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Matric NO: 17/ENGG06/034

ENG 281

1. $\lim_{x \rightarrow 3} f(x)$

Soln
 $f(x) = \pi$
 $\therefore \lim_{x \rightarrow 3} \pi = \pi$

2. $f(x) = 5x - 21$

Soln
 $\delta = 0.1$, Step: 0.01

	x	$f(x)$
$5(6.1) - 21 = 9.5$	6.1	9.5
$5(6.01) - 21 = 9.05$	6.01	9.05
$5(6.001) - 21 = 9.005$	6.001	9.005
$5(6.0001) - 21 = 9.0005$	6.0001	9.0005
$5(6.00001) - 21 = 9.00005$	6.00001	9.00005
$5(6.000001) - 21 = 9.000005$	6.000001	9.000005
$5(6.0000001) - 21 = 9.0000005$	6.0000001	9.0000005

$\therefore [f(x) = 5x - 21]$ tends towards 9 as $x \rightarrow 6$

3. $\lim_{x \rightarrow 3^+} \frac{3-x}{3-x}$

Solution

$$\therefore \lim_{x \rightarrow 3^+} \frac{3-x}{3-x} = \frac{3-(3+h)}{3-(3+h)} = \frac{3-3-h}{3-3-h}$$

$$= \frac{0+h}{0+h} = \frac{h}{h} \quad \text{hence } h \rightarrow 0 = \frac{0}{0}$$

\therefore The limit is indeterminate at the right hand limit.

4 $\lim_{x \rightarrow 3} \frac{x-3}{|x-3|}$

$\therefore x < 0$

$$\lim_{x \rightarrow 3^-} \frac{(3-h)-3}{(3-h)-3}$$

where $h \rightarrow 0$

At $x \geq 0$

$$\lim_{x \rightarrow 3^+} \frac{(3+h)-3}{(3+h)-3} \quad \text{where } h \rightarrow 0$$

$$= \frac{3-3}{3-3} = \frac{0}{0} \quad \text{indeterminate}$$

$\therefore \frac{0}{0}$ i.e. indeterminate form.

\therefore The limits do not exist from both left hand and right hand limits.

Show that $f(x) = \sqrt{x-4}$ is continuous on interval $[4, 8]$

Soln

At $f(x) = \sqrt{x-4}$

$$x \rightarrow 4 = \sqrt{4-4} = \sqrt{0-0}$$

$$f(x) = \sqrt{x-4}$$

$$\text{At } x \rightarrow 8 = \sqrt{8-4} = \sqrt{4} = 2$$

\therefore Hence $f(x)$ is continuous at $(4, 8)$