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① Given a function  $f(x)$   $\lim_{x \rightarrow 3} f(x)$

Since there is no

function to substitute the limits of  $x$ , we can say that  $f(x) = x$

$$x = 3$$

$$\therefore 3.142.$$

② The model of a system has been developed by an engineer to be as given in the equation  $f(x)$ ,  $5x - 24$ . Given that  $\delta = 0.01$ , and using a step  $-20.01$  demonstrate, in a tabular form, that the limit of the model as  $x \rightarrow 6$  is equal to 9.

| $f(x)$ | $x - \delta$ | $x = 6$ | $x + \delta$ | $f(x)$ |
|--------|--------------|---------|--------------|--------|
| 8.50   | 5.90         |         | 6.10         | 9.50   |
| 8.55   | 5.91         |         | 6.09         | 9.45   |
| 8.60   | 5.92         |         | 6.08         | 9.40   |
| 8.65   | 5.93         |         | 6.07         | 9.35   |
| 8.70   | 5.94         |         | 6.06         | 9.30   |
| 8.75   | 5.95         |         | 6.05         | 9.25   |
| 8.80   | 5.96         |         | 6.04         | 9.20   |
| 8.85   | 5.97         |         | 6.03         | 9.15   |
| 8.90   | 5.98         |         | 6.02         | 9.10   |
| 8.95   | 5.99         |         | 6.01         | 9.05   |
| 9.00   | 6.00         | ↓       | 6.00         | 9.00   |

③ Find the limit of the model system question given below

$$\lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|}$$

$$\lim_{x \rightarrow 3^+} \frac{3-x}{|3-x|} = \frac{3-(3+8)}{|3-(3+8)|} = \frac{3-3-8}{|3-3-8|}$$

$$= \frac{-8}{|-8|} = \frac{-8}{8} = -1$$

④ Evaluate the limit of the model given  $\lim_{x \rightarrow 3} \frac{x-3}{|x-3|}$

$$\lim_{x \rightarrow 3} \frac{x-3}{|x-3|} = \frac{(3)-3}{|(3)-3|} = \frac{0}{0} \text{ undefined}$$

Since the  $\lim_{x \rightarrow 3} \frac{x-3}{|x-3|}$  is undefined, use substitute  $(3+8)$  and  $(3-8)$  for:

$$\lim_{x \rightarrow 3^+} \frac{x-3}{|x-3|} = \frac{(3-8)-3}{|(3-8)-3|} = \frac{-8}{8} = -1$$

Therefore, the R.H.S and L.H.S limits do not combine the limit of  $\frac{x-3}{|x-3|}$  as the equation to 3 doesn't exist.

⑤ Show that the function given in equation  $f(x) = \sqrt{x-4}$  is continuous on the interval  $(4, 8)$

$$f(x) = \sqrt{x-4}$$

Substituting 4 for x  $f(x) = \sqrt{(4)-4} = \sqrt{0} = 0$

Substituting 8 for x  $f(x) = \sqrt{(8)-4} = \sqrt{4} = 2$

| x | f(x) = $\sqrt{x-4}$ |
|---|---------------------|
| 4 | 0                   |
| 5 | 1.0                 |
| 6 | 1.41                |
| 7 | 1.73                |
| 8 | 2                   |

