

NAME: Tanilayo Alulco

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MECHATRONICS ENGINEERING

Assignment 2

$$F(x) = e^{-0.5x} (4-x) - 2$$

* Using Newton Raphson Method

$$x = g(x)$$

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$$

$$F(x) = e^{-0.5x} (4-x) - 2$$

$$f'(x) = e^{-0.5x} (-3 + x/2)$$

* Initial guess value of 0.5 Hence; $x_i = 0.5$

①

$$f(0.5) = e^{-0.5(0.5)} (4-0.5) - 2 = 0.7258027407$$

$$f'(0.5) = (0.5-6) e^{-0.5(0.5)} / 2 = -2.141702133$$

$$x_{i+1} = 0.5 - \frac{0.7258027407}{-2.141702133} = 0.838890606$$

②

$$f(0.84) = e^{-0.5(0.84)} (4-0.84) - 2 = 0.07814929794$$

$$f'(0.84) = (0.84-6) e^{-0.5(0.84)} / 2 = -1.696486032$$

$$x_{i+1} = 0.838890606 - \frac{0.07814929794}{-1.696486032} = 0.884956003$$

③

$$f(0.885) = e^{-0.5(0.885)} (4-0.885) - 2 = 0.00123657519$$

$$f'(0.885) = (0.885-6) e^{-0.5(0.885)} / 2 = -1.643060762$$

$$x_{i+1} = 0.884956003 - \frac{0.00123657519}{-1.643060762} = 0.885708605$$

④

$$f(0.886) = e^{-0.5(0.886)} (4-0.886) - 2 = 0.000000323521408$$

$$f'(0.886) = (0.886-6) e^{-0.5(0.886)} / 2 = -1.642200929$$

$$x_{i+1} = 0.885708605 - \frac{0.000000323521408}{-1.642200929} = 0.885708802$$

MATLAB CODE FOR NEWTON-RHAPSON METHOD

Function $[x_1, err, relerr] = ass2(x_0, Max1, tol, iter, f, fprime)$

$x_0 = 0.5;$

$Max1 = 100;$

$tol = 0.000000001;$

$iter = 1$

$f = @(x)((\exp(-0.5 * x)) * (4 - x))^{-2};$

$fprime = @(x)(-\exp(-0.5 * x)) + ((-0.5 * \exp(-0.5 * x)) * (4 - x));$

for $i = 1 : Max1$,

$x_1 = x_0 - \text{feval}(f, x_0) / \text{feval}(fprime, x_0);$

$err = \text{abs}(x_1 - x_0); relerr = \text{abs}(x_1 - x_0) / x_1;$

$fprint f ('%2.0f %10.10f %10.10f %10.10f %10.10f \n')$
 $iter, x_0, x_1, err, relerr)$

$x_0 = x_1, iter = 1 + iter;$

if $err \leq tol$,

break

end

end