

A Plate (leaf) of mass is falling freely in air with Velocity V is subjected to a downward gravitation force and an upward frictional drag force due to air. If the drag force, F_D is given by equ (1)

$$F_D = \frac{0.3V^2}{500 + (\ln V)^3} - 0.02V \quad \text{--- (1)}$$

and the terminal Velocity is reached when the drag force equals the gravitational force, that is; $F_D = mg$. Taking the values of m and g to be 3.5 kg and 9.8 m/s^2 respectively, Using a guess value of $V_0 = 0.5 \text{ m/s}$ { employs Fixed-Point Iteration method, develop a MATLAB Program to estimate the terminal velocity. Also develop a MATLAB Program to estimate the terminal Velocity. Take the absolute Percentage relative error tolerance to be less than or equal to $1E-11$

Sol

$$F_D = \frac{0.3V^2}{500 + (\ln V)^3} - 0.02V \quad \text{--- (1)}$$

$$F_D = mg = 3.5 \times 9.8 = 34.3 \quad \text{--- (2)}$$

equating equ 1 & 2

$$mg = 34.3 = \frac{0.3V^2}{500 + (\ln V)^3} - 0.02V$$

making V^2 Subject of formula

$$34.3 + 0.02V = \frac{0.3V^2}{500 + (\ln V)^3}$$

$$0.3 V^2 = 34.3 + 0.02V \times (500 + (\ln V)^3)$$

$$V^2 = \frac{(34.3 + 0.02V) \times (500 + (\ln V)^3)}{10.3}$$

$$V = \sqrt{(34.3 + 0.02V) \times (500 + (\ln V)^3) / 10.3}$$

Initial guess value $\Rightarrow V_0 = 0.5 \text{ m/s}$ Absolute %

relative error, $\epsilon_a(1.1) \leq 1E-11$