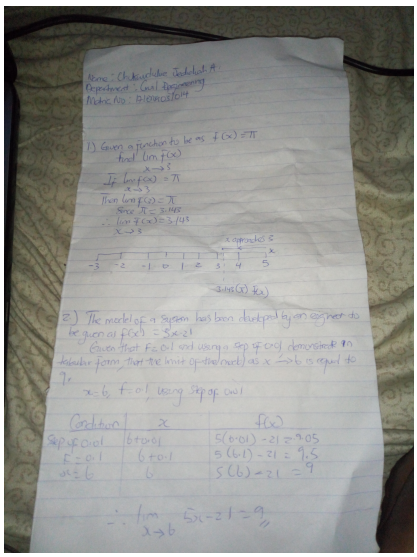

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1) Given a function to be as $f(x) = \pi$
find $\lim_{x \to 3} f(x)$
The $\lim_{x \to 3} f(x) = \pi$
$\lim_{x \to 3} f(x) = \pi$
Since $\pi = 3.142$
$\therefore \lim_{x \to 3} f(x) = 3.142$

x approaches 3

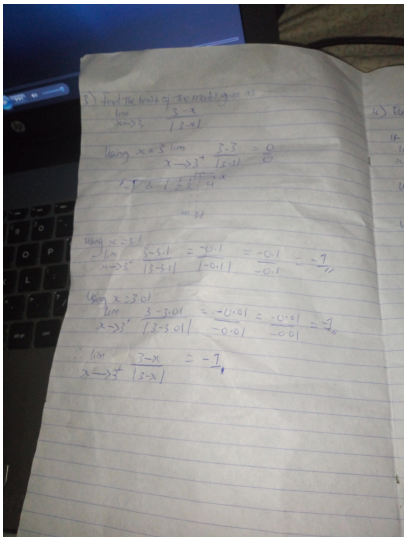
-3 -2 -1 0 1 2 3 4 5 x

3 = lim(x) f(x)

2) The model of a system has been developed by an engineer to be given as $f(x) = 5x - 21$
Given that $\varepsilon = 0.1$ and using a step of 0.01 demonstrate by definition form that the limit of the model as $x \to 6$ is equal to 9.
$x \to 6$, $\varepsilon = 0.1$, using Step of 0.01

Condition	x	f(x)
Step of 0.01	6+0.01	5(6.01) - 21 = 9.05
$\varepsilon = 0.1$	6+0.1	5(6.1) - 21 = 9.5
$x = 6$	6	5(6) - 21 = 9

$\therefore \lim_{x \to 6} 5x - 21 = 9$ //



3) Proof the limit of the modal given as

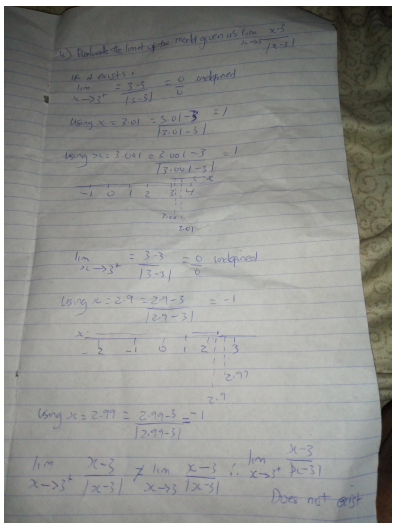
$\lim_{x \to 3} \frac{3-x}{|3-x|}$

Using $x = 3$ $\lim_{x \to 3^+} \frac{3-3}{|3-3|} = \frac{0}{0}$

Using $x = 3.1$
$\lim_{x \to 3^+} \frac{3-3.1}{|3-3.1|} = \frac{-0.1}{|-0.1|} = \frac{-0.1}{0.1} = -1$ //

Using $x = 3.01$
$\lim_{x \to 3^+} \frac{3-3.01}{|3-3.01|} = \frac{-0.01}{|-0.01|} = \frac{-0.01}{0.01} = -1$ //

$\lim_{x \to 3^+} \frac{3-x}{|3-x|} = -1$



4) Proof the limit of the model given as $\lim_{x \to 3} \frac{x-3}{|x-3|}$

$\lim_{x \to 3^+} \frac{3-3}{|3-3|} = \frac{0}{0}$ undefined

Using $x = 3.01$ $\frac{3.01-3}{|3.01-3|} = 1$

Using $x = 3.001$ $\frac{3.001-3}{|3.001-3|} = 1$

-1 0 1 2 3 4 x

3.001

3.01

$\lim_{x \to 3^+} \frac{3-3}{|3-3|} = \frac{0}{0}$ undefined

Using $x = 2.9$ $\frac{2.9-3}{|2.9-3|} = -1$

2 -1 0 1 2 3

2.9

Using $x = 2.99$ $\frac{2.99-3}{|2.99-3|} = -1$

$\lim_{x \to 3^+} \frac{x-3}{|x-3|} \neq \lim_{x \to 3^-} \frac{x-3}{|x-3|} \therefore \lim_{x \to 3} \frac{x-3}{|x-3|}$ Does not exist