

2) The model of a system has been developed by an Eng

$$f(x) = 5x - 21$$

Given that  $\delta$  (small increment) = 0.1  
and using step of 0.01 demonstrate the limit of model  
as  $x \rightarrow 6$  is equal to 9

$$\text{for } x^+ = 6 + 0.1 = 6.1 \quad \text{for } x^- = 6 - 0.1 = 5.9$$

$x^-$	$f(x^-)(5x - 21)$	$x$	$x^+$	$f(x^+)(5x - 21)$
5.90	8.50		6.10	9.50
5.91	8.55		6.09	9.45
5.92	8.60		6.08	9.40
5.93	8.65		6.07	9.35
5.94	8.70		6.06	9.30
5.95	8.75		6.05	9.25
5.96	8.80		6.04	9.20
5.97	8.85		6.03	9.15
5.98	8.90		6.02	9.10
5.99	8.95		6.01	9.05
6.00	9.00		6.00	9.00

Since the limits on  $x^+$  and  $x^-$  are both real and are both approaching 9.00

The limit of  $f(x) = 5x - 21$  as  $x \rightarrow 6$   
is equal to 9

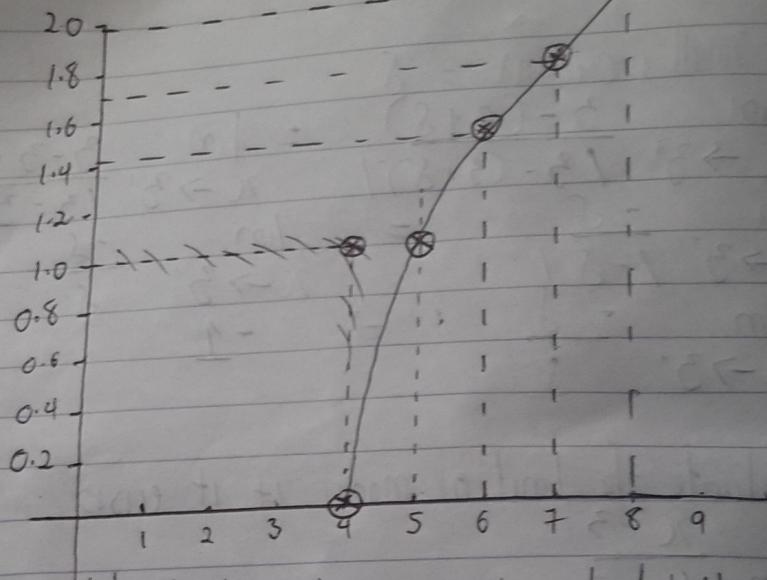
The limit as  $x$  tends to 3 doesn't exist

5) Show that the function given

$$f(x) = \sqrt{x-4}$$

i) continuous on interval (4, 8)

$x$	$f(x)$
4	0
5	1
6	$\sqrt{2}$ or 1.41
7	$\sqrt{3}$ or 1.73
8	2



Since the graph did not stop at any point and didn't require my hand to be raised up when drawing, it is a continuous graph.

Q) Given a function to be

$$f(x) = \pi \quad \text{find the limit as } x \text{ approaches 3}$$

$$\lim_{x \rightarrow 3} \pi = \pi = 3.142$$

The limit is  $\pi$  because it's a constant and contains no variable

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3) find the limit of model equation

$$\lim_{x \rightarrow 3^+} \frac{3 - x}{13 - x}$$

for small increment =  $\delta$

$$\Rightarrow \lim_{x \rightarrow 3^+} \frac{3 - (3 + \delta)}{13 - (3 + \delta)} = \lim_{x \rightarrow 3^+} \frac{3 - 3 - \delta}{13 - 3 - \delta}$$

$$= \lim_{x \rightarrow 3^+} \frac{-\delta}{10 - \delta} \neq \lim_{x \rightarrow 3^+} \frac{-\delta}{\delta}$$

$$= \lim_{x \rightarrow 3^+} \frac{-\delta}{\delta} \Rightarrow -1$$

4) Evaluate the limit of model if it exists

$$\lim_{x \rightarrow 3} \frac{x - 3}{x - 3}$$

$$\Rightarrow \lim_{x \rightarrow 3} \frac{x - 3}{|x - 3|} \Rightarrow \lim_{x \rightarrow 3} \frac{3 - 3}{13 - 3}$$

$\lim_{x \rightarrow 3}$  0/0 is undefined. Undefined  
 $x \rightarrow 3$

Since it's undefined we'll do for  $3^+$  and  $3^-$

$$\lim_{x \rightarrow 3^+} \frac{x - 3}{|x - 3|} = \lim_{x \rightarrow 3^+} \frac{3 + \delta - 3}{13 + \delta - 3}$$

$$= \lim_{x \rightarrow 3^+} \frac{\delta}{10 + \delta} = \lim_{x \rightarrow 3^+} \frac{\delta}{\delta} = 1$$

for  $3^-$

$$\lim_{x \rightarrow 3^-} \frac{x - 3}{|x - 3|} = \lim_{x \rightarrow 3^-} \frac{3 - \delta - 3}{13 - \delta - 3} = \lim_{x \rightarrow 3^-} \frac{-\delta}{10 - \delta}$$

$$= \lim_{x \rightarrow 3^-} \frac{-\delta}{\delta} = -1$$

Since  $\lim_{x \rightarrow 3^+} f(x)$  and  $\lim_{x \rightarrow 3^-} f(x)$  are not equal