



There exists a possible error of 1.5% for
 a and b , $\therefore \frac{1.5}{100} \times a = 0.015a$, $\frac{1.5}{100} \times b = 0.015b$

$$A = \frac{1}{2}ab = \frac{ab}{2}$$

$$\frac{\partial A}{\partial a} = \frac{b}{2}$$

$$\frac{\partial A}{\partial b} = \frac{a}{2}$$

For positive

$$\delta A = \frac{\partial A}{\partial a} \delta a + \frac{\partial A}{\partial b} \delta b$$

$$\delta A = \frac{b}{2} \cdot 0.015a + \frac{a}{2} \cdot 0.015b$$

$$\delta A = \frac{0.015ab}{2} + \frac{0.015ab}{2} = \frac{0.03ab}{2}$$

Recall $\frac{ab}{2} = A$

$$\therefore \delta A = 0.03A$$

For negative

$$\delta A = \frac{b}{2} \cdot (-0.015a) + \frac{a}{2} \cdot (-0.015b)$$

$$\delta A = -\frac{0.015ab}{2} - \frac{0.015ab}{2}$$

$$= -\frac{0.03ab}{2}$$

Recall $\frac{ab}{2} = A$

$$\therefore \delta A = -0.03A$$

\therefore The percentage increment/decrement in Area
 $= \pm 0.03A$

b Change in Length of h

by pythagoras theorem

$$h^2 = a^2 + b^2$$

$$h = \sqrt{a^2 + b^2} = (a^2 + b^2)^{1/2}$$

$$\text{Let } u = a^2 + b^2$$

$$h = u^{1/2} \quad \frac{dh}{du} = \frac{1}{2} u^{-1/2}$$

$$\frac{du}{da} = 2a, \quad \frac{du}{db} = 2b$$

$$\therefore \frac{dh}{da} = \frac{dh}{du} \times \frac{du}{da}$$

$$= (2a) \cdot \frac{1}{2} (a^2 + b^2)^{-1/2}$$

$$= 2a$$

$$\frac{1}{2} (a^2 + b^2)^{-1/2}$$

$$\frac{dh}{db} = \frac{dh}{du} \times \frac{du}{db}$$

$$= (2b) \cdot \frac{1}{2} (a^2 + b^2)^{-1/2}$$

$$= \frac{2b}{2 (a^2 + b^2)^{1/2}}$$

$$\therefore \delta h = \frac{dh}{da} \cdot \delta a + \frac{dh}{db} \cdot \delta b$$

$$\text{for positive} = \left[\frac{2a}{\frac{1}{2} (a^2 + b^2)^{1/2}} \right] (0.015a) + \left[\frac{2b}{\frac{1}{2} (a^2 + b^2)^{1/2}} \right] (0.015b)$$

$$= \frac{0.03a^2 + 0.03b^2}{\frac{1}{2} (a^2 + b^2)^{1/2}} = \frac{0.03(a^2 + b^2)}{\frac{1}{2} (a^2 + b^2)^{1/2}} = \frac{0.03h^2}{\frac{1}{2} (h^2)^{1/2}} = \frac{0.03h^2}{0.5h}$$

$$\delta h = 0.06h$$

$$\text{for negative} = \left[\frac{2a}{\frac{1}{2} (a^2 + b^2)^{1/2}} \right] (-0.015a) + \left[\frac{2b}{\frac{1}{2} (a^2 + b^2)^{1/2}} \right] (-0.015b)$$

$$= \frac{-0.03(a^2 + b^2)}{\frac{1}{2} (a^2 + b^2)^{1/2}} = \frac{-0.03h^2}{0.5h} = -0.06h$$

$$\therefore \delta h = \pm 0.06h$$