

Assignment 2

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16/Eng06/007

Mechanical

ENG382

If the maximum percentage absolute error is desired to be 1×10^{-9} , using the Newton-Raphson iteration method and initial guess value of 0.5, find the root of the function given in eqn (1-1)

(a) Manually and

(b) With the aid of MATLAB

Sol

$$(a) f(x) = e^{-0.5x}(4-x) - 2$$

$$f'(x) =$$

$$\text{Let } u = e^{-0.5x} \text{ \& } v = (4-x)$$

$$S_u = -0.5e^{-0.5x}; S_v = -1$$

$$f'(x) = -e^{-0.5x} - 0.5e^{-0.5x}(4-x)$$

$$x_0 = 0.5 \text{ [Initial Guess]}$$

General Newton Raphson Formula

$$x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$$

$$f(x_0) = f(0.5) = 0.725827407$$

$$f'(x_0) = f'(0.5) = -2.141702153$$

$$x_1 = x_0 - \frac{f(x_0)}{f'(x_0)} = 0.8388906061$$

$$f(x_1) = 0.0781429779$$

$$f'(x_1) = -1.642200929$$

$$x_2 = x_1 - \frac{f(x_1)}{f'(x_1)} = 0.885708802$$

$$f(x_2) = 7.875 \times 10^{-3}$$

$$f'(x_2) = -1.642200704$$

$$x_3 = x_2 - \frac{f(x_2)}{f'(x_2)} = 0.885708802$$



• Features
• Specs
• Support

SCAN

Standard data rates may apply

MATLAB

1. \square Function [x1, err,] = (x0, maxI, tol, iter, f_prime)

x0 = 0.5;

max I = 100;

tol = 0.0000000001;

iter = 1

f = (a)(x) [exp(-0.5 * x)] * (4-x) - 2;
f_prime = (a)(x) [-exp(-0.5 * x)] * [0.5 * exp(-0.5 * x)] * (4-x);

\square for i = 1 : max I
x1 = x0 - feval(f, x0) / feval(f_prime, x0);

err = abs(x1 - x0); verror = abs(x1 - x0) / x1;

f_prime = f (10.2 of 10.10 - 10 f 10.10 - 10 f 10.10 - 10.10 f ln, iter, x0, x1, err, verror)

x0 = x1, iter = 1 + iter;

ferr <= tol, break, end

end