

O GOMUEGBUNAM FAVOUR CHIDI

CHEMICAL ENGINEERING

17/ENAG1021

A ENG281 Assignment 2.

The hypotenuse of a right angled triangle is denoted as c , and the other two sides are denoted as a and b . If the possible error of measuring each of a and b is $\pm 1.5\%$, find the maximum possible error in calculating (a) the area of the triangle (b) the length of the hypotenuse.

sol

$$(a) \text{ Area} = \frac{1}{2} ab$$

$$\delta A = \frac{\partial A}{\partial a} \delta a + \frac{\partial A}{\partial b} \delta b$$

$$\frac{\partial A}{\partial a} = \frac{b}{2} \quad \frac{\partial A}{\partial b} = \frac{a}{2}$$

$$\delta a = \pm \frac{3a}{200} \quad \delta b = \pm \frac{3b}{200}$$

$$\delta A = \frac{b}{2} \left(\pm \frac{3a}{200} \right) + \frac{a}{2} \left(\pm \frac{3b}{200} \right)$$

$$= \pm \frac{a \cdot b}{2} \left[\frac{3}{200} + \frac{3}{200} \right] = \pm A \cdot \frac{3}{100}$$

$$\therefore \delta A = 3 \text{ percent of } A$$

$$(b) \quad h = \sqrt{a^2 + b^2} = (a^2 + b^2)^{1/2}$$

$$\delta h = \frac{dh}{da} \delta a + \frac{dh}{db} \delta b$$

$$\frac{dh}{da} = \frac{1}{2} (a^2 + b^2)^{-1/2} (2a) = a \cdot (a^2 + b^2)^{-1/2} = \frac{a}{\sqrt{a^2 + b^2}}$$

$$\frac{dh}{db} = \frac{1}{2} (a^2 + b^2)^{-1/2} (2b) = b \cdot (a^2 + b^2)^{-1/2} = \frac{b}{\sqrt{a^2 + b^2}}$$

$$\delta a = \pm \frac{3a}{200} \quad \delta b = \pm \frac{3b}{200}$$

$$\therefore \delta h = \frac{a}{\sqrt{a^2 + b^2}} \left(\pm \frac{3a}{200} \right) + \frac{b}{\sqrt{a^2 + b^2}} \left(\pm \frac{3b}{200} \right)$$

$$= \pm \frac{3}{200} \cdot \frac{a^2 + b^2}{\sqrt{a^2 + b^2}}$$

$$= \pm \frac{3}{200} \cdot \sqrt{a^2 + b^2}$$

$$= \pm \frac{3}{200} (h)$$

~~$\therefore \delta h = 0.015\%$ percent of h~~

$\therefore \delta h = 1.5$ percent of h