x-3|} \right] = \frac{3+\delta-3}{|3+\delta-3|} = \lim_{x \rightarrow 3^+} \frac{\delta}{|\delta|}$$

$$= 1$$

$$\cdot \text{ for } \lim_{x \rightarrow 3^-} \left[ \frac{x-3}{|x-3|} \right]$$

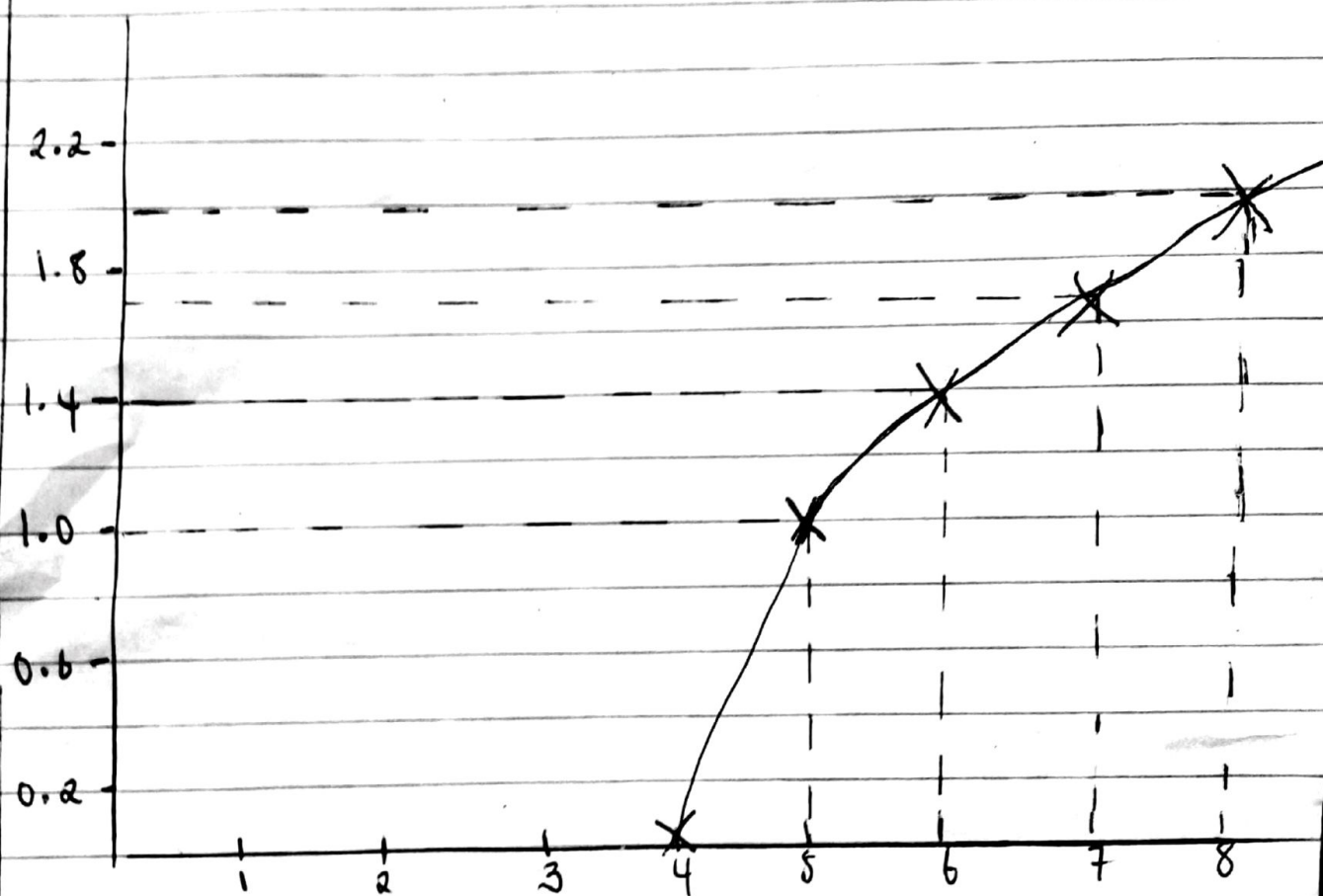
$$\lim_{x \rightarrow 3^-} \left[ \frac{3-\delta-3}{|3-\delta-3|} \right] = \lim_{x \rightarrow 3^-} \left[ \frac{-\delta}{|-\delta|} \right]$$

$$\lim_{x \rightarrow 3^-} \left[ \frac{-\delta}{\delta} \right] = -1$$

Since both limits are not equal, the  $\lim_{x \rightarrow 3}$  doesn't exist.

5.

$x$	$f(x)$
4	0.00
5	1.00
6	1.41
7	1.73
8	2.00



It is a continuous graph since it is not a straight-line graph.