

$$\delta h = \frac{\partial h}{\partial a} \cdot \delta a + \frac{\partial h}{\partial b} \cdot \delta b$$

$$u = (a^2 + b^2)^{1/2}$$

$$u^2 = a^2 + b^2$$

$$u = \sqrt{a^2 + b^2}$$

$$\frac{dh}{du} = \frac{1}{2} u^{-1/2} \quad \frac{du}{da} = 2a$$

$$\begin{aligned} \frac{dh}{da} &= \frac{dh}{du} \cdot \frac{du}{da} \\ &= \frac{1}{2} u^{-1/2} \times 2a \\ &= \frac{1}{2} (a^2 + b^2)^{-1/2} \times 2a \\ &= \frac{a}{\sqrt{a^2 + b^2}} \end{aligned}$$

$$= \left(\frac{a}{\sqrt{a^2 + b^2}} \pm \frac{3a}{200} \right) + \left(\frac{b}{\sqrt{a^2 + b^2}} \pm \frac{3b}{200} \right)$$

$$= \frac{a^2}{\sqrt{a^2 + b^2}} \pm \frac{3}{200} + \frac{b^2}{\sqrt{a^2 + b^2}} \pm \frac{3}{200}$$

$$= \frac{a^2 + b^2}{\sqrt{a^2 + b^2}} \pm \left(\frac{3}{100} \right)$$

$$= \frac{a^2 + b^2}{\sqrt{a^2 + b^2}}$$

~~∴~~ ∴ increases and decreases by 3%

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MECH. ENG.

ENIG 281



Recall that $A = \frac{1}{2}ab$

$$\eta = \frac{\Delta A}{A} \times 100\%$$

$$\Delta SA = \frac{\Delta a}{2a} \cdot ba + \frac{\Delta b}{2b} \cdot ab$$

$$= \frac{1}{2} \cdot \frac{\Delta a}{a} \cdot ba + \frac{1}{2} \cdot \frac{\Delta b}{b} \cdot ab$$

$$\Delta SB = \pm \frac{1.5}{100} \times b$$

$$= \pm \frac{3 \cdot a}{200}$$

$$\Delta Sa = \pm \frac{1.5}{100} \times a$$

$$= \pm \frac{3 \cdot a}{100}$$

$$= \frac{1}{2} \cdot \pm \frac{3}{100} \cdot ba + \frac{1}{2} \cdot \pm \frac{3}{100} \cdot ab$$

$$= \frac{3ab}{2} \left(\pm \frac{1}{200} + \pm \frac{1}{200} \right)$$

$$= \frac{3ab}{2} \left(\pm \frac{1}{100} \right)$$

$$\text{Area} = \frac{ab}{2}$$

$$3A = \left(\pm \frac{1}{100} \right)$$

$$A = \left(\pm \frac{3}{100} \right)$$

A increases and decreases by 3%