

FINBARRS-EZEMA BERNARD

ASSIGNMENT 1

16/ENG03/027

CIVIL ENGINEERING

ENG382

Finbarrs - Ezema Bernard
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Civil Engineering
ENG 382

2/02/19

A flat plate of mass m falling freely in air with velocity V is subjected to a downward gravitational force and an upward frictional drag force due to air. If the drag force, f_0 is given by Equation (1)

$$f_0 = \frac{0.3V^2}{500 + (\ln V)^3} - 0.02V$$

and the terminal velocity is reached when the drag force equals the gravitational force, that is $f_0 = mg$ taking the values of m and g to be 3.5kg and 9.8m/s^2 respectively, using a guess value of $V_0 = 0.5\text{m/s}$, and employing fixed point iteration method, develop a MATLAB program to estimate the terminal velocity. Take the absolute percentage relative error tolerance to be less than or equal to $1\text{E}-11$.

Solution

$$F_0 = \frac{0.3V^2 - 0.02V}{500 + (\ln V)^3}$$

$$f_0 = \frac{0.3V^2}{500 + (\ln V)^3} - 0.02V = f(V)$$

$$m = 3.5\text{kg}$$
$$g = 9.81\text{m/s}^2$$
$$f_0 = mg$$

$$= 3.5 \times 9.81$$

$$f_D = 34.3 \text{ N}$$

Making V subject of formula

$$(0.02V + 34.3) = \frac{0.3V^2}{500 + (\ln V)^3}$$

$$(0.02V + 34.3)(500 + (\ln V)^3) = 0.3V^2$$

$$(0.02V + 34.3)500 + (0.02V + 34.3)((\ln V)^3) = 0.3V^2$$

$$(0.02V + 34.3)((\ln V)^3) = 0.3V^2 - (0.02V + 34.3)500$$

$$(\ln V)^3 = \frac{0.3V^2 - (0.02V + 34.3)500}{0.02V + 34.3}$$

$$V = e^{\left(\left(\frac{0.3V^2 - 10V - 17150}{0.02V + 34.3} \right)^{1/3} \right)}$$

$$V_{i+1} = e^{\left(\left(\frac{0.3V_i^2 - 10V_i - 17150}{0.02V_i + 34.3} \right)^{1/3} \right)}$$

MATLAB CODE

```
commandwindow
```

```
clear
```

```
clc
```

```
syms v
```

```
v=0.5;
```

```
for i=1:50
```

```
    iter(i+1)=i
```

```

v(i+1)=exp((((0.3*(v(i))^2)-10*v(i)-17150)/(0.02*v(i)+34.3))^(1/3))
Ea(i+1)=abs((v(i+1)-v(i))/v(i+1))*100
if Ea(i+1)<=1E-11
    break
end
end
v'
iter'
Ea'
tablo=[iter' v' Ea']

```

COMMAND WINDOW

tablo =

```

0.0000 + 0.0000i  0.5000 + 0.0000i  0.0000 + 0.0000i
1.0000 + 0.0000i  43.9475 -29.4542i  99.2163 + 0.0000i
2.0000 + 0.0000i  50.4454 -26.8898i  12.2200 + 0.0000i
3.0000 + 0.0000i  50.6792 -24.9333i  3.4887 + 0.0000i
4.0000 + 0.0000i  50.1890 -24.6434i  1.0186 + 0.0000i
5.0000 + 0.0000i  50.0588 -24.7398i  0.2901 + 0.0000i
6.0000 + 0.0000i  50.0695 -24.7843i  0.0820 + 0.0000i
7.0000 + 0.0000i  50.0823 -24.7865i  0.0232 + 0.0000i
8.0000 + 0.0000i  50.0843 -24.7834i  0.0066 + 0.0000i
9.0000 + 0.0000i  50.0837 -24.7825i  0.0019 + 0.0000i
10.0000 + 0.0000i  50.0834 -24.7826i  0.0005 + 0.0000i
11.0000 + 0.0000i  50.0834 -24.7827i  0.0001 + 0.0000i
12.0000 + 0.0000i  50.0834 -24.7827i  0.0000 + 0.0000i
13.0000 + 0.0000i  50.0834 -24.7827i  0.0000 + 0.0000i
14.0000 + 0.0000i  50.0834 -24.7827i  0.0000 + 0.0000i
15.0000 + 0.0000i  50.0834 -24.7827i  0.0000 + 0.0000i

```

16.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
17.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
18.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
19.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
20.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
21.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
22.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
23.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
24.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i
25.0000 + 0.0000i 50.0834 -24.7827i 0.0000 + 0.0000i