

ENG 381

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Computer ENGINEERING.

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$$y = e^{-2x} + x$$

$$y' = (2x+1) e^{x^2+x}$$

where : $u = 2x+1$

$$v = e^{x^2+x}$$

$$\frac{dy}{dx} = 2 \frac{du}{dx} = (2x+1) e^{x^2+x}$$

$$y'' = u \frac{du}{dx} + v \frac{dv}{dx}$$

$$y'' = (2x+1)(2x+1) e^{x^2+x} + e^{x^2+x}(2)$$

$$\therefore y'' = y' (2x+1) + 2y$$

From ~~the~~ Leibniz theorem

$$y'' - y' (2x+1) - 2y = 0$$

$$1 = y'' \quad u = 1$$

$$u^n = y^{n+2}$$

$$u = y'' \quad v' = 0$$

$$m_1 = n(2u - 0)u = y^{n+2}$$

$$w_2 = y_1 (2x+1)$$

$$u = y'$$

$$v = 2x+1$$

$$u^n = y^{n+1}$$

$$v' = 2$$

$$u'' \neq 0$$

$$u^n = n(2u^{n-1}v + m(u^{n-1}v))$$

$$= v^n v + n u^{n-1} v$$

$$= y^{n+1} (2x+1) + n y^n$$

$$w_5 = 2y$$

$$u = y$$

$$u^n = y^n$$

$$v = 2 \quad v' = 0$$

$$w_3 = n(2u^{n-1}v)$$

$$= 2y^n$$

$$y^{n+1} - y^n (2x+1) - 2y = 0$$

$$y^{n+2} - y^{n+1} (2x+1) - 2y^n = 0$$

$$y^{n+2} - y^{n+1} (2x+1) - 2y^n (n+1) = 0$$

$$y^{n+2} = y^{n+1} (2x+1) + 2y^n (n+1)$$

$$2) y = x^3 e^{4x}$$

$$V^0 = x^3, V^1 = 3x^2, V^2 = 6x, V^3 = 6$$

$$U = e^{4x}, U^1 = 4e^{4x}, U^2 = 16e^{8x}, U^3 = 64e^{12x}$$

$$U^n = 4^n e^{4nx}$$

$$y^n = \sum (U^n \cdot 0 \cdot V^0 + \sum (U^{n-1} V^1 + \dots + (U^{n-2} V^2 + \dots + (U^{n-3} V^3 + \dots + U^n V^n))$$

$$= V^0 V^1 + n U^{n-1} V^1 + \frac{n(n-1)}{2!} U^{n-2} V^2 + \frac{n(n-1)(n-2)}{3!} U^{n-3} V^3 + \dots + U^n V^n$$

U^n

$$= 4^n e^{4nx} x^3 + n 4^{n-1} e^{4(n-1)x} 3x^2 + \frac{n(n-1)}{2} 4^{n-2} e^{4(n-2)x} 6x + \frac{n(n-1)(n-2)}{6} 4^{n-3} e^{4(n-3)x} 6$$

$$+ (n-1)(n-2)$$

$$\frac{4^{n-3} e^{4(n-3)x} \cdot 6 \cdot 6}{3 \times 2}$$

$$= 4^n e^{4nx} x^3 + n 4^{n-1} e^{4(n-1)x} 3x^2 + n(n-1) 4^{n-2} e^{4(n-2)x} 3x + n(n-1)(n-2) 4^{n-3} e^{4(n-3)x}$$

$$= 4^{n-3} e^{4nx} [4^3 x^3 + n 4^2 3x^2 + n(n-1) 4 \cdot 3x + n(n-1)(n-2)]$$

$$= 4^{n-3} e^{4nx} [64x^3 + n 48x^2 + 12(n-1)x + n(n-1)(n-2)]$$

$$y^3 = 4^{3-3} e^{4 \cdot 3x} [64x^3 + (5 \times 48)x^2 + 12 \times 5(n-1)x + 5(5-1)(5-2)]$$

$$y^3 = 16e^{12x} [64x^3 + 240x^2 + 240x + 60]$$

$$) x^2 \frac{d^2 y}{dx^2} + x \frac{dy}{dx} + y = 0$$

$$x^2 y'' + x y' + y = 0$$

$$w_1 = x^2 y''$$

$$U^0 = V - y''$$

$$V^1 = y''' \quad V^2 = y^{(4)}$$

$$U^n = y^n + 2$$

$$w_2 = x y'$$

$$U^0 = U = y'$$

$$V = x, V^1 = 1, V^2 = 0$$

$$V^1 = y'' \quad U^2 = y'$$

$$U^1 = y'' \quad V^2 = y^{(4)}$$

$$u^n = y^{n+1}$$

$$w_1 = y$$

$$u = y$$

$$v = 1, v' = 0$$

$$u' = y', u'' = y''$$

$$u^n = y^n$$

$$w_1'' = 1^n [0 \cdot u^n - 0 \cdot v'' + n(n-1) u^{n-2} v'^2 + n(n-1) u^{n-2} v'' + 2n u^{n-1} v' u']$$

$$= y^{n+2} v + n y^{n+1} 2x + \frac{n(n-1)}{2} y^n x^2$$

$$= y^{n+2} v + n y^{n+1} 2x + (n-1)n y^n$$

$$= y^n [y^2 x^2 + n y^2 + n(n-1)]$$

$$w_2'' = n [0 \cdot u^{n-2} v'' + n(n-1) u^{n-3} v'^2 + n(n-1) u^{n-3} v'' + 2n u^{n-2} v' u']$$

$$u^{n-3} v''$$

$$= u^n u'' + n u^{n-1} v' + \frac{(n-1)n}{2} u^{n-2} \cdot 0$$

$$= y^{n+1} x + n y^n + 0$$

$$= y^n (xy + n)$$

$$w_3'' = 0 [0 \cdot u^{n-0} v'' + n(n-1) u^{n-1} v']$$

$$= u^n v'' + 0$$

$$= y^n$$

$$x^2 y'' + x y' + y = 0$$

$$w_1 + w_2 + w_3 = 0$$

$$y^n [y^2 x^2 + n 2xy + n(n-1)] + y^n (xy + n) + y^n = 0$$

$$\text{At } x = 0$$

$$y^n n(n-1) + y^n n + y^n = 0$$

$$n(n-1) + n + 1 = 0$$

$$y^n - y^n (n-1) - n y^n$$

$$\text{at } n = 1$$

$$y = -0 - y'$$

$$y = -y'$$

$$\begin{aligned}
 &= x^2 y^{n+2} + n^2 x y^{n+1} + n(n-1) y^n + 2x y^{n+1} + n y^n + y^n = 0 \\
 &= x^{n+2} + 2x y^{n+1} (2n+1) + y^n (n^2 - n + n + 1) = 0 \\
 &= x^2 y^{n+2} + (2n+1) x y^{n+1} + (n^2 + 1) y^n = 0
 \end{aligned}$$