

Name: Anyanechi Obinna  
Dept: Computer Engineering  
Matrix no: 17/ENGUAL811

- 1) The hypotenuse of a right angle triangle is denoted by  $a$ , and the other two sides are denoted as  $a$  and  $b$ . If the possible error of measuring each of  $a$  and  $b$  is 1.5%, find the maximum possible in calculating
- The area of the triangle
  - The length of the hypotenuse

$$a) A = \frac{ab}{2} \quad dA = \frac{da}{2} + \frac{db}{2}$$

$$\frac{da}{a} = \frac{b}{2}, \quad \frac{db}{b} = \frac{a}{2} \quad da = \pm \frac{3a}{200} \quad db = \pm \frac{3b}{200}$$

$$dA = \frac{b}{2} \left( \pm \frac{3a}{100} \right) + \frac{a}{2} \left( \frac{3b}{100} \right)$$

$$= \frac{a \cdot b}{2} \left( \frac{3a}{100} + \frac{3b}{100} \right)$$

$$dA = 3\% \text{ of } A$$

$$b) h = \sqrt{a^2 + b^2} \quad (a^2 + b^2)^{-1/2}$$
$$dh = \frac{da}{\sqrt{a^2 + b^2}} + \frac{db}{\sqrt{a^2 + b^2}}$$

$$\frac{da}{\sqrt{a^2 + b^2}} = \frac{3a}{2} (a^2 + b^2)^{-1/2}$$

$$\frac{db}{\sqrt{a^2 + b^2}}$$

$$\frac{db}{\sqrt{a^2 + b^2}} = \frac{3b}{2} (a^2 + b^2)^{-1/2}$$

$$\frac{b}{\sqrt{a^2 + b^2}}$$

$$\Delta a = \pm \frac{3a}{200}$$

$$\Delta b = \pm \frac{3b}{200}$$

$$\Delta h = \frac{g}{\sqrt{a^2+b^2}} \left( \pm \frac{3a}{200} \right) + \frac{b}{\sqrt{a^2+b^2}} \left( \pm \frac{3b}{200} \right)$$

$$= \frac{3}{100} \left( \frac{a^2+b^2}{\sqrt{a^2+b^2}} \right)$$

$$= \pm \frac{3}{100} \sqrt{a^2+b^2} \quad \pm \frac{3}{200}$$

$$\Delta h = 1.5 \% \Delta h$$