

Engineering Math Assignment II

Submitted by:

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If the maximum percentage absolute error is desired to be $1E-9$, using the Newton-Raphson iteration method and initial ^{guess} value of 0.5, find the root of the function given below

$$f(x) = e^{-0.5x} (4-x) - 2$$

Solution

$$f(x) = e^{-0.5x} (4-x) - 2$$

$$f'(x) = -e^{-0.5x} - 0.5e^{-0.5x} (4-x)$$

$$f''(x) = -e^{-0.5x} - 2e^{-0.5x} + 0.5e^{-0.5x}$$

$$f(x) = e^{-0.5x} (4-x) - 2$$

$$f'(x) = 0.5xe^{-0.5x} - 3e^{-0.5x}$$

$$\cancel{x_{i+1} = x_i +}$$

$$x_{i+1} = x_i - \frac{f(x_i)}{f'(x_i)}$$

where $x = 0.5$

$$x_1 = 0.5 \left(\frac{e^{-0.5 \times 0.5} (4 - 0.5) - 2}{(0.5 \times 0.5 e^{-0.5 \times 0.5}) - (3e^{-0.5 \times 0.5})} \right)$$

$$x_1 = 0.858890$$

$$x_2 = 0.858890 - \frac{e^{-0.5 \times 0.858890} (4 - 0.858890) - 2}{(0.5 \times 0.858890 e^{-0.5 \times 0.858890}) - (3e^{-0.5 \times 0.858890})}$$
$$= 0.88496$$

$$x_3 = 0.88496 - \frac{e^{-0.5 \times 0.88496} (4 - 0.88496) - 2}{(0.5 \times 0.88496 e^{-0.5 \times 0.88496}) - (3e^{-0.5 \times 0.88496})}$$
$$= 0.88570$$

When $x = 0.88570$

$$x_7 = 0.88570 - \left(\frac{e^{-0.5 \times 0.88570} (4 - 0.88570) - 2}{(0.5 \times 0.88570 e^{-0.5 \times 0.88570}) - (3e^{-0.5 \times 0.88570})} \right)$$

$$= 0.88571$$

When $x_7 = 0.88571$

$$x_8 = 0.88571 - \left(\frac{e^{-0.5 \times 0.88571} (4 - 0.88571) - 2}{(0.5 \times 0.88571 e^{-0.5 \times 0.88571}) - (3e^{-0.5 \times 0.88571})} \right)$$

$$= 0.88571$$

When $x_8 = 0.88571$

$$x_9 = 0.88571 - \left(\frac{e^{-0.5 \times 0.88571} (4 - 0.88571) - 2}{(0.5 \times 0.88571 e^{-0.5 \times 0.88571}) - (3e^{-0.5 \times 0.88571})} \right)$$

$$= 0.88571$$

For error

$$E_0 = \left| \frac{x_{i+1} - x_i}{x_{i+1}} \right| \times 100$$

$$E_0 = \frac{0.888890 - 0.5}{0.888890} \times 100 = 40.897\%$$

$$E_{02} = \frac{0.88496 - 0.888890}{0.888890} \times 100 = 5.205\%$$

$$E_{03} = \frac{0.88571 - 0.88570}{0.88571} \times 100 = 2.224 \times 10^{-5}\%$$

$$E_{03} = \frac{0.88570 - 0.88496}{0.88570} \times 100 = 0.0849\%$$

$$E_{04} = \frac{0.88571 - 0.88570}{0.88571} \times 100 = 2.224 \times 10^{-5}\%$$

$$E_{05} = \frac{0.88571 - 0.88571}{0.88571} \times 100 = 0\%$$

i	x	$\Sigma_0 (\%)$
0	0.5	40.397
1	0.938890	5.205
2	0.88496	0.0849
3	0.88570	2.224×10^{-5}
4	0.88571	0
5	0.88571	0

MathLab Code

```
commandwindow
clear
clc
format short g
syms x
a=(exp(-0.5*x))*((4-x))-2
b=diff(a)
x=0.5;
xa=x
for i=1:5
    iter(i+1)=i
    x= double(subs(x-(a/b)))
    xa(i+1)=x
    ea(i+1)=abs(( xa(i+1)-xa(i))/xa(i+1))*100
    if ea(i+1)<=1E-9
        break
    end
end
tab=[iter' ea' xa']
```

Output

a =

- exp(-x/2)*(x - 4) - 2

b =

(exp(-x/2)*(x - 4))/2 - exp(-x/2)

xa =

0.5

iter =

0 1

x =

0.83889

xa =

0.5 0.83889

ea =

0 40.397

iter =

0 1 2

x =

0.88496

xa =

0.5 0.83889 0.88496

ea =

0 40.397 5.2054

iter =

0 1 2 3

x =

0.88571

xa =

0.5 0.83889 0.88496 0.88571

ea =

0 40.397 5.2054 0.084972

iter =

0 1 2 3 4

x =

0.88571

xa =

0.5 0.83889 0.88496 0.88571 0.88571

ea =

0 40.397 5.2054 0.084972 2.2247e-05

iter =

0 1 2 3 4 5

x =

0.88571

xa =

0.5 0.83889 0.88496 0.88571 0.88571 0.88571

ea =

```
0    40.397    5.2054    0.084972    2.2247e-05    1.5293e-12
```

```
tab =
```

```
0      0      0.5
1    40.397    0.83889
2     5.2054    0.88496
3    0.084972    0.88571
4    2.2247e-05    0.88571
5    1.5293e-12    0.88571
```

```
>>
```