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1. $y = x^3 e^{4x}$
 $y = UV$
 $U = e^{4x} \quad U' = 4e^{4x} \quad U'' = 16e^{4x} \quad U''' = 64e^{4x}$
 $V = x^3 \quad V' = 3x^2 \quad V'' = 6x \quad V''' = 6$

$y^{(5)} = U^{(5)}V + 5U^{(4)}V' + 10U^{(3)}V'' + 10U^{(2)}V''' + 5U'V^{(4)} + UV^{(5)}$
 $y^{(5)} = 1024e^{4x} \cdot x^3 + 5 \cdot 256e^{4x} \cdot 3x^2 + 10 \cdot 64e^{4x} \cdot 6x + 10 \cdot 16e^{4x} \cdot 6 + 5 \cdot 4e^{4x} \cdot 6 + e^{4x} \cdot 0$
 $y^{(5)} = 1024e^{4x} \cdot x^3 + 3840e^{4x} \cdot x^2 + 3840e^{4x} \cdot x + 960e^{4x}$
 $y^{(5)} = e^{4x} (1024x^3 + 3840x^2 + 3840x + 960)$
 $y^{(5)} = 64e^{4x} (16x^3 + 60x^2 + 60x + 15)$

ii) $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = 0$
 $x^2 y'' + x y' + y = 0$

Differentiating n times using Leibnitz theorem $x^2 y''$
 taking $u = y''$ and $v = x^2$
 $x^2 y'' = n C_0 u^{(n)} v + n C_1 u^{(n-1)} v' + n C_2 u^{(n-2)} v''$
 $(1) y^{(n+2)} x^2 + n y^{(n+1)} \cdot 2x + \frac{n(n-1)}{2!} y^{(n)} \cdot 2 + 0$
 $y^{(n+2)} x^2 + n y^{(n+1)} \cdot 2x + \frac{n(n-1)}{2!} y^{(n)} \cdot 2 + 0$

$x y'$
 taking $u = y'$ and $v = x$
 $x y' = (1) y^{(n+1)} x + n y^{(n)} \cdot 1 + 0$
 $y^{(n+1)} x + n y^{(n)} + 0$
 $y = y^{(n)}$
 Adding all the terms:

