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17/ENGG06/001

MECHANICAL ENGINEERING

ENG 281

MATHS QUIZ

(a) Area of a triangle

$$A = \frac{1}{2} ab$$

$$\Delta A = \frac{\Delta A}{\Delta a} \cdot \Delta a + \frac{\Delta A}{\Delta b} \cdot \Delta b$$

$$\therefore = \frac{b}{2} \Delta a + \frac{a}{2} \Delta b$$

$$\Delta a = \pm \frac{0.5a}{100}, \quad \Delta b = \pm \frac{0.5b}{100}$$

$$\therefore = \frac{b}{2} \cdot \left(\frac{\pm 0.5a}{100} \right) + \frac{a}{2} \left(\frac{\pm 0.5b}{100} \right)$$

Factorizing out $\frac{ab}{2}$

$$\text{Therefore; } \frac{1}{2} ab \pm \left(\frac{1}{100} \right)$$

$$\text{But Area} = \frac{ab}{2}$$

$$\therefore \pm A = \frac{1}{100}$$

② The length of hypotenuse wrt length

$$\text{Recall, } h = \sqrt{a^2 + b^2}$$

$$\delta h = \frac{\delta h}{\delta a} \cdot \delta a + \frac{\delta h}{\delta b} \cdot \delta b$$

$$\text{Let } h = \sqrt{u}, \quad \text{where } u = a^2 + b^2$$

$$\frac{\delta u}{\delta a} = 2a$$

$$\frac{\delta u}{\delta b} = 2b$$

$$\frac{\delta h}{\delta u} = \frac{1}{2} u^{-1/2}$$

$$\frac{\delta h}{\delta a} = \frac{\delta u}{\delta a} \times \frac{dh}{du}$$

$$\text{i) } \frac{\delta h}{\delta a} = \frac{1}{2} u^{-1/2} \times 2a$$

$$= a u^{-1/2}$$

$$\therefore \frac{\delta h}{\delta a} = \frac{a}{\sqrt{u}}$$

$$\text{Since } u = a^2 + b^2$$

$$\therefore \frac{\delta h}{\delta a} = \frac{a}{\sqrt{a^2 + b^2}}$$

$$\text{ii) } \frac{\delta h}{\delta b} = \frac{\delta h}{\delta u} \times \frac{\delta u}{\delta b}$$

$$= \frac{1}{2} u^{-1/2} \times 2b$$

$$\frac{\delta h}{\delta b} = \frac{b}{\sqrt{u}}$$

$$\text{Recall, } u = a^2 + b^2$$

$$\therefore \frac{\delta h}{\delta b} = \frac{b}{\sqrt{a^2 + b^2}}$$

$$\delta a = \pm \frac{1.5}{100} a$$

$$\delta b = \pm \frac{1.5}{100} b$$

$$\delta h = \frac{\delta h}{\delta a} \cdot \delta a$$

$$+ \frac{\delta h}{\delta b} \cdot \delta b$$

$$\delta h = \frac{a}{\sqrt{a^2+b^2}} \left(\pm \frac{1.5 a}{100} \right) + \frac{b}{\sqrt{a^2+b^2}} \left(\pm \frac{1.5 b}{100} \right)$$

By factoring ~~$\frac{\pm 1.5}{100}$~~ $(a$

$$a \frac{\pm 1.5 a^2}{100 \sqrt{a^2+b^2}} + \frac{\pm 1.5 b^2}{100 \sqrt{a^2+b^2}}$$

$$\therefore \frac{\pm 3}{100} \left(\frac{a^2+b^2}{\sqrt{a^2+b^2}} \right) \Rightarrow \frac{\pm 3}{100} (\sqrt{a^2+b^2})$$

Recall that $h = \sqrt{a^2+b^2}$

$$\therefore \delta h = \frac{\pm 3}{100} (h)$$

\therefore The change in h is $\pm 3\%$ when there's a change of $\pm 1.5\%$ in the lengths 'a and b'