

Given the function $f(x) = 5x - 21$. Find $\lim_{x \rightarrow 8} f(x)$

Answer

There isn't a means of substitution for $x = 8$ therefore it is undefined

Find the limit of the model equation given below

$$\lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|} = \frac{3-3+\delta x}{|3-3+\delta x|} = \frac{\delta x}{\delta x} = 1$$

The model of a system has been developed by an engineer to be as given
 $f(x) = 5x - 21$. Given $\delta = 0.1$, and using a step of 0.01 , demonstrate in tabular form that limit of the model as $x \rightarrow 6.9$

$f(x)$	$x - \delta$	x	$x + \delta$	$f(x)$
8.05	5.90	6	6.1	9.50
8.55	5.11	6.09	6.09	9.45
8.60	5.92	6.08	6.08	9.40
8.65	5.93	6.07	6.07	9.35
8.70	5.94	6.06	6.06	9.30
8.75	5.95	6.05	6.05	9.25
8.80	5.96	6.04	6.04	9.20
8.85	5.97	6.03	6.03	9.15
8.90	5.98	6.02	6.02	9.10
8.95	5.99	6.01	6.01	9.05
9	5.00	6.00	6.00	9.00

The limit is defined for $x = 6.9$ as the LHS & RHS are the same

$$\lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|} = \frac{3-3}{|3-3|} = \frac{0}{0} = \text{Undefined}$$

Evaluate the limit of the model given.

$$\lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|} = \frac{3+8-3}{|3+8-3|} = \frac{8}{8} = 1$$

$$\lim_{x \rightarrow 3^-} \frac{3-x}{|3-x|} = \frac{3-8-3}{|3-8-3|} = \frac{-8}{8} = -1$$

$$\lim_{x \rightarrow 3} \frac{3-x}{|3-x|} = \frac{3-3}{|3-3|} = \frac{0}{0} = \text{Undefined}$$

Show that the function given in equation $f(x) = \sqrt{x-4}$ is continuous on the interval $(4, 8)$

Sub 4 for $x = \sqrt{4-4} = \sqrt{0} = 0 \dots \dots \dots$ (1)
 Sub 8 for $x = \sqrt{8-4} = \sqrt{4} = 2 \dots \dots \dots$ (2)

x (component)	y (component)
4	0
5	1.4
6	1.41
7	1.73
8	2

From the graph figure 1.0, the function can be said to be continuous.

