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 16/EN0604/021
 Electrical/Electronics Engineering
 EAG 381 Assignment.

1. $y = e^{x^2+x}$
 $y' = (2x+1)e^{x^2+x}$
 where: $y = 2x+1, v = e^{x^2+x}$
 $\frac{dy}{dx} = 2 \quad \frac{dy}{dx} = (2x+1)e^{x^2+x}$

$$y'' = y \frac{dy}{dx} + v \frac{dy}{dx}$$

$$y'' = (2x+1)(2x+1)e^{x^2+x} + e^{x^2+x} \quad (2)$$

$$\therefore y'' = y'(2x+1) + 2y$$

from Leibnitz Theorem

$$y'' - y'(2x+1) - 2 = 0$$

$$w_1 = y'', u = 1, u' = y^{n+2}$$

$$u = y''; v' = 0; m_1^n = n! u^{n-0} v^x$$

$$w_2 = y'(2x+1), v = 2x+1 = y^{n+2}$$

$$u = y'; v' = 2$$

$$u^n = y^{n+1}; u_1^n = n! u^{n-0} u' + n! u^{n-1} v'$$

$$v'' = 0$$

$$= u^n v + n u^{n-1}$$

$$= y^{n+1}(2x+1) + n y^n - 2$$

$$w_3 = 2y$$

$$u = y; v = 2; v' = 0$$

$$u^n = y^n$$

$$w_3^n = n! u^{n-0} v$$

$$= 2y^n$$

$$y^n - y'(2x+1) - 2y = 0$$

$$y^{n+1} - y^{n+1}(2x+1) - 2ny^n - 2y^n = 0$$

$$y^{n+2} - y^{n+1}(2x+1) - 2y^n(n+1) = 0$$

$$y^{n+2} - y^{n+1}(2x+1) + 2y^n(n+1)$$

2. $y = x^3 e^{4x}$

$$v^0 = x^3; v' = 3x^2; v'' = 6x; v''' = 6$$

$$u = e^{4x}; u' = 4e^{4x}; u'' = 16e^{4x}; u''' = 64e^{4x}$$

$$u^n = 4^n e^{4x}$$

$$y^n = n! u^{n-0} v^0 + n! u^{n-1} v' + n! u^{n-2} v'' + n! u^{n-3} v'''$$

$$= u^n v' + n u^{n-1} v'' + \frac{n(n-1)}{2!} u^{n-2} v''' + \frac{n(n-1)(n-2)}{3!} u^{n-3} v''''$$

$$= 4^n e^{4x} \cdot x^3 + n 4^{n-1} e^{4x} \cdot 3x^2 + \frac{n(n-1) 4^{n-2} e^{4x} \cdot 6x}{2} + \frac{n(n-1)(n-2) 4^{n-3} e^{4x} \cdot 6}{3x}$$

$$= 4^n e^{4x} x^3 + n 4^{n-1} e^{4x} 3x^2 + n(n-1) 4^{n-2} e^{4x} 3x + n(n-1)(n-2) 4^{n-3} e^{4x}$$

$$4e^{n-3} e^{4x}$$

$$= 4^{n-3} e^{4x} [4x^3 + n4^2 3x^2 + n(n-1)4 \cdot 3x + n(n-1)(n-2)]$$

$$= 4^{n-3} e^{4x} [64x^3 + n48x^2 + 12(n-1) + n(n-1)(n-2)]$$

$$y^3 = 4^{5-3} e^{4x} [64x^3 + (5 \times 48)x^2 + 12 \times 5(5-1)x + 5(5-1)(5-2)]$$

$$y^3 = 16e^{4x} [64x^3 + 240x^2 + 240x + 60]$$

ii. $x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = 0$

$$x^2 y'' + x y' + y = 0$$

$$w_1 = x^2 y''$$

$$u^0 = v = y''$$

$$v' = y''', v'' = y^{(4)}$$

$$v^n = y^{n+2}$$

$$w_2 = x y'$$

$$v^0 - u = y'$$

$$v' = y''', v'' = y^{(4)}$$

$$v^n = y^{n+1}$$

$$w_3 = y$$

$$v = y$$

$$v = y', v'' = y''$$

$$v^n = y^n$$

$$w_1^n = 1^n (0 \cdot 0 \cdot u^{n-0} v^0 + \binom{n}{1} v^{n-1} v' + \binom{n}{2} v^{n-2} v''$$

$$= n y^n + n w^{n-1} v' + \frac{n(n-1)}{2!} v^{n-2} v''$$

$$= y^{n+2} v + n y^{n+1} 2x + \frac{n(n-1) 2 y^n x}{2}$$

$$= y^{n+2} v + n y^{n+1} 2x + (n-1) n y^n x$$

$$= y^n (y^2 x^2 + n y^2 x + n(n-1))$$

$$u_2^n = n (0 \cdot v^{n-0} v^0 + \binom{n}{1} v^{n-1} v' + \binom{n}{2} v^{n-2} v''$$

$$v'' + \binom{n}{3} v^{n-3} v''$$

$$= v^n u^0 + n v^{n-1} v' + \frac{(n-1)n v^{n-2}}{2!} 0$$

$$= y^{n+1} x + n y^0 \cdot 1 + 0$$

$$= y^n (x y + n)$$

$$w_3^n = n (0 \cdot v^{n-0} v^0 + \binom{n}{1} v^{n-1} v'$$

$$= u^n y^0 + 0$$

$$= y^n$$

$$x^2 y'' + x y' + y = 0$$

$$w_1 + w_2 + w_3 = 0$$

$$y^n (y^2 x^2 + n^2 x y + n(n-1)) + y^n (x y + n) + y^n = 0$$

$$\text{At } x = 0$$

$$y^n n(n-1) + y^n n + y^n = 0$$

$$n(n-1) + n + 1 = 0$$

$$y^n \dots y^n n(n-1) - ny^n$$

$$\text{at } n=1$$

$$y = 0 - y'$$

$$y = -y'$$

$$\Rightarrow x^2 y^{n+2} + n^2 x y^{n+1} + n(n-1) y^n$$

$$x y^{n+1} + n y^n + y^n = 0$$

$$\Rightarrow x^2 y^{n+2} + x y^{n+1} (2n+1) + y^n (n^2 + n + 1) = 0$$

$$\Rightarrow x^2 y^{n+2} + (2n+1) x y^{n+1} + (n^2 + 1) y^n = 0$$